

## Current absolute seismometer calibration methods have issues at frequency band edges and in transportation of reference

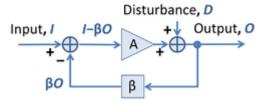
- 1. Traceable lab-calibration of broadband seismometers
  - Accuracy decreases at upper and lower corners (100 s, 100 Hz)
  - Not yet accounting for temperature
- 2. Transportation of lab-calibrated sensor to field for side-by-side testing
  - Accuracy decreases away from mid-band
  - Requires that transfer function does not change in transport



Laboratory absolute calibration setup with shake table and laser (Bloomquist, Merchant, & Slad, 2023)

# The main benefit of a mechanical calibration is to verify operation of the force transducer

A feedback control system has a forward path A and a feedback path β:

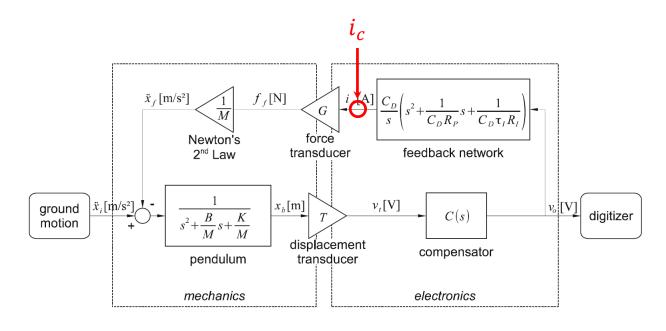


A basic property is that for sufficiently high loop-gain, the transfer function is determined by the feedback path alone:

$$\frac{O}{I} = \frac{A}{1 + A\beta} \cong \frac{1}{\beta}$$

In a force-feedback inertial sensor, an electrical calibration:

- Should not alter the loop gain
- May introduce a low-pass filter
- Injects current into the force transducer



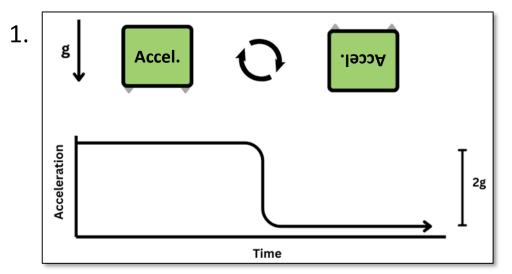
During electrical calibration, the force transducer becomes part of the forward path. It is not part of the closed-loop response.

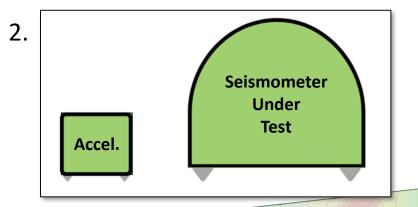
Left: <a href="https://en.wikipedia.org/wiki/Negative\_feedback">https://en.wikipedia.org/wiki/Negative\_feedback</a>. Right: Fig. 6 from Ackerley, N. (2015). Principles of broadband seismometry. In *Encyclopedia of earthquake engineering* (pp. 1941-1970). Springer, Berlin, Heidelberg.

Your reference sensor can be calibrated in the field, and immediately compared to a sensor under test

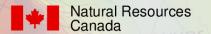
#### Method:

- 1. Absolute calibration of reference strong-motion accelerometer using gravity (slide 4)
  - Sensitivity is affected by temperature (slide 5)
  - Need to account for local gravity (slides 6-8)
- 2. Side-by-side relative calibration of instrument under test at mid-band (slide 9)
  - Only valid where SNR is high, around 0.2 Hz (slide 10)
  - Trade-off between duration x SNR and accuracy (slide 11)
- 3. Electrical calibration of both sensors across full frequency band (slide 12)
- 4. Combine results and propagate errors (slides 13-16)





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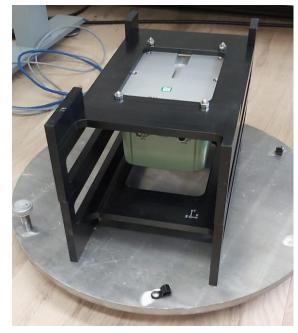


### Step 1: Absolute Accelerometer Calibration

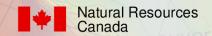
 Difference between upright and upside-down readings gives twice the sensitivity to gravity

$$S_z = \frac{1}{2 \, \mathrm{g}} (Z_{upright} - Z_{inverted})$$

- Instrument must have clip level > 2 g
- Works for horizontal axes as well
- Could be extended to give off-axes sensitivities
- Requires a "six-sided box" jig permitting accurate placement on 6 sides, and a flat & level surface
- We have developed a tool which outputs StationXML with calibrated response



