

Variable Global Grid Refinement and Travel-Time Prediction using the RSTT Model

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RSTT Model

- The Regional Seismic Travel Time (RSTT) is a global model (Myers et al. 2010, Begnaud et al. 2021, 2021a) that rapidly predicts travel times of regional seismic phases (Pn, Sn, Pg and Lg)
- RSTT accounts for Moho, crystalline crust layers, sedimentary layers and surface water/ice layers of the 3-D crustal and upper mantle structures.
- RSTT models utilize a model grid of constant $\sim 1^\circ$ cells.
- Pn/Sn travel time (TT) in the RSTT model is given as:

$$TT = \sum_{i=1}^N d_i s_i + \alpha + \beta + \gamma$$

RSTT Global Tessellation at $\sim 1^\circ$

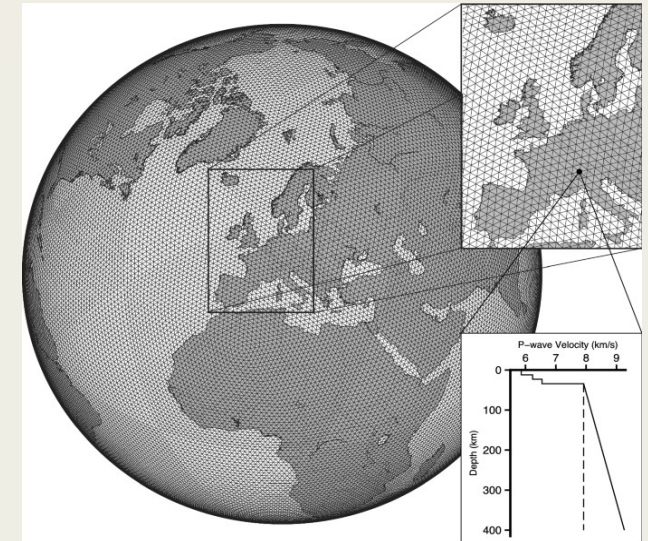
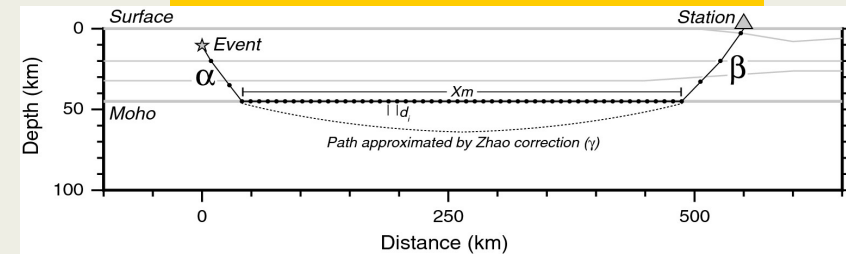


