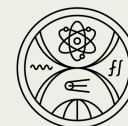


Analysis of Seismic Ambient Noise for Resonance Seismometry OSI Technique – the FISP Method

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Bratislava

Presentation Date: 11 September 2025

Outline

Motivation

FISP – methodology

FISP – applications

Conclusions



CTBTO on-site inspection team seeks cavities hundreds of meters underground

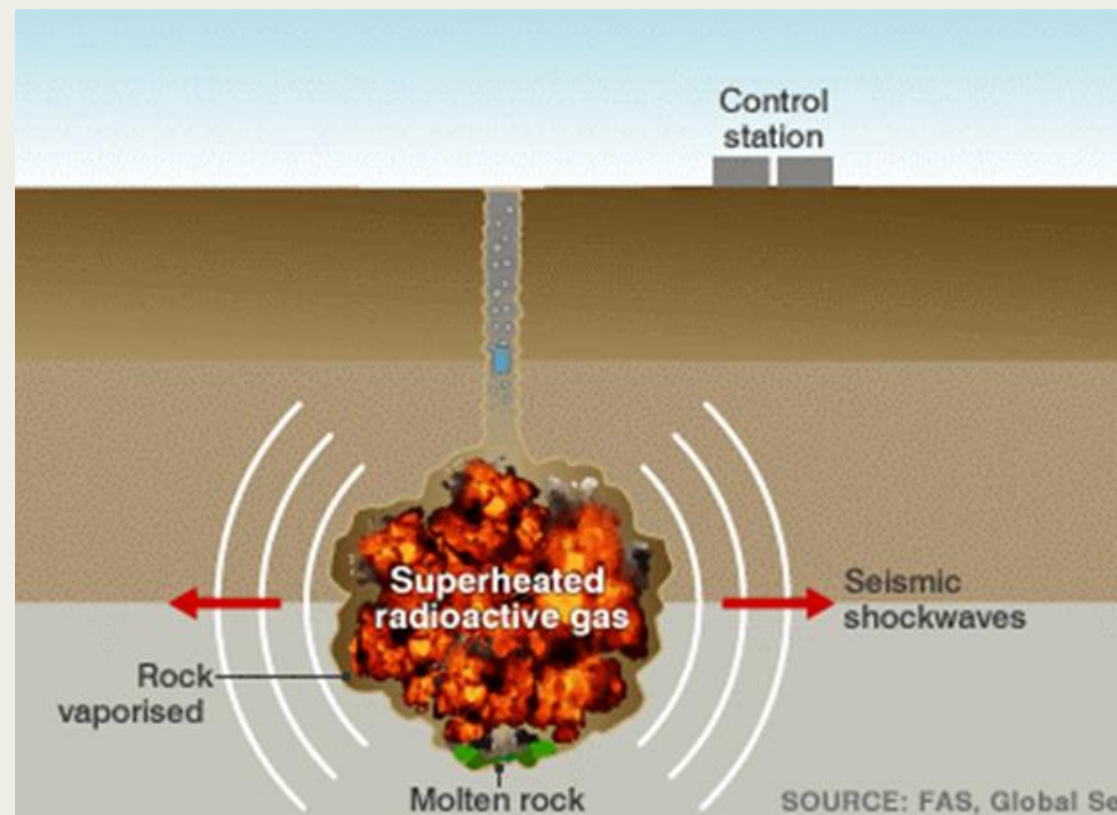
limited time for inspection

limited number of seismic stations

limited possibilities to deploy a large and dense array

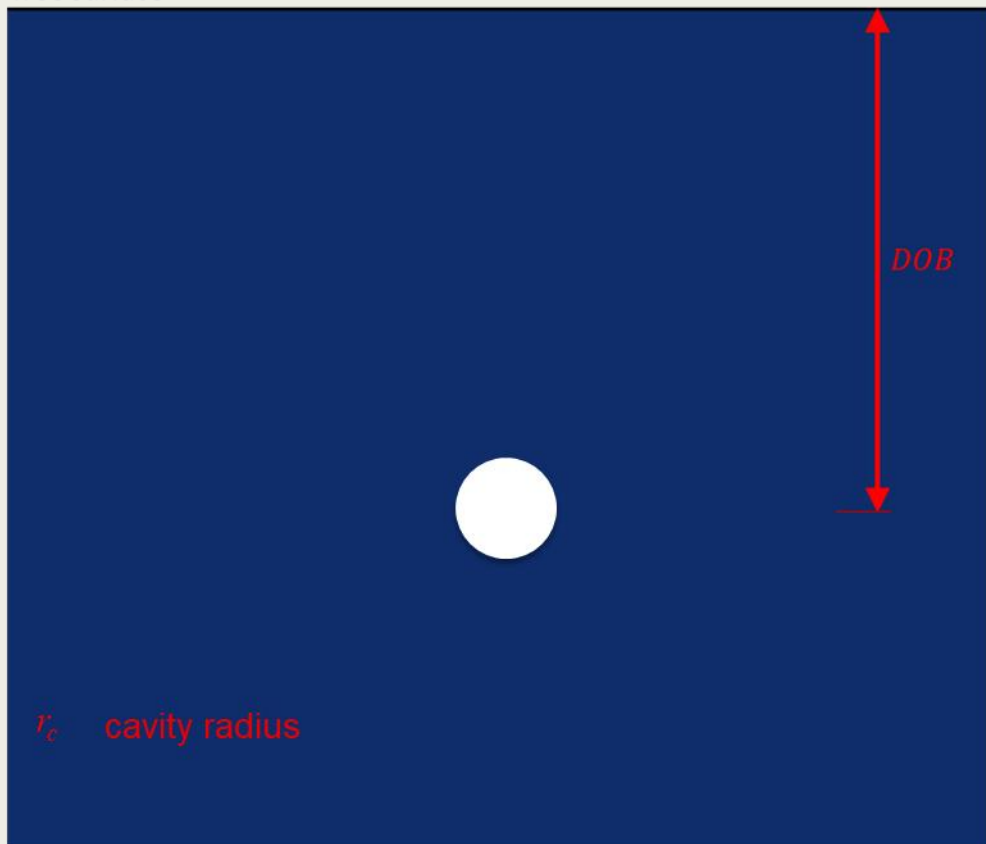


it is useful to have a robust method
utilizing seismic ambient noise
applicable to data from
single station (or a few stations) measurements