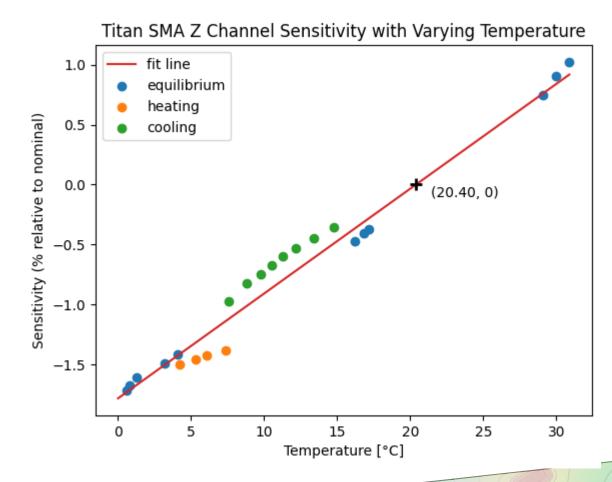
Titan SMA bolted into trimming jig on top of leveling plate





### Step 1a: Temperature is important

- Sensitivity of the Titan SMA varies ~2.5% from 0 to 30 °C
- Results differ while the instrument is heating or cooling
- Conclusion: Wait for temperature to stabilize before comparing data



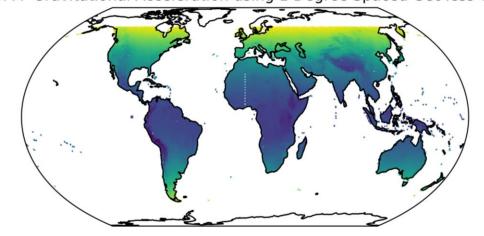
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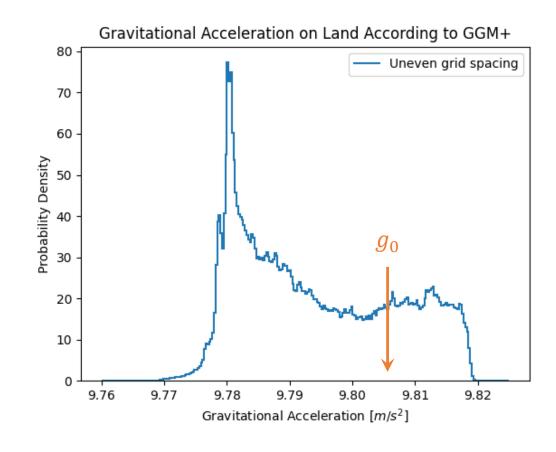


### Step 1b: Accounting for Local Gravity

- Using GGM+ model for gravitational acceleration on the Earth's surface
  - GRACE satellite gravimetry
  - Resolution improved by accounting for topography (SRTM)

GGM+ Gravitational Acceleration using 1 Degree Spaced GeoTess Grid

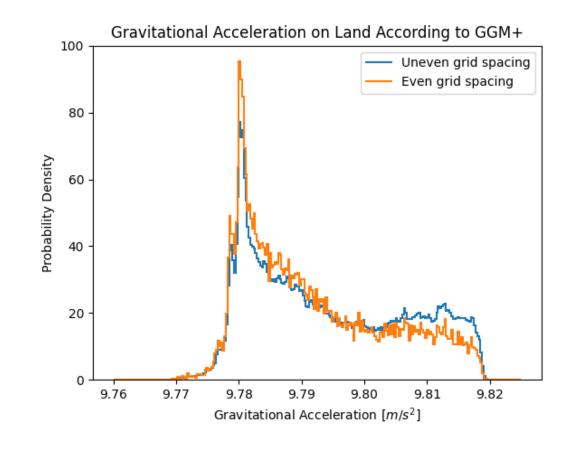




Hirt, C., S. Claessens, T. Fecher, M. Kuhn, R. Pail, and M. Rexer (2013), New ultrahigh-resolution picture of Earth's gravity field, *Geophys. Res. Lett.*, 40, 4279–4283, doi:10.1002/grl.50838.