Illustration of a Pn/Sn wave in RSTT

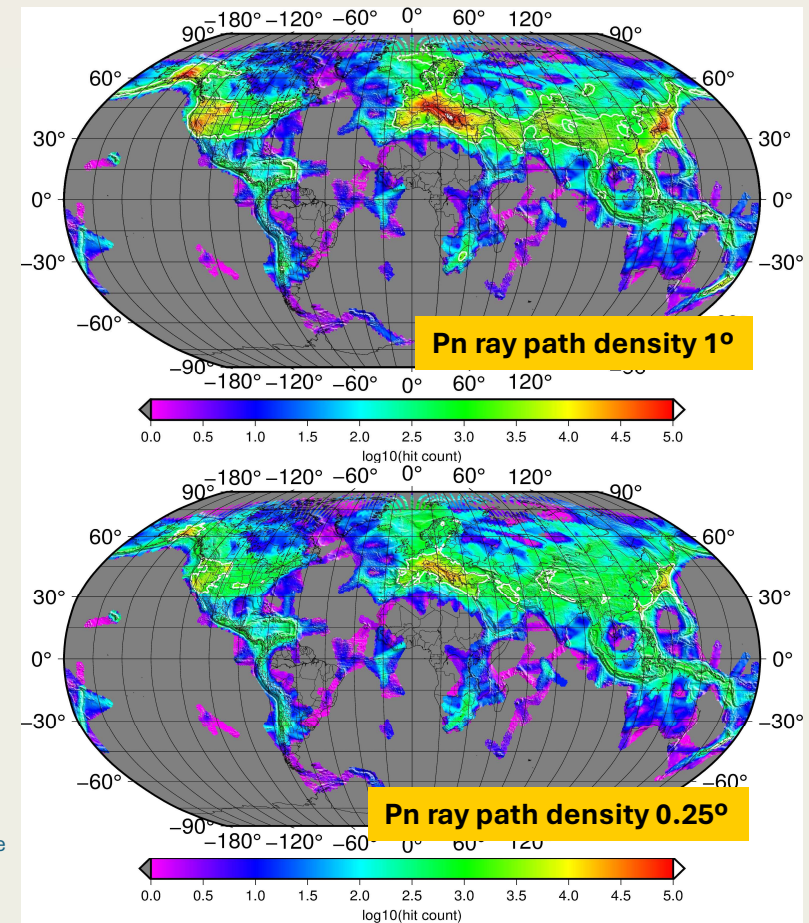


Begnaud et al. 2021, "Updates to the Regional Seismic Travel Time (RSTT) Model: 1. Tomography"