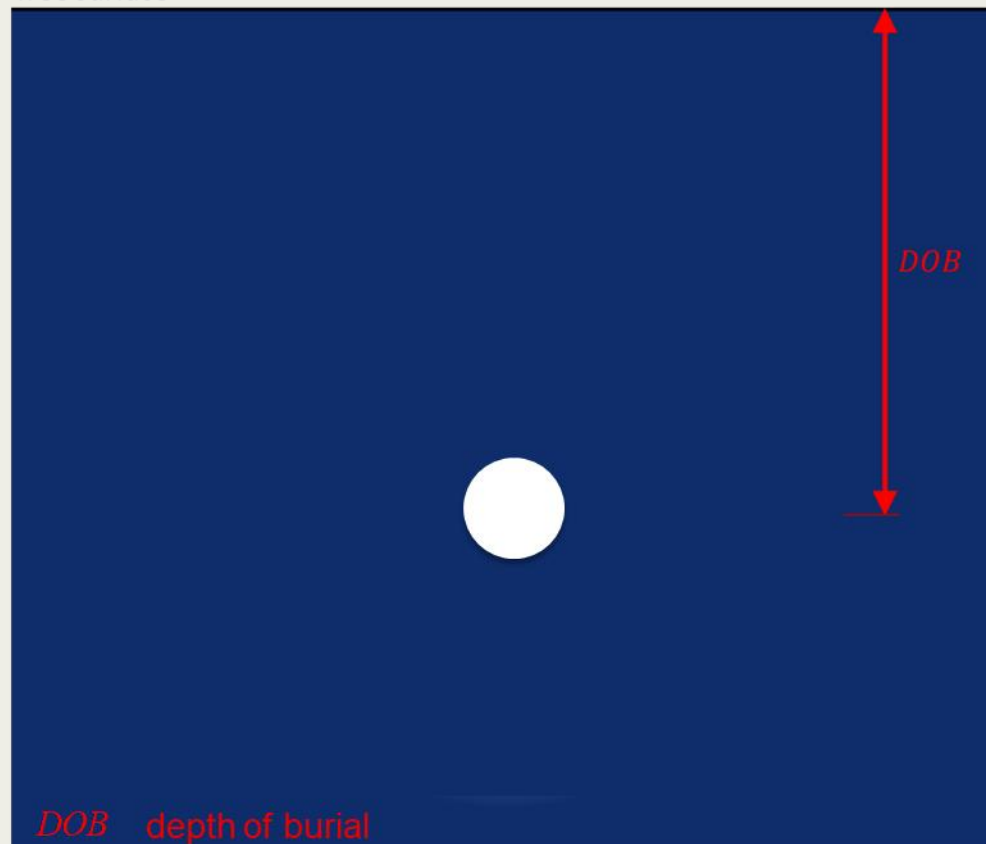


Structural Models for the Vertical Emplacement

free surface



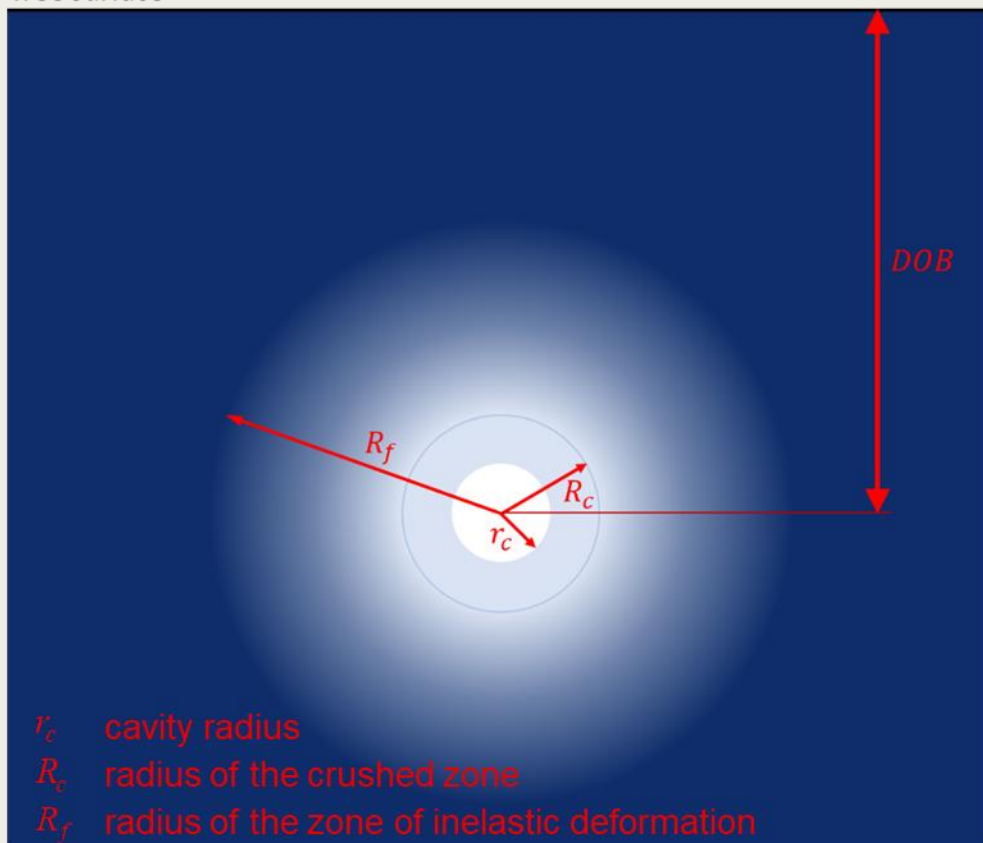
free surface



Structural Models for the Vertical Emplacement

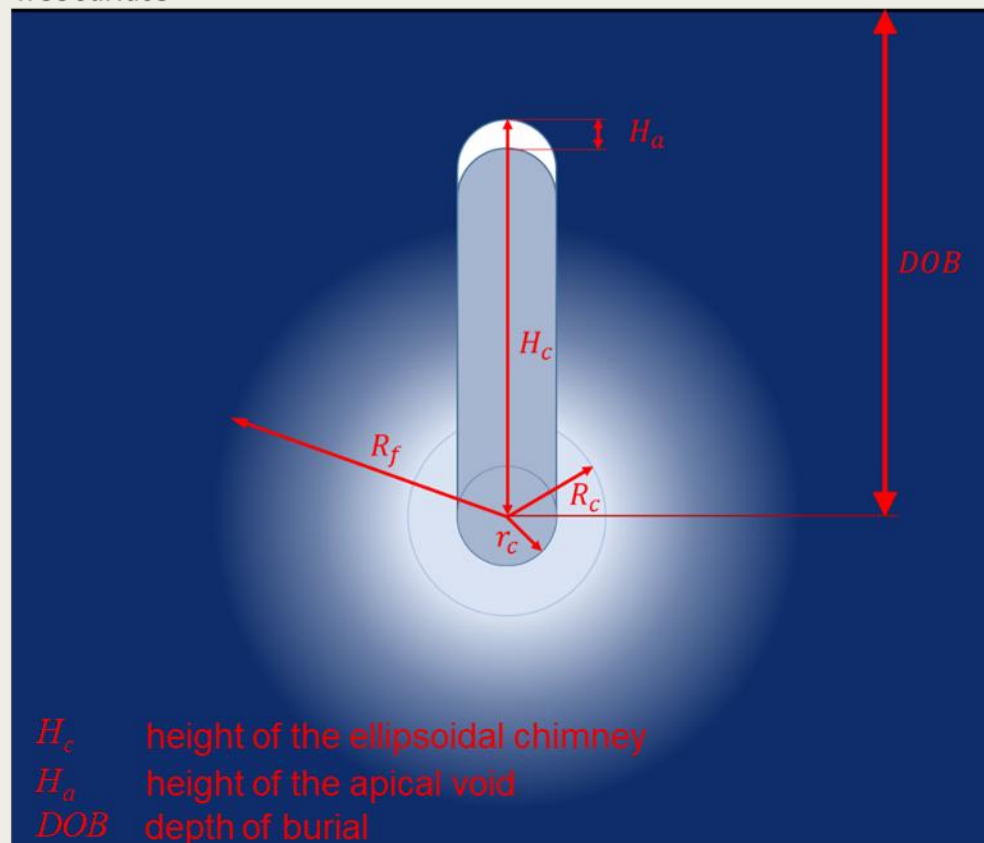
cavity without chimney (for plastic rock)

free surface



cavity with chimney filled with rubble + apical void

free surface



Result of Analysis of Synthetics

Amplitude Fourier spectra

averaged over
all 6400 receivers

tuff

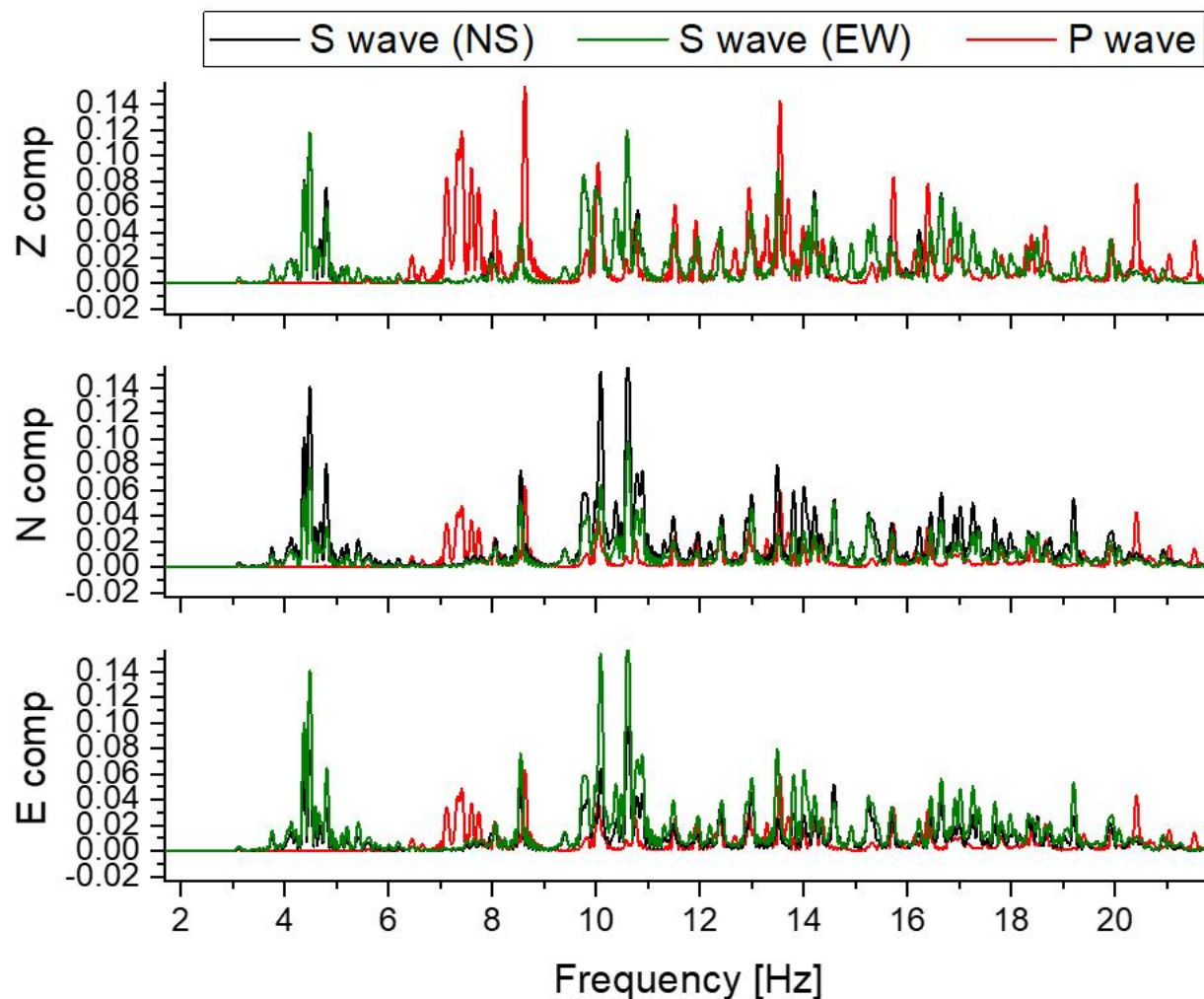
low yield (1kt)

GAS filling of apical void

minimal depth of burial
(180 m)

Select

- Type of excitation**
- ☒ plane waves
 - ☐ point double-couple sources



The Finite-Interval Spectral Power Method (FISP)

instead of problematic identification
of individual weak peaks
and
calculation of the corresponding spectral characteristics,
the FISP is based **on evaluation
of signal energy (spectral power)
within a finite-interval of frequencies**

Kristekova et al. 2021. Geophys. J. Int., 945-960



The Finite-Interval Spectral Power Method (FISP)

we proposed to evaluate spectral power
representing the entire reasonably selected frequency interval $[F_{min}, F_{max}]$

$$FISP_Z = \int_{F_{min}}^{F_{max}} \left| \tilde{X}^Z(f) \right|^2 df$$

$$FISP_H = \int_{F_{min}}^{F_{max}} \left| \tilde{X}^E(f) \right| \left| \tilde{X}^N(f) \right| df$$

$$\frac{FISP_H}{FISP_Z}$$

$\left| \tilde{X}^C(f) \right|^2$ is a smoothed power spectral density (PSD) of one component of noise

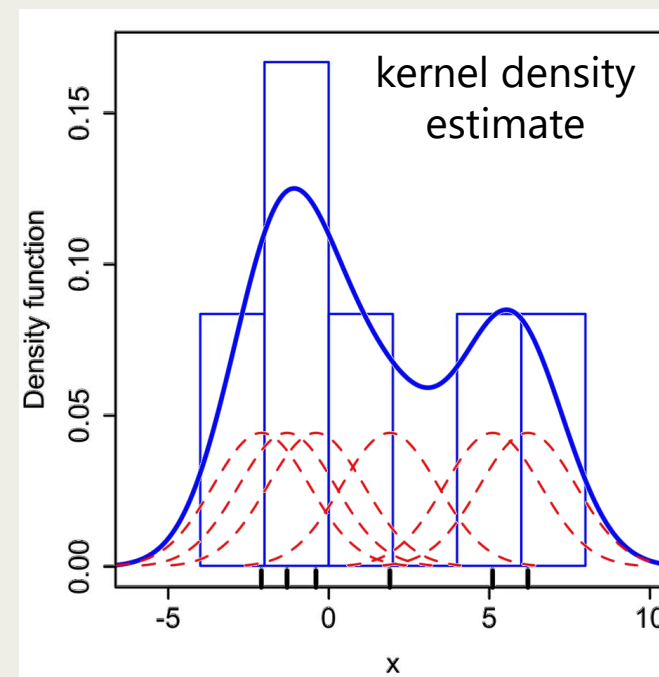


The Finite-Interval Spectral Power Method (FISP)