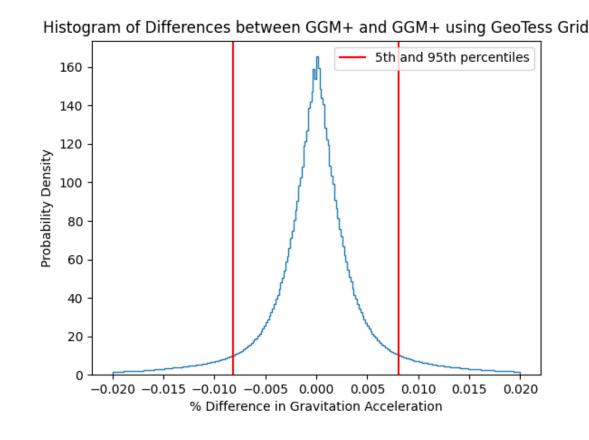
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- Re-gridded using GeoTess evenly space grid
  - Saves disk space
  - Better represents likelihood of finding any particular value of g on Earth



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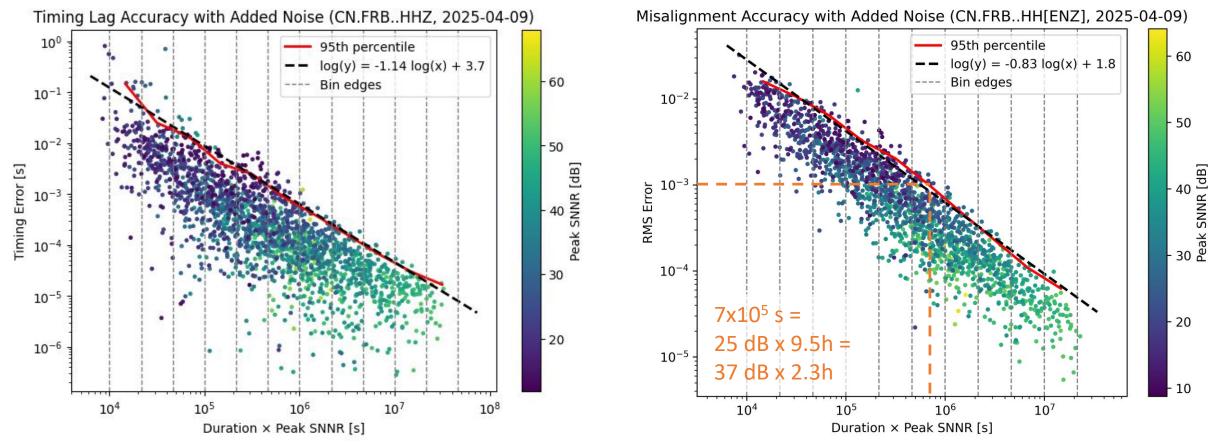
### Step 2: Side-by-Side Testing

- Only data with temperature close to the final temperature is used
- Preprocessing:
  - Responses are removed
  - Traces are bandpassed around the microseismic peak frequency
- Linear least squares:  $R = (A^T A)^{-1} A^T B$ 
  - Expect a diagonal matrix where the values represent the sensitivities of each channel



Titan SMA set up beside Trillium 120 QA

# Step 2a: Errors in Side-by-Side Timing and Misalignment Estimates Decrease with Increasing SNR and Duration



Plots generated by adding white noise flat in acceleration to simulate the noise floor of an accelerometer





# Step 2b: Accelerometer sensitivities change as expected between gain modes

- Compared absolute calibrations in 2g and 4g mode:
  - Observed ~0.01% difference in expected sensitivity
- This allows us to perform the side-by-side calibration with the accelerometer in 0.25g mode
  - Lower noise floor means higher SNR → smaller error OR shorter test

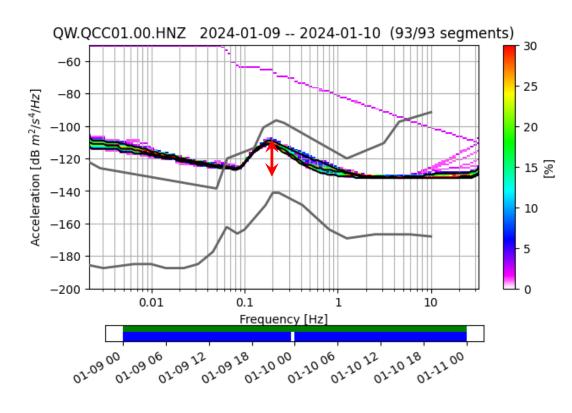
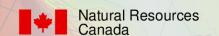