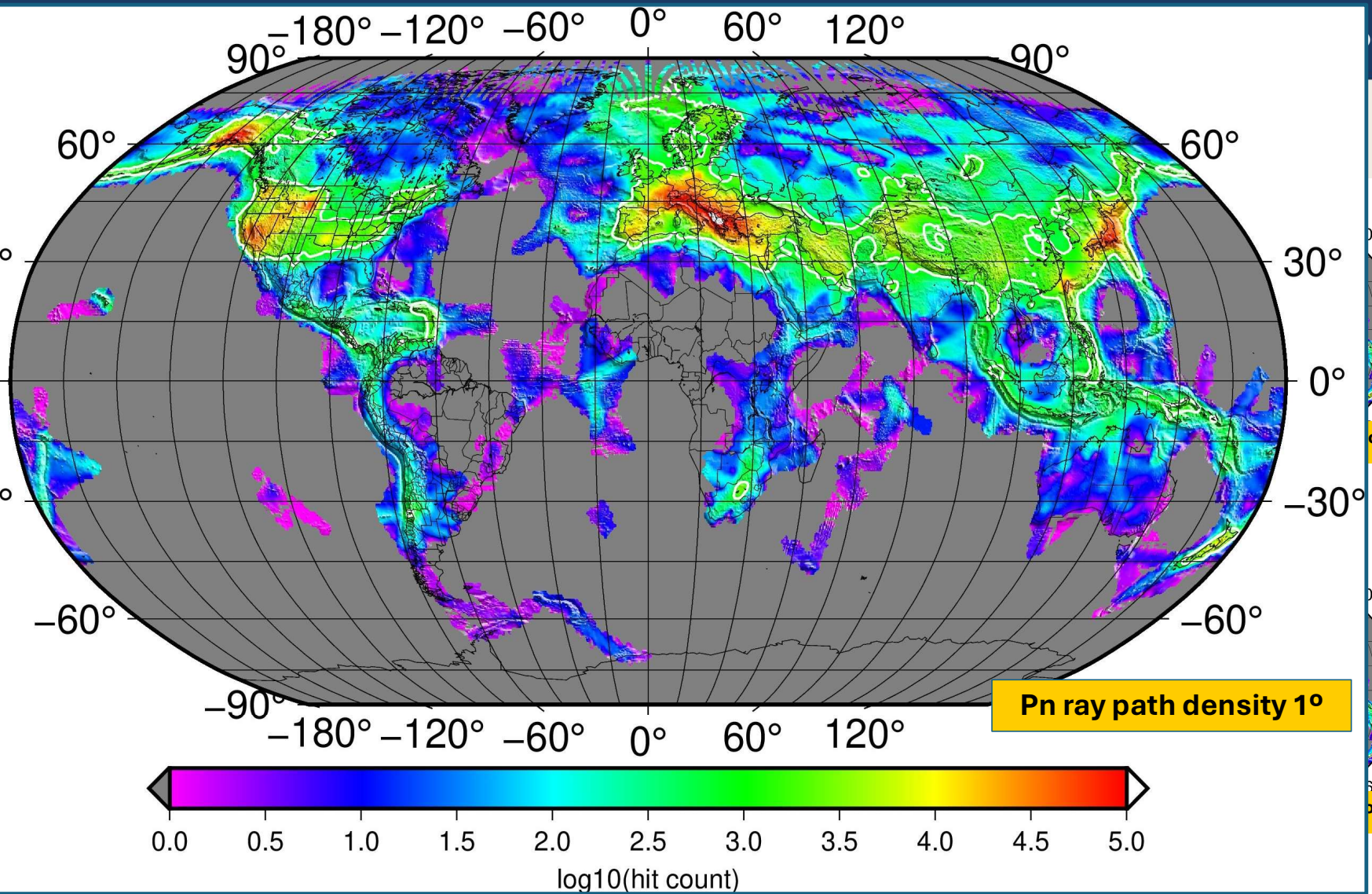
Grid Refinement in RSTT

- Babikoff et al. (2022) implemented data driven grid refinement of **upper mantle Pn velocity and upper mantle velocity gradient** in Israel and the Middle East using Pn and Pg waves for $1^\circ \rightarrow 0.5^\circ \rightarrow 0.25^\circ \rightarrow 0.125^\circ$.
- They successfully image smaller velocity features and improved travel time prediction in the region.
- A data driven global grid refinement of RSTT is warranted in regions (western U.S., Europe and the Middle East and East Asia) with **high density ray path coverage** to improve travel time prediction.

Ranasinghe et al. 2025, "Data-informed Grid Refinement to Improve Travel Time Accuracy in the Regional Seismic Travel Time (RSTT) Model"