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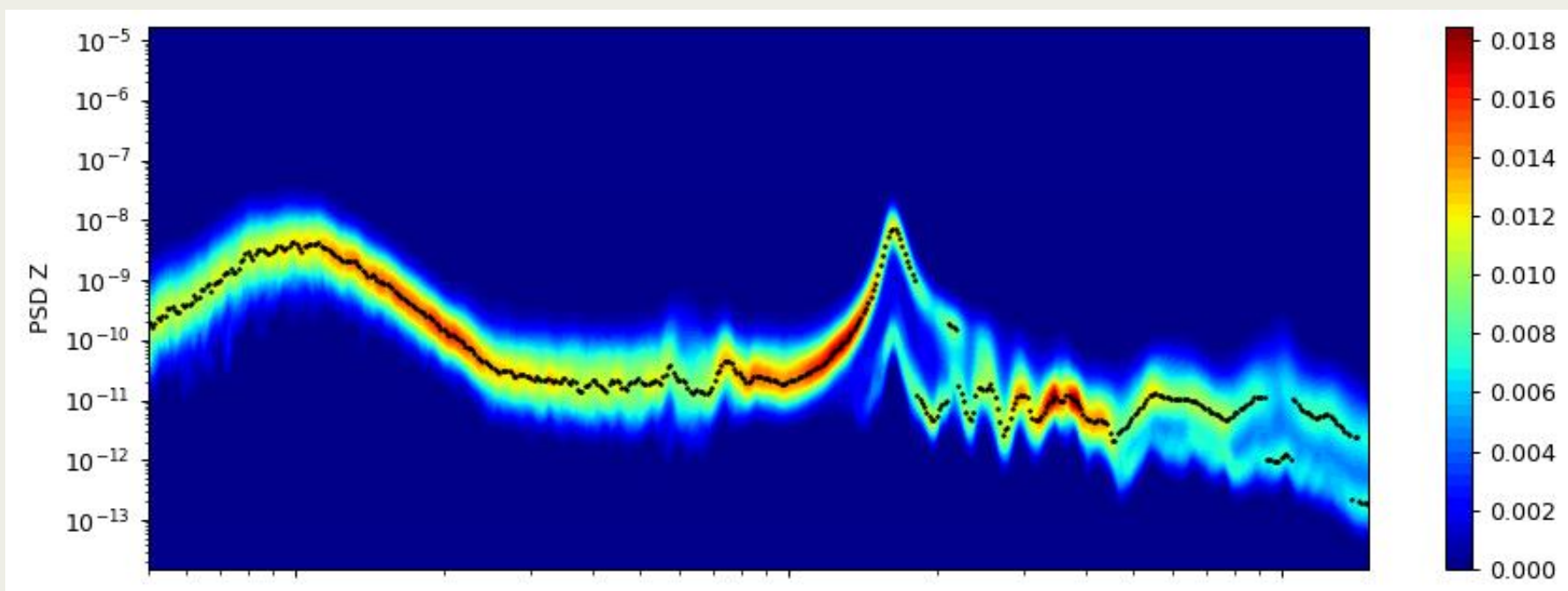
? how to estimate power spectral density (PSD)
in case of non-unimodal distribution?

$PSD(f) =$ the maximum of
kernel density estimate



The Finite-Interval Spectral Power Method (FISP)

we proposed to evaluate spectral power
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The Finite-Interval Spectral Power Method (FISP)

we proposed to evaluate spectral power
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the **coefficient of variation**

$$CV(f) = \sqrt{\exp[\sigma^2(f)] - 1}$$

quantifies the differences
between the segments
regardless of the value of PSD



$$SNR(f) = -10 \log_{10} CV(f)$$

is the **signal-to-noise ratio**
in decibels

the larger signal-to-noise ratio,
the smaller differences
between the segments
and therefore
more reliable measurement



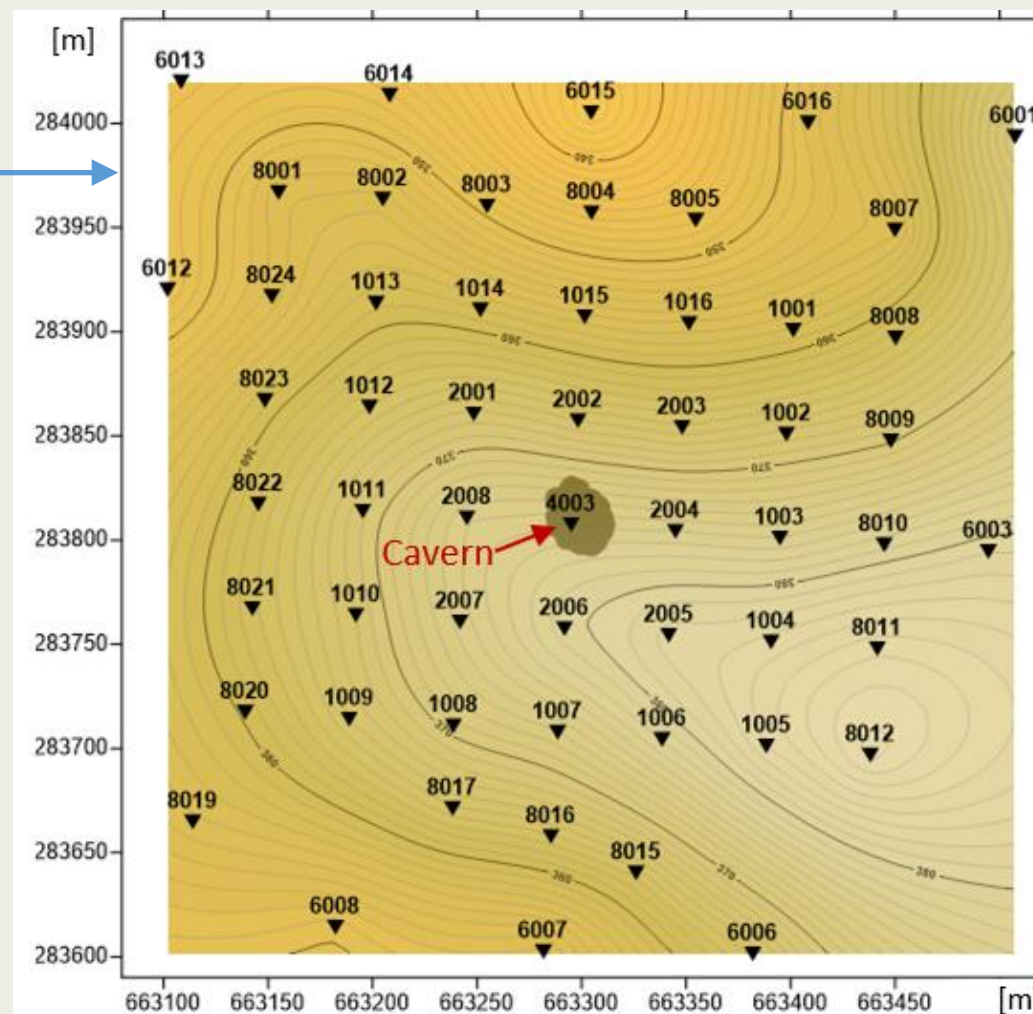
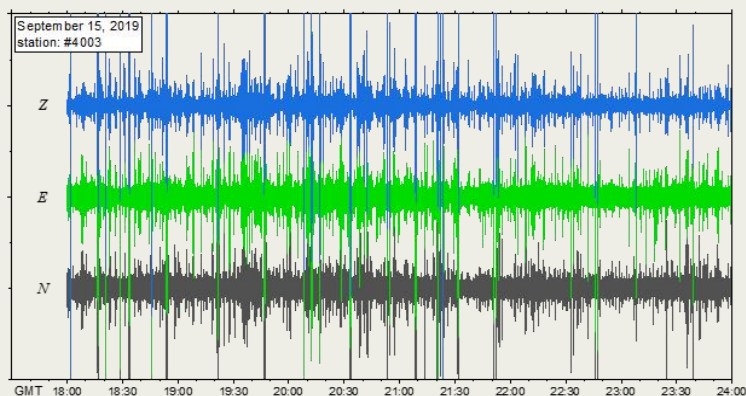
The Finite-Interval Spectral Power Method (FISP)

we assume

a set of measurement points
at the free surface
above a suspected cavity

and

sufficiently long
3-component records of noise
at all measurement points



Real-site application of FISP

Great Cavern, Hungary

roughly oval shape
horizontal span: 28 - 30 m
height: 25 - 28 m
depth (ceiling): ~70 m

Tiny Tot, NNSS, Nevada

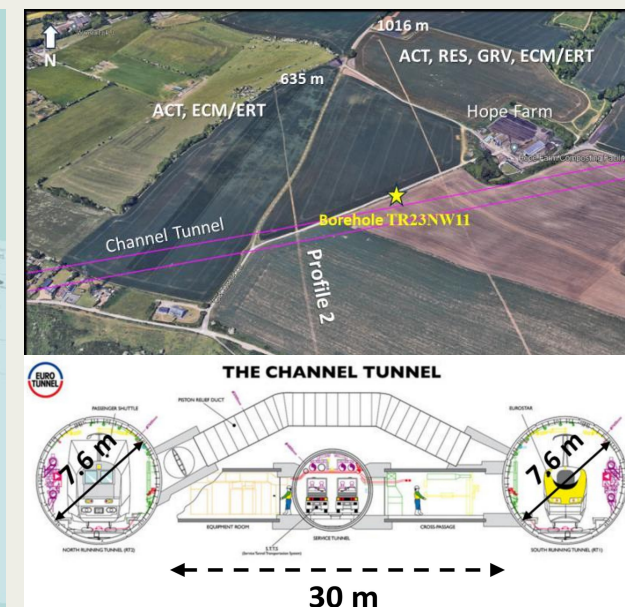
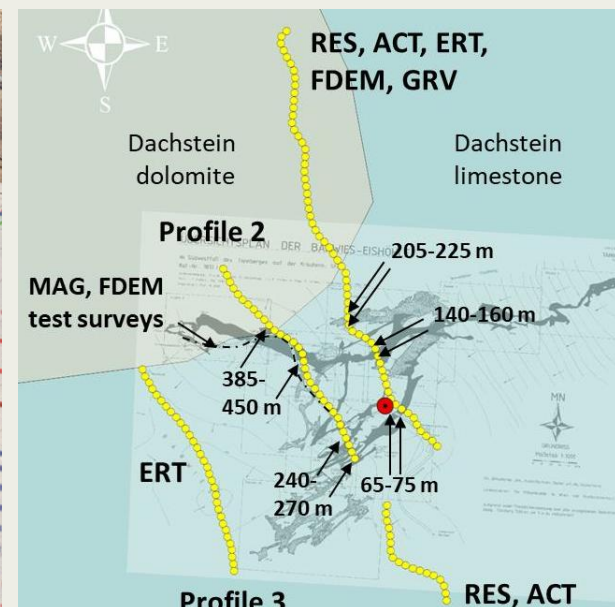
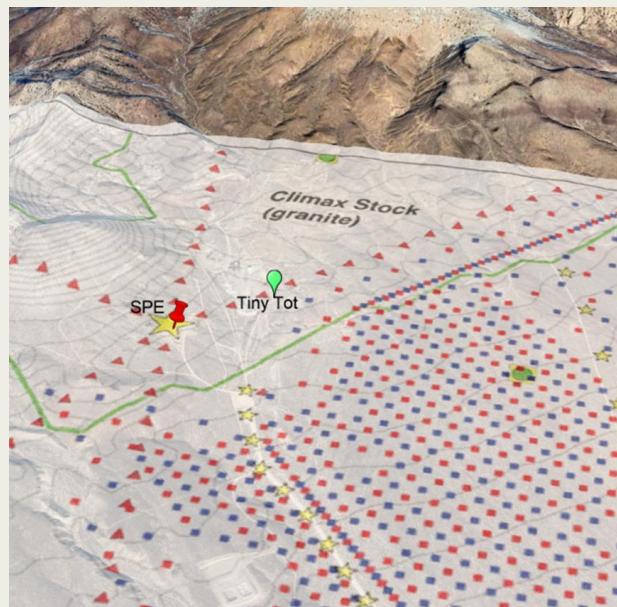
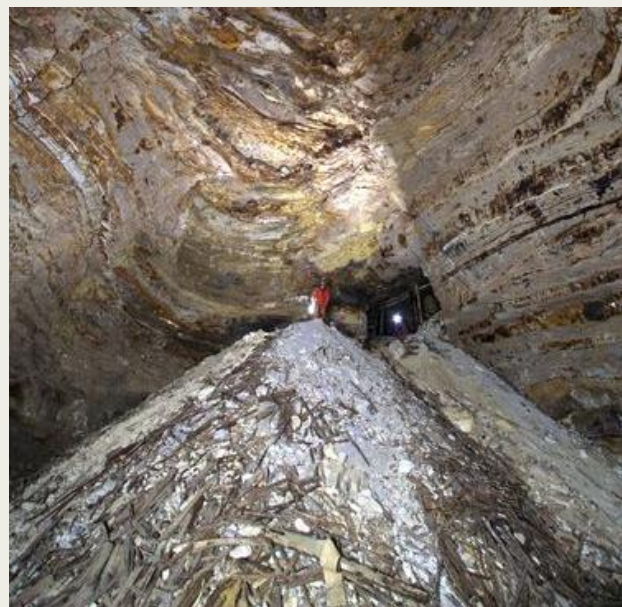
cavity from yield 20kT
horizontal span: ???
height: ???
depth: ~111 m