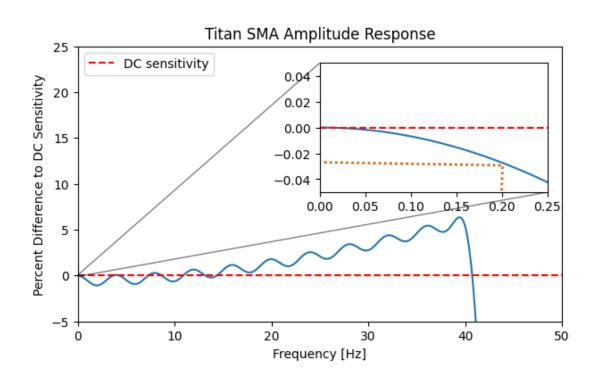
Figure: Typical earthquake early warning station in 2g mode; SNR is 20-25 dB

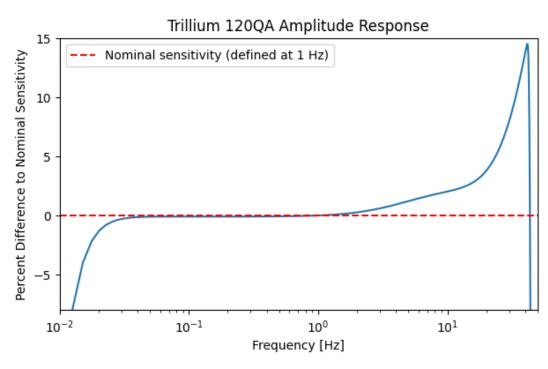




### Step 3: Response removal

There is a slight difference in the accelerometer response at 0.2 Hz and DC ...





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Source	Error [%]	
Temperature ( $20 \pm 10^{\circ}$ C)	0.877	
Gravity	0.180	
Tilt (±0.3°)	0.001	
Response error	0.027	
Noise error (40 dB SNNR, 2.5 hours)	0.068	
Quantization error	< 0.001	
Total (Root sum of squares)	0.898	
Total (Worst case)	1.154	

Temperature fluctuations mean that the side-by-side data won't be at the exact same temperature as the accelerometer calibration

Acceleration due to gravity varies slightly depending on location

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The surface that the accelerometer calibration is performed on may not be perfectly level

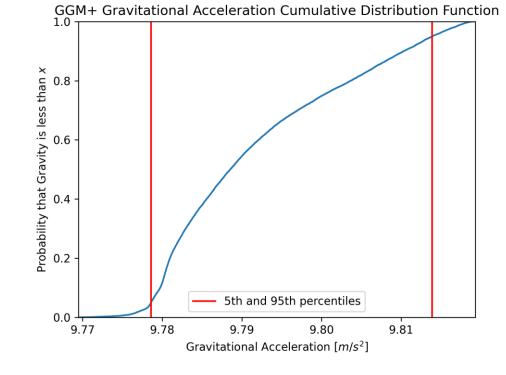


Source	Error [%]	
Temperature ( $20 \pm 0.3^{\circ}$ C)	0.058	
Gravity	0.180 0.001 0.027	
Tilt (±0.3°)		
Response error		
Noise error (40 dB SNNR, 2.5 hours)	0.068	
Quantization error	< 0.001	
Total (Root sum of squares)	0.203	
Total (Worst case)	0.335	

We reduce temperature variance by only using data with temperature near the temperature of the calibration

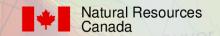
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$$\frac{9.81388305 - 9.77859455}{2 \times 9.80665} \times 100\% = 0.180\%$$

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Source	Error [%]	
Temperature ( $20 \pm 0.3^{\circ}$ C)	0.058	
Gravity grid inaccuracy	0.008	
GGM+ uncertainty	0.002	Latitudes and longitudes are rounded to fit on a less dense grid
Tilt (±0.3°)	0.001	The off a feet acrise gifa
Response error	0.027	
Noise error (40 dB SNNR, 2.5 hours)	0.068	Uncertainty on provided accelerations in the GGM+ model
Quantization error	< 0.001	
Total (Root sum of squares)	0.094	Main adjustable parameter: duration-
Total (Worst case)	0.165	SNR-accuracy trade-off





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#### Summary

Field calibration of strong motion accelerometers:

- Can greatly simplify field calibration of weak motion seismometers
- Cannot replace lab calibration for verification that calibration input and ground motion output responses are as manufacturer states

As far as I know, neither GRACE nor GGM+ nor calibrated in a traceable way, yet gravity itself may be able to serve as an important reference.

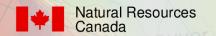
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#### **Next Steps**

- Training of field operations staff in Canada
- Opportunistic calibration of CNSN stations
- Compare calibration results to laboratory calibration?

#### **Questions?**

nicholas.ackerley@nrcan-rncan.gc.ca







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