Rotmoos, Austria

karst area
horizontal span: ???
height: ???
depth: 60 - 450 m

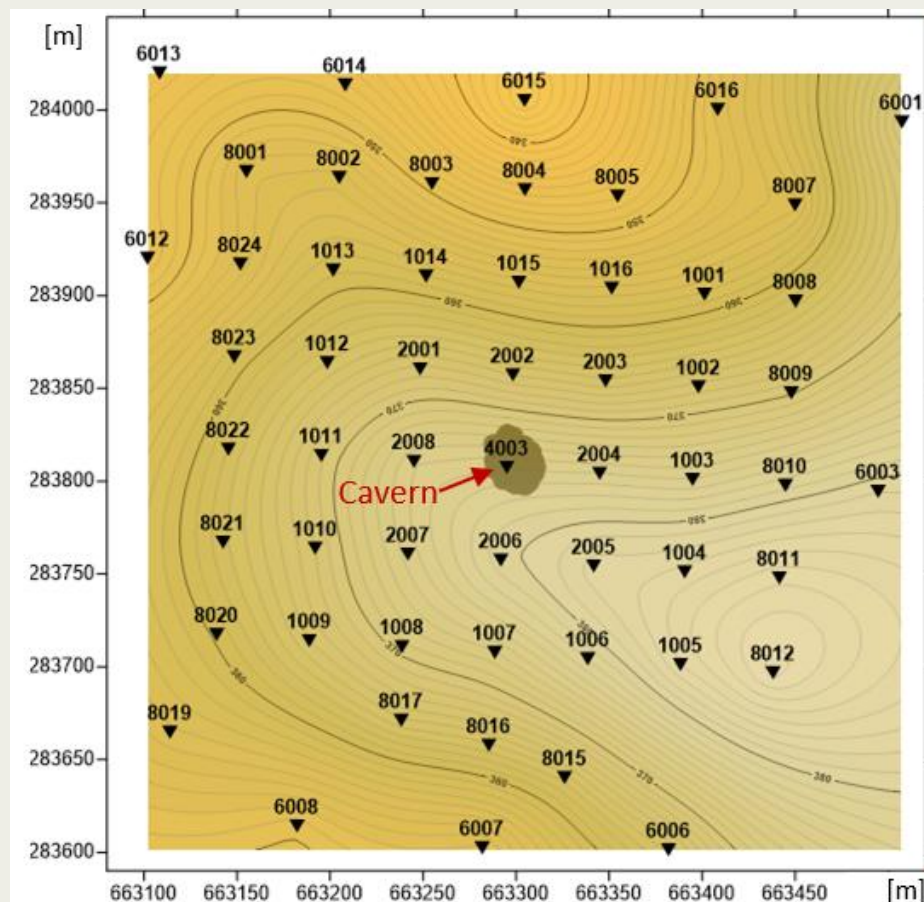
Channel Tunnel, UK

two tubes 30m apart
horizontal span: 46 m
height: 7.6 m
depth: ~90 m



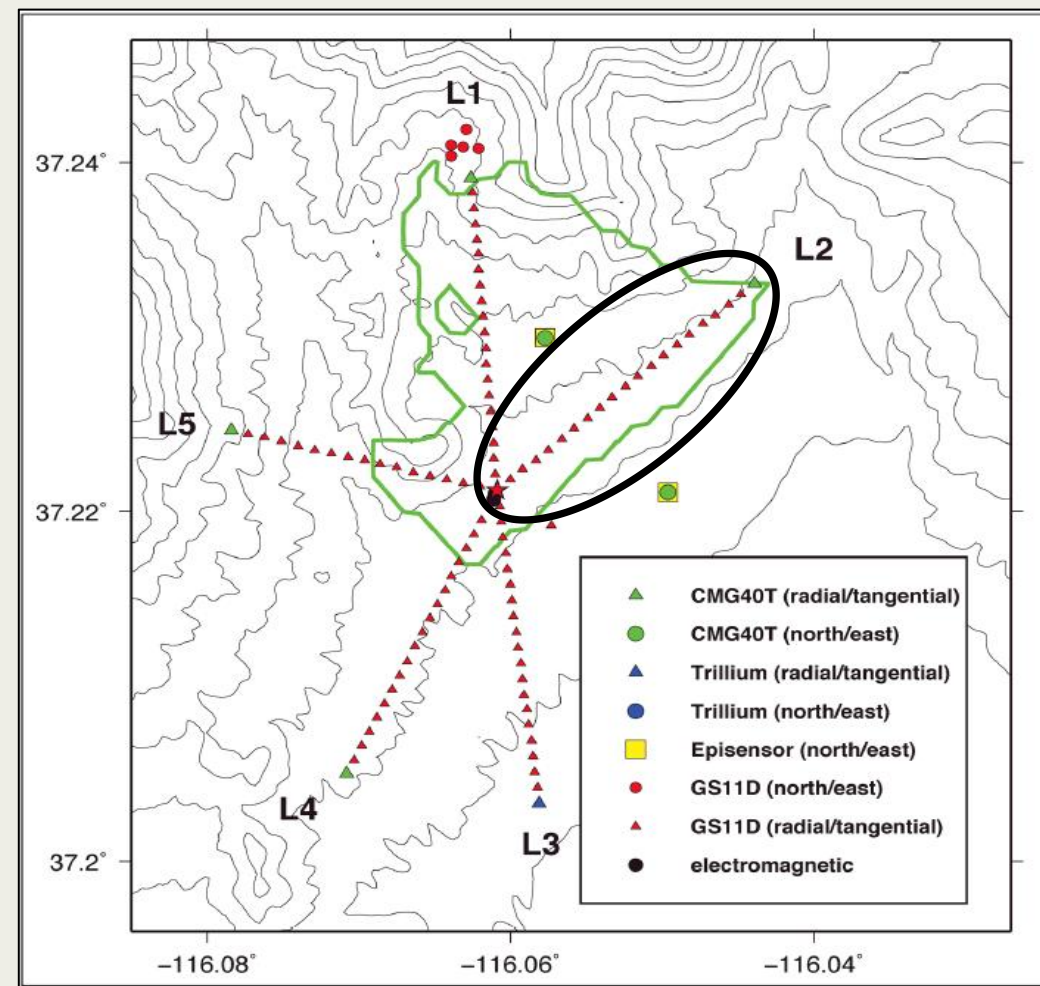
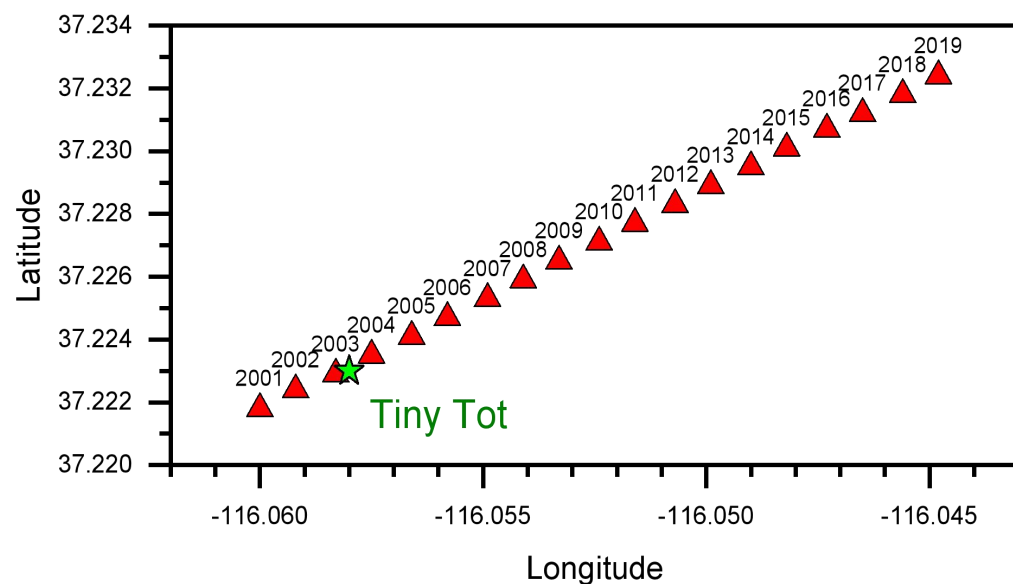
Real-site application of FISP – Great Cavern, Hungary

3-component records of noise
at 50 measurement points (interstation distance ~50 m)



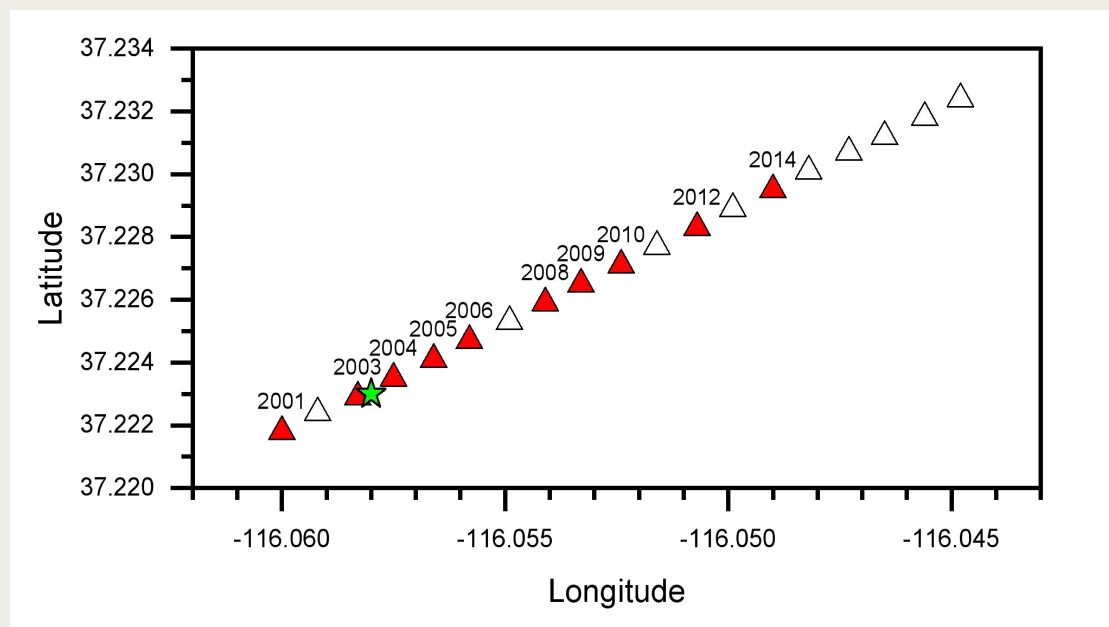
Real-site application of FISP – Tiny Tot, NNSS, Nevada

3-component records of noise
from SPE-5 and SPE-6

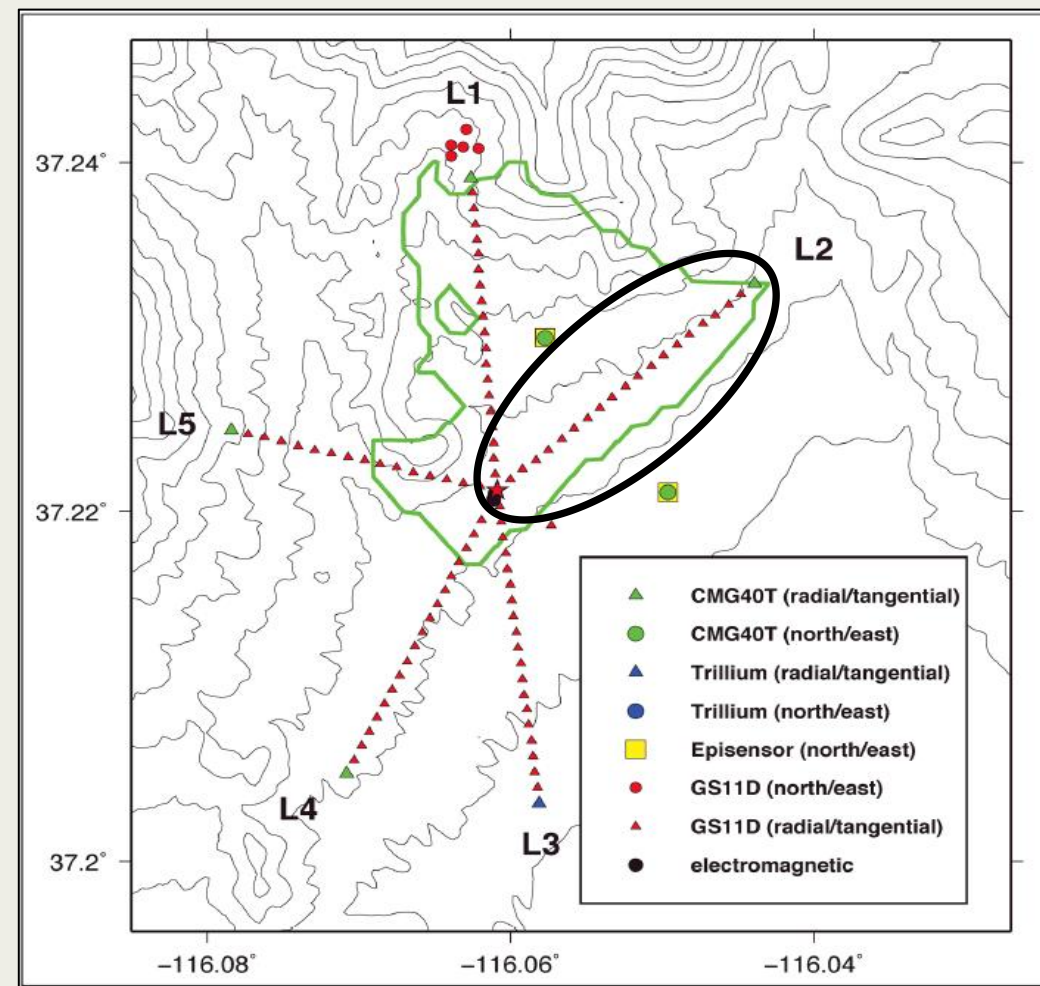


Real-site application of FISP – Tiny Tot, NNSS, Nevada

3-component records of noise
from SPE-5 and SPE-6

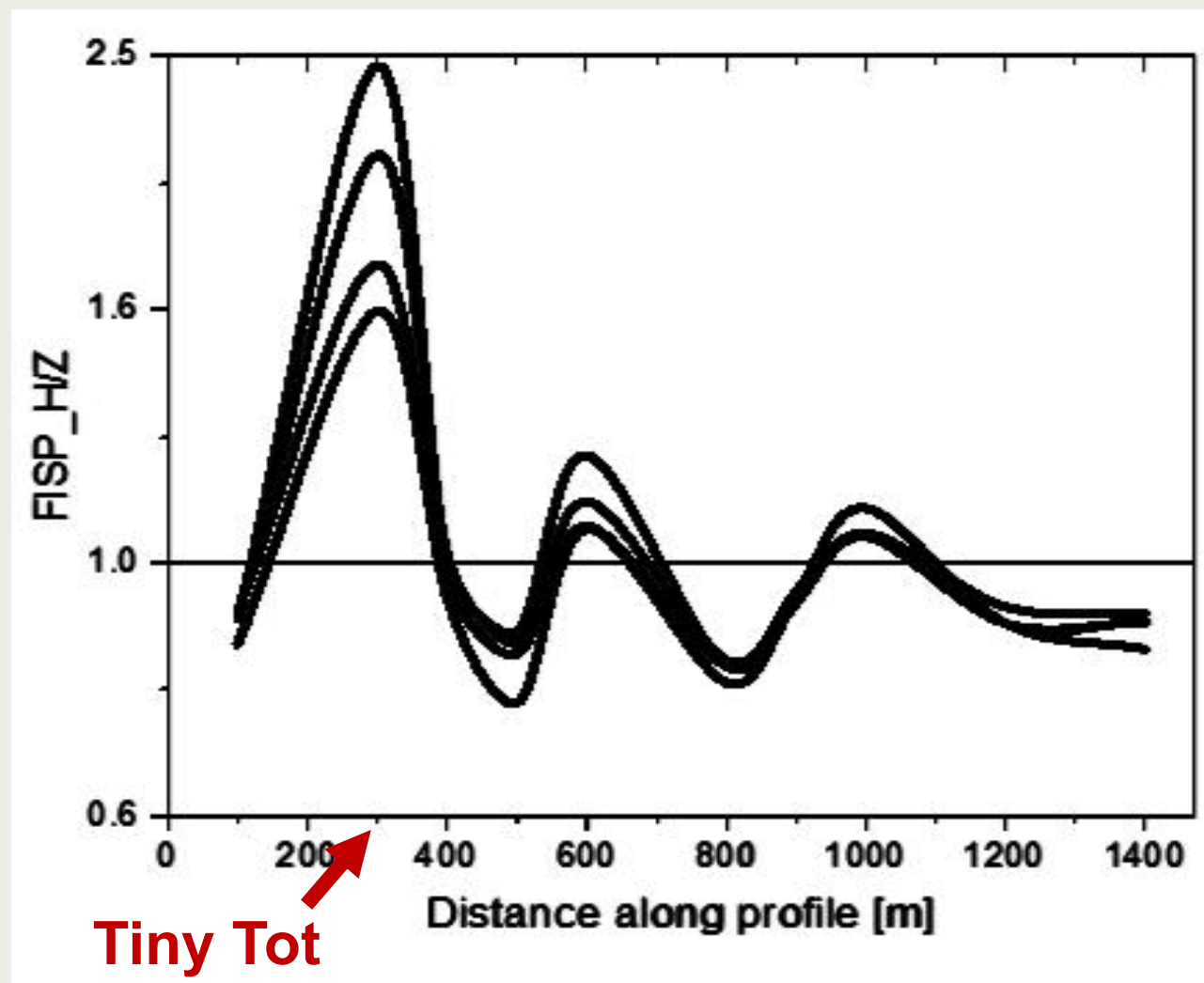


data from many receivers unusable either due to malfunction
or due to strong interference at most frequencies

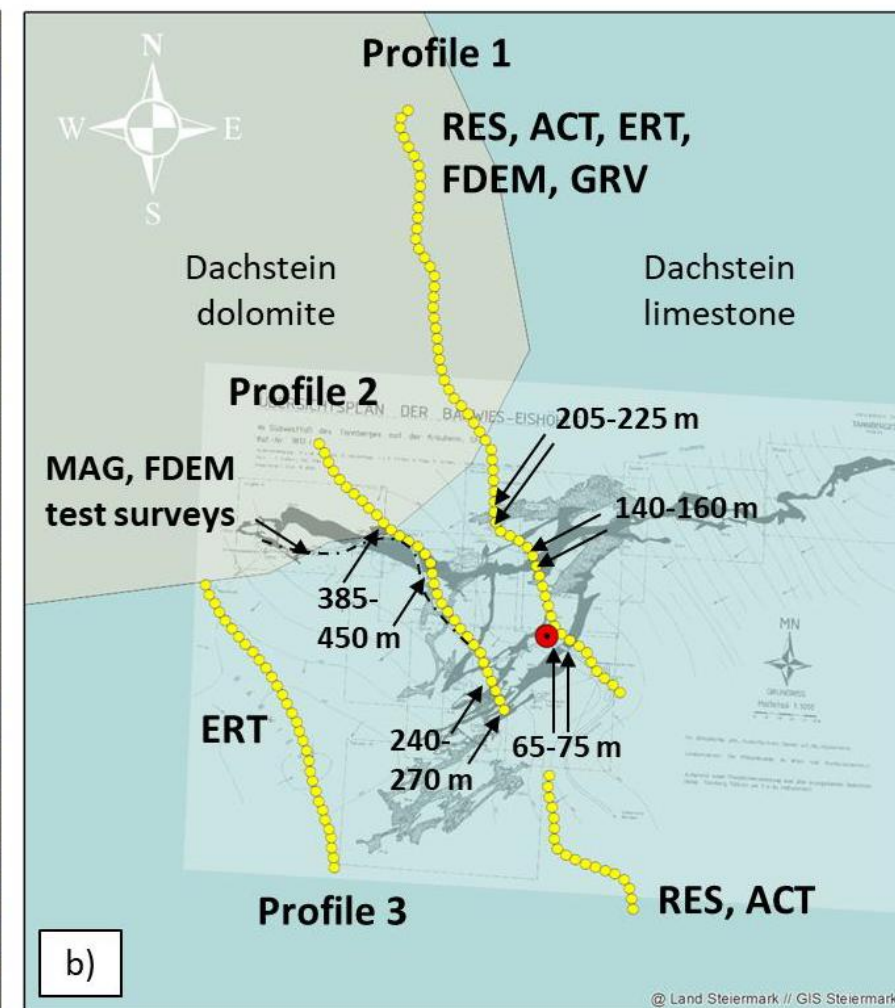
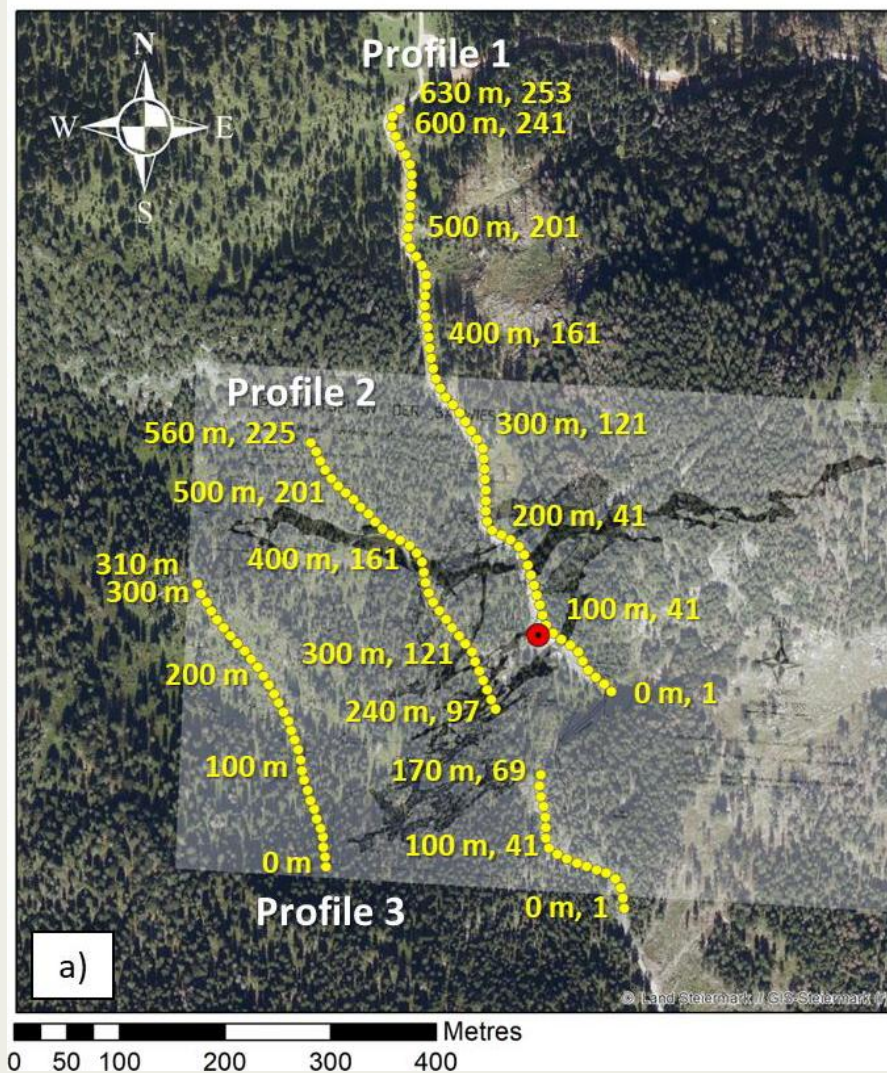


Real-site application of FISP – Tiny Tot, NNSS, Nevada

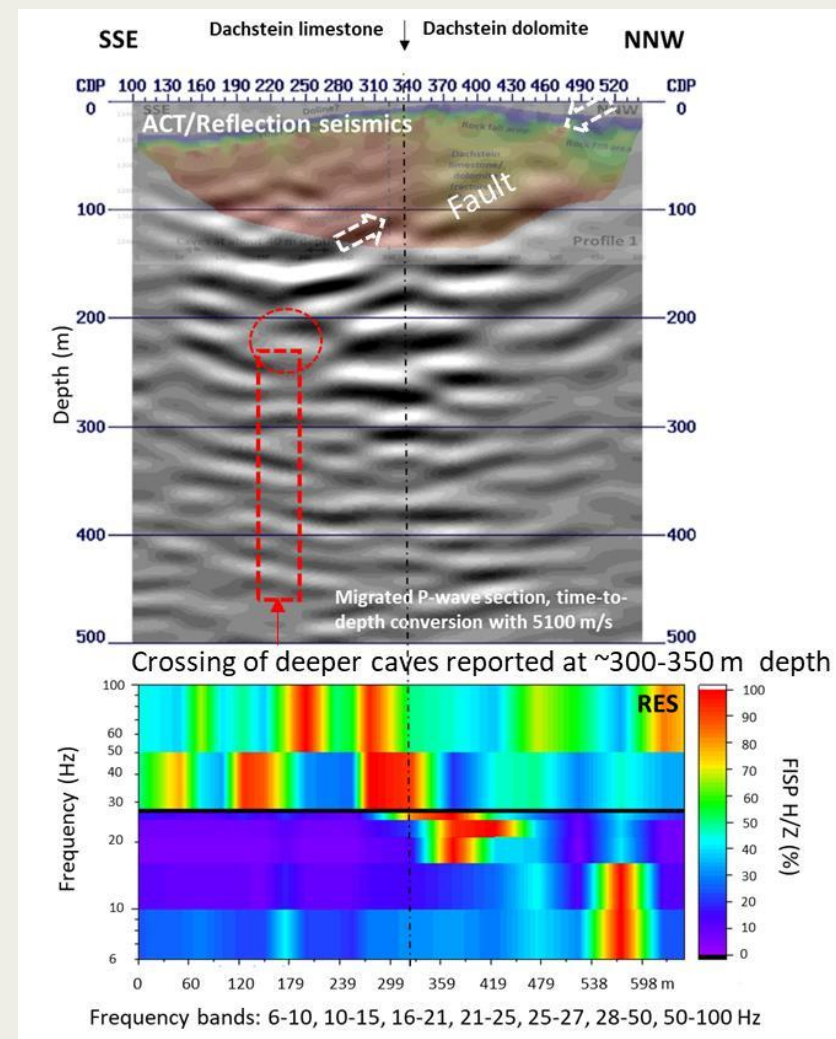
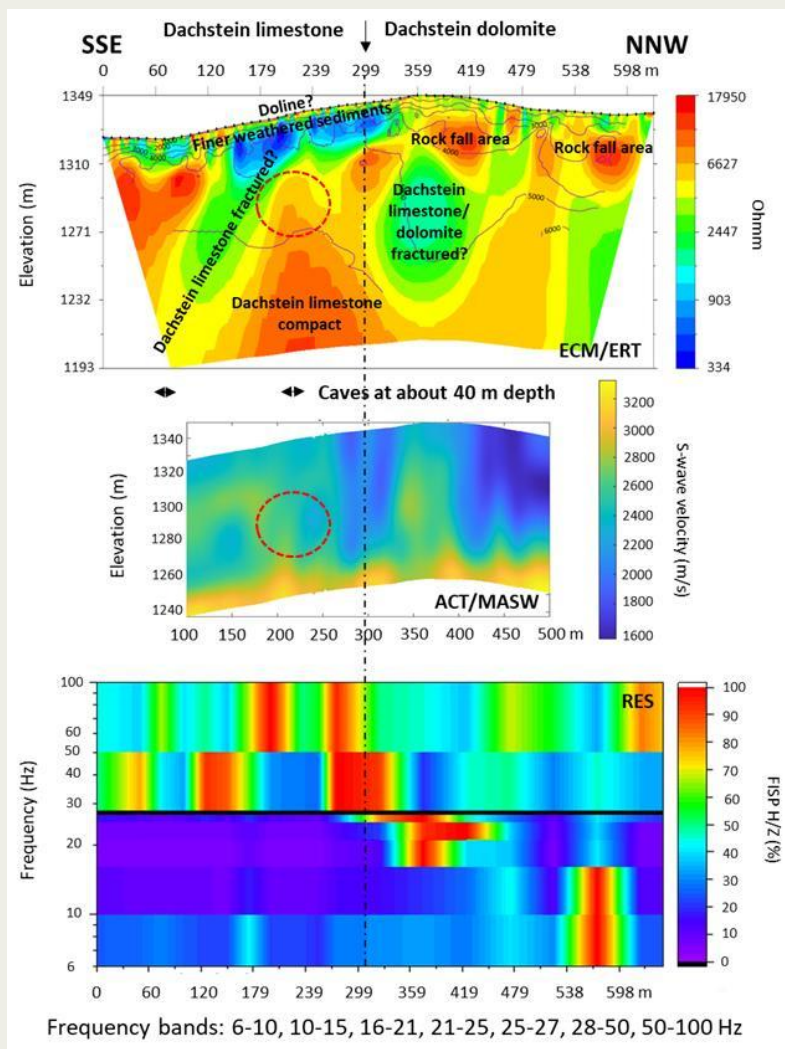
FISP_{H/Z} computed
for frequency interval 17 - 24 Hz
for 4 variations of FISP parameters



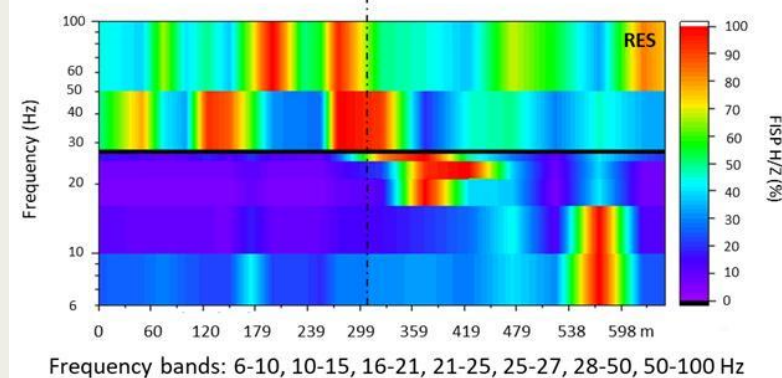
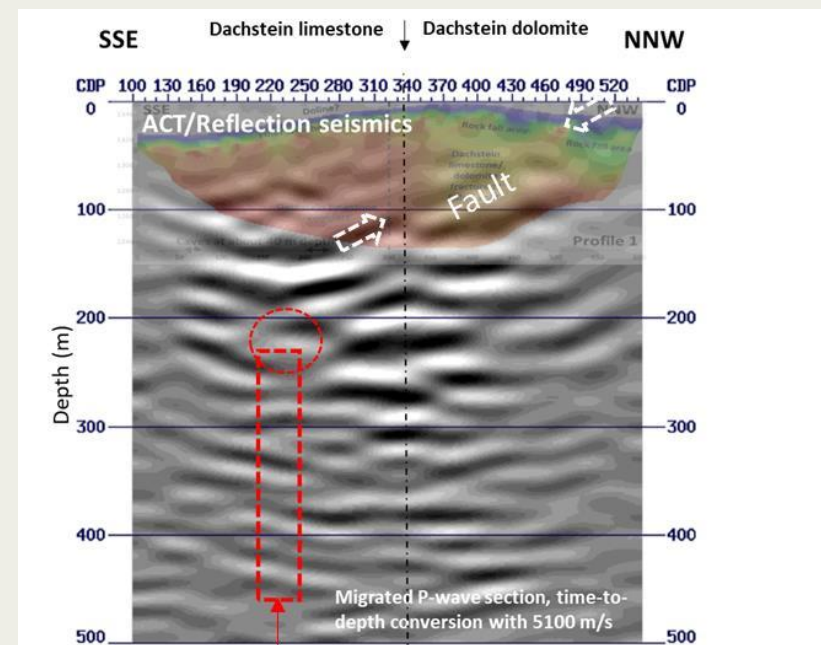
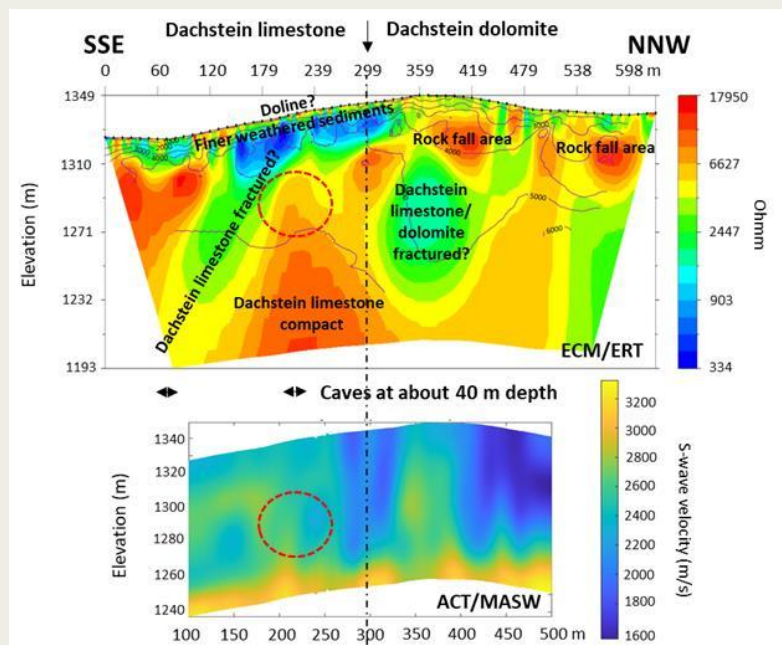
Real-site application of FISP – Rotmoos, Austria



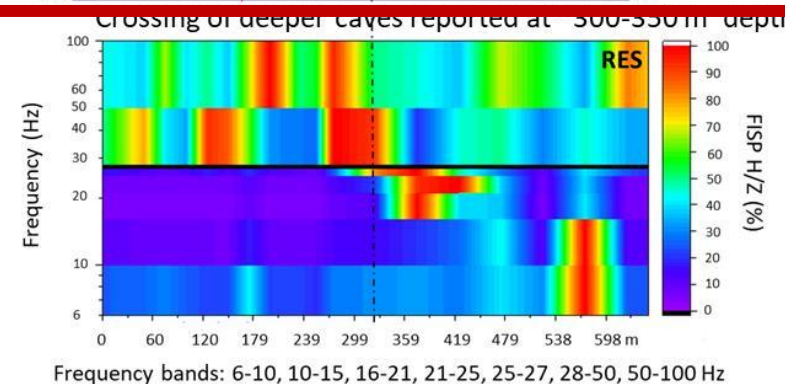
Real-site application of FISP – Rotmoos, Austria



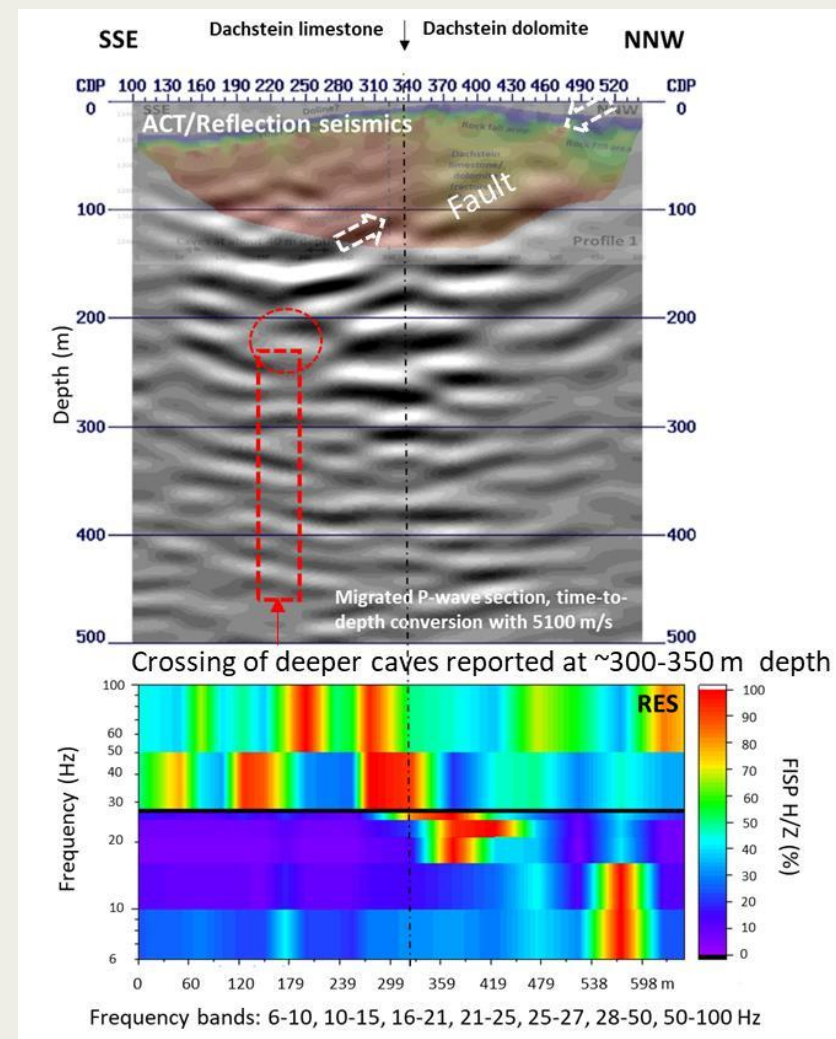
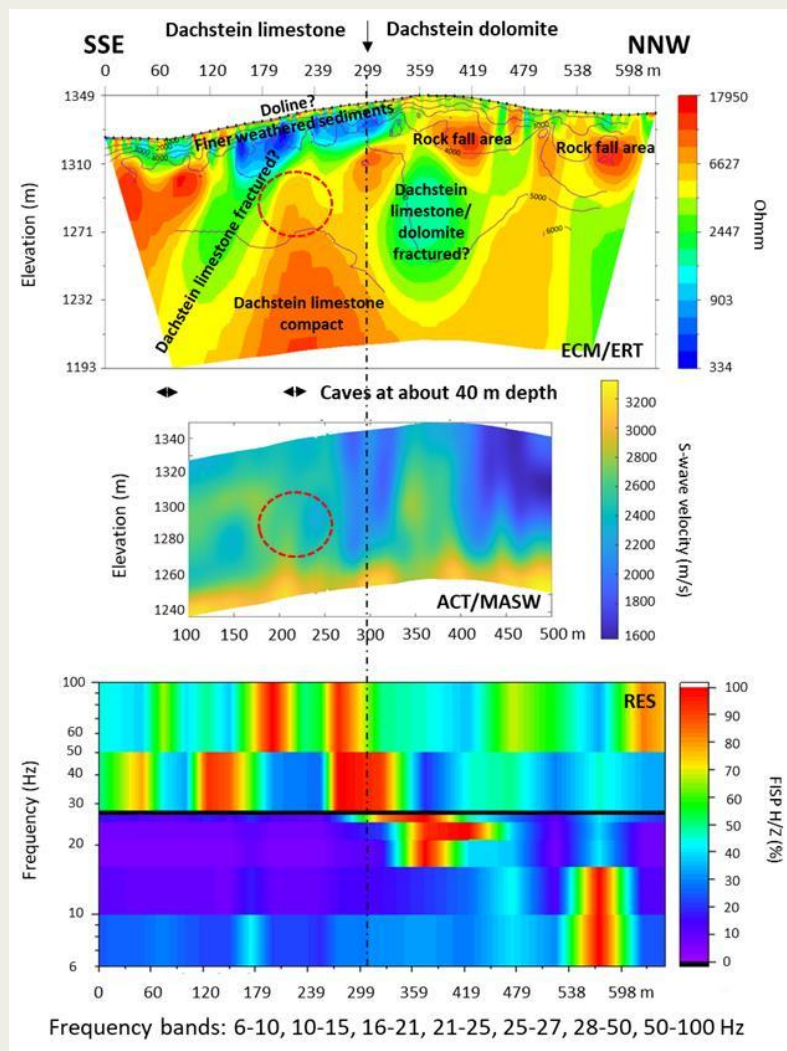
Real-site application of FISP – Rotmoos, Austria



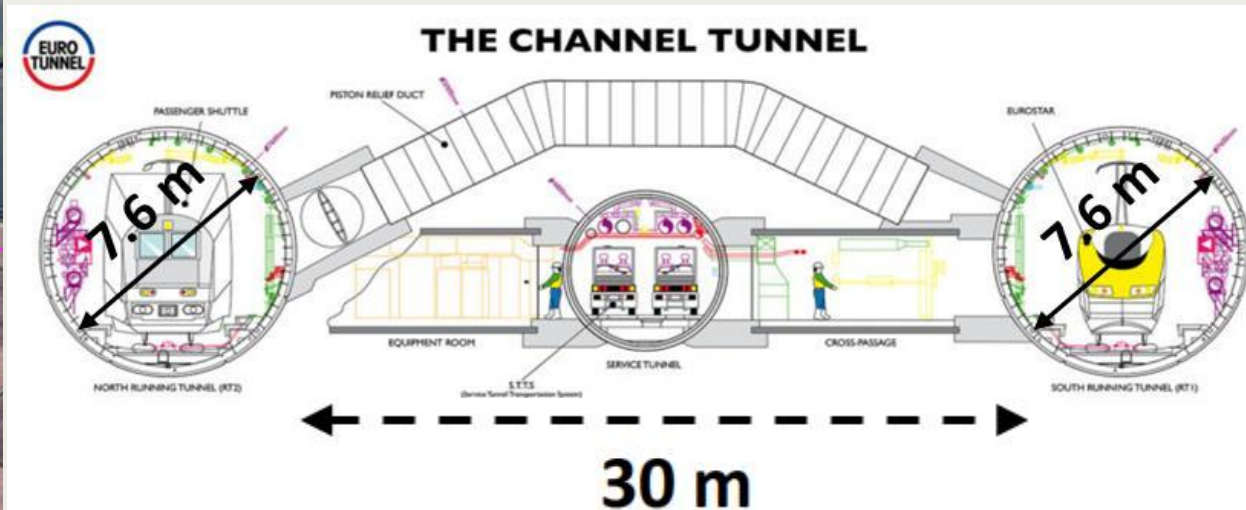
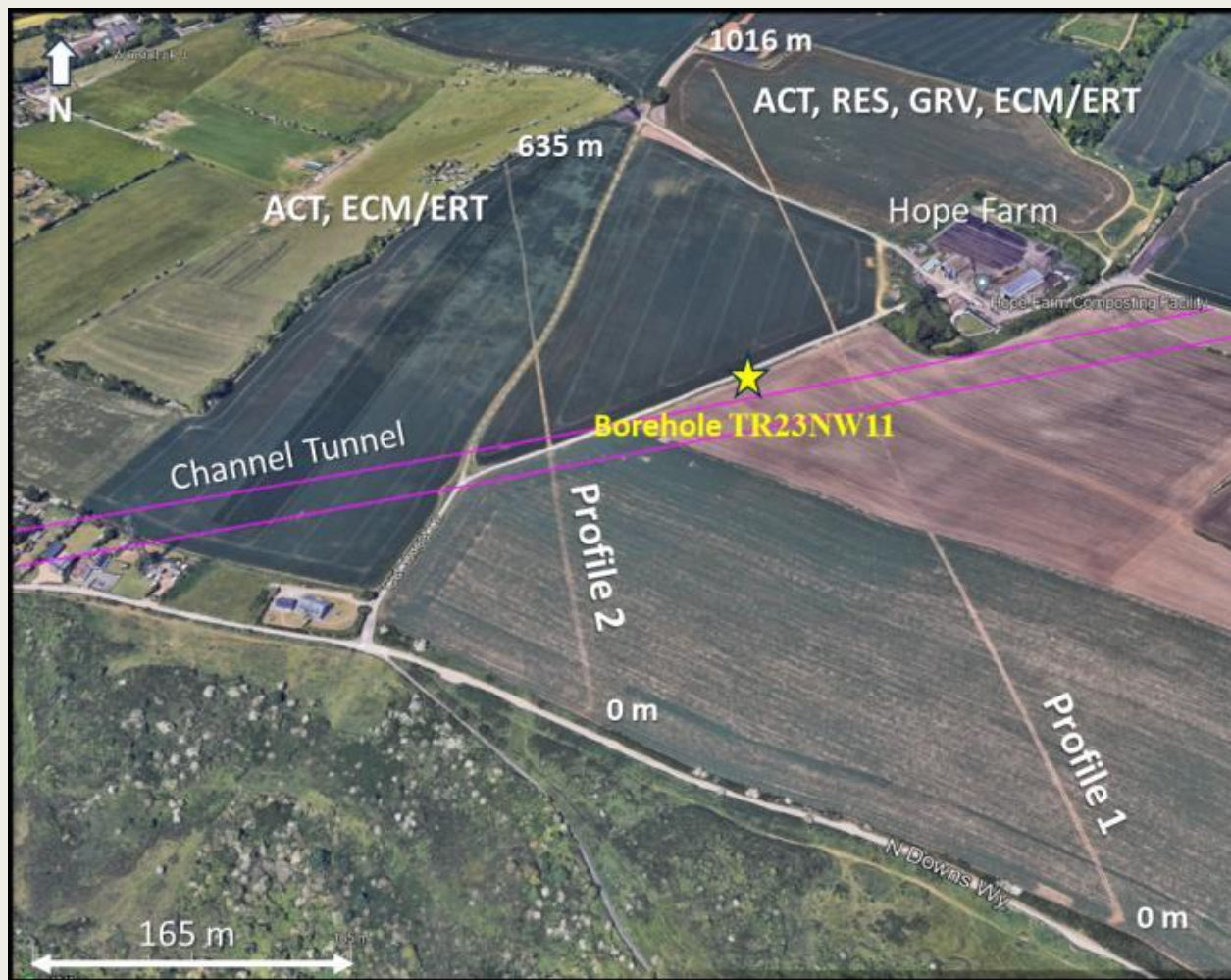
FISP H/Z



Real-site application of FISP – Rotmoos, Austria

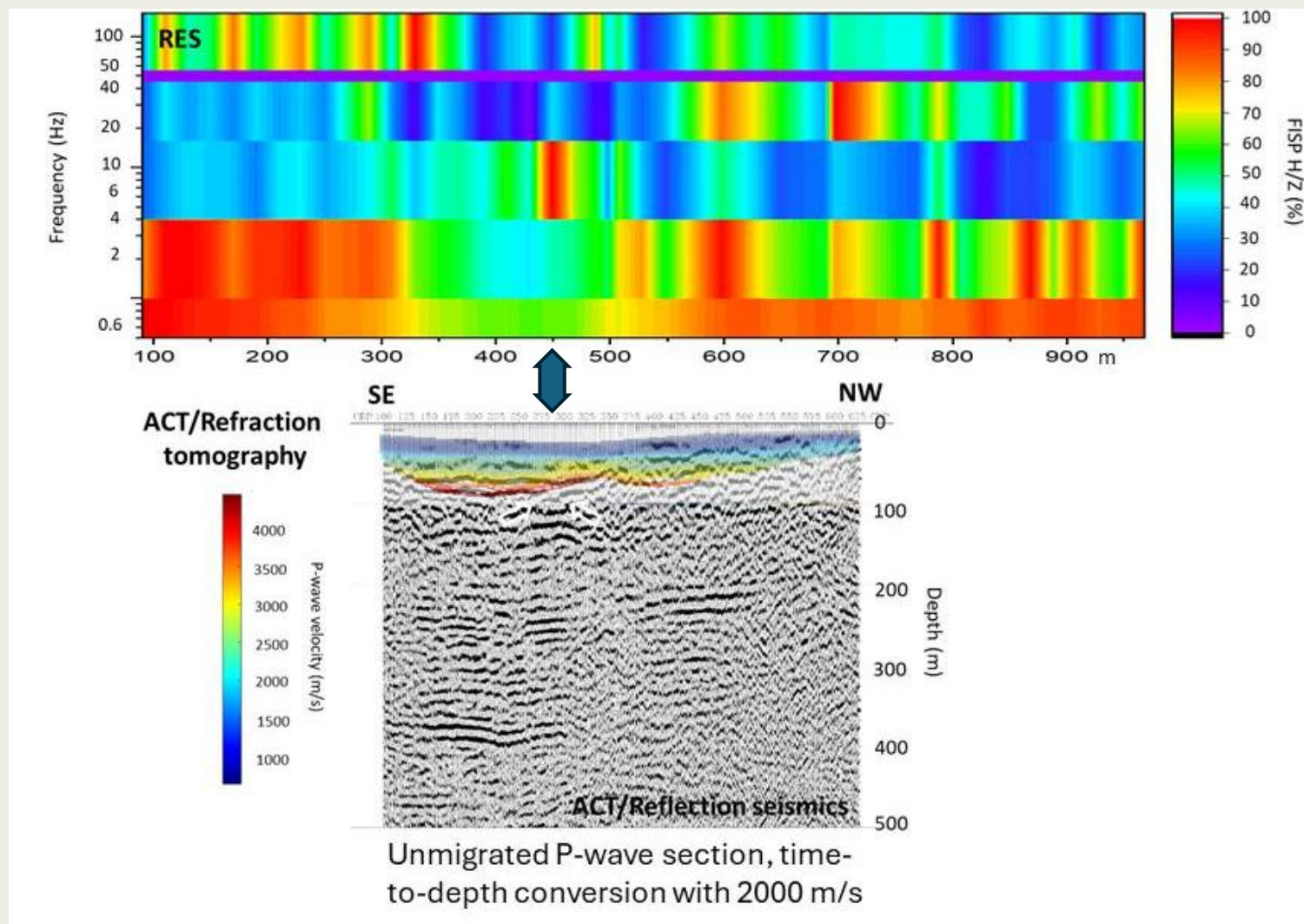


Real-site application of FISP – Channel Tunnel, UK



used data from Profile 1
across the Channel Tunnel
excavated in chalk marl at 90 m depth

Real-site application of FISP – Channel Tunnel, UK



Conclusions

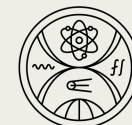
The application of FISP at various locations
has shown that
the method has the potential
to identify and locate underground cavities.



Conclusions

Based on our experience in processing data we have the following recommendations for organizing future noise measurements for resonance seismometry:

- measuring instruments must be **sufficiently sensitive** to be able to record even the weakest level of seismic noise in the range of at least several hundred counts,
- if two or more measuring instruments are to be used, it is necessary to ensure and **test that the seismic noise recorded** by all instruments **at the same place is the same**,
- seismic noise should be measured at all locations in the **most similar conditions possible**,



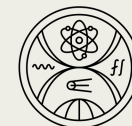
Conclusions

- measurements should be **disturbed as little as possible** by technogenic activities (including staff),
- after the initial measurement in the basic grid of measuring points and after the first analysis of FISP anomalies it is useful to perform **additional measurements in denser grid** around the places with anomalous values of FISP to verify and/or ensure the reliability of obtained of FISP anomaly,
- when selecting suitable frequency interval for FISP calculation, **avoid frequencies** containing an energy **from technogenic sources**,
- subject the obtained results to **sensitivity analysis** in relation to different time windows selection and different time segment selection.



Many thanks

**to the CTBTO team of experts who performed the measurements at all sites,
and
to the members of the CTBTO Expert Group for the fruitful discussions.**



Thank you !

See also: P3.3-556 Results of 2022 and 2023 OSI Field Tests for Seismic Techniques