- Background velocity
- The feature in
- A wave detection

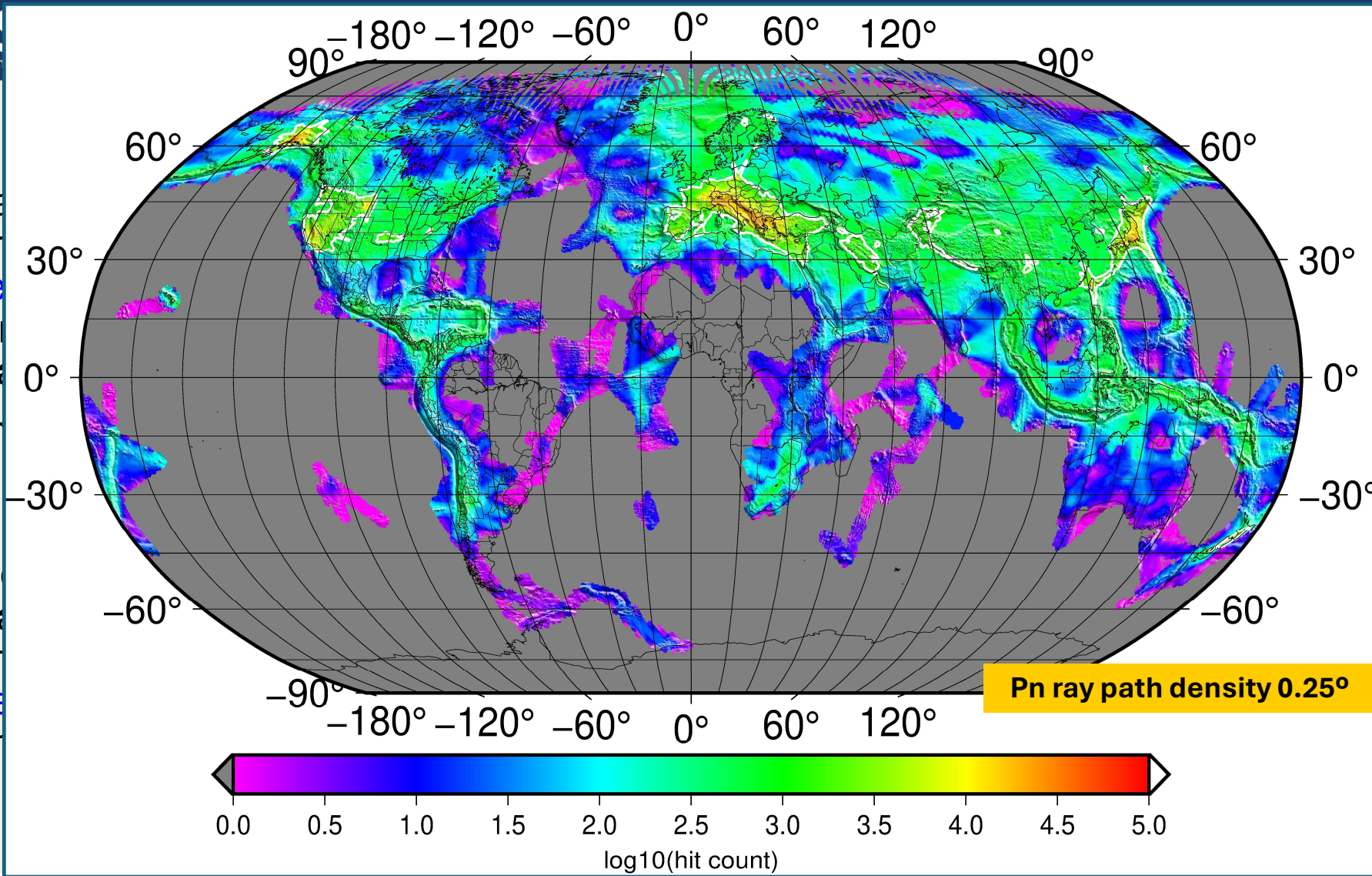


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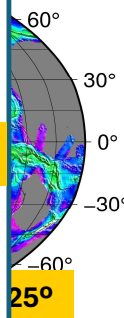
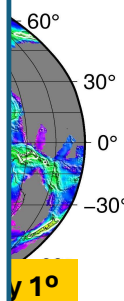


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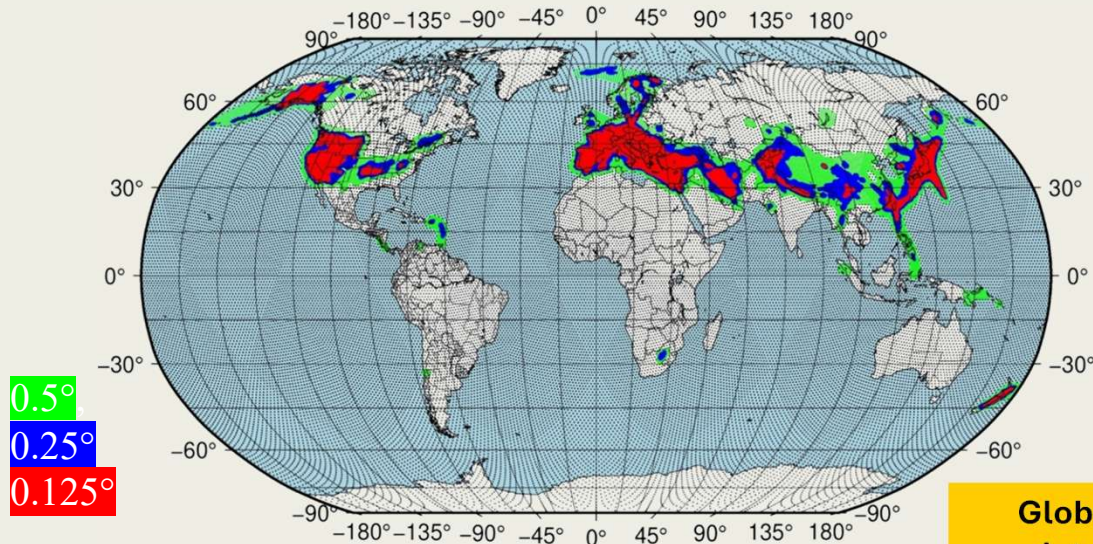
Model

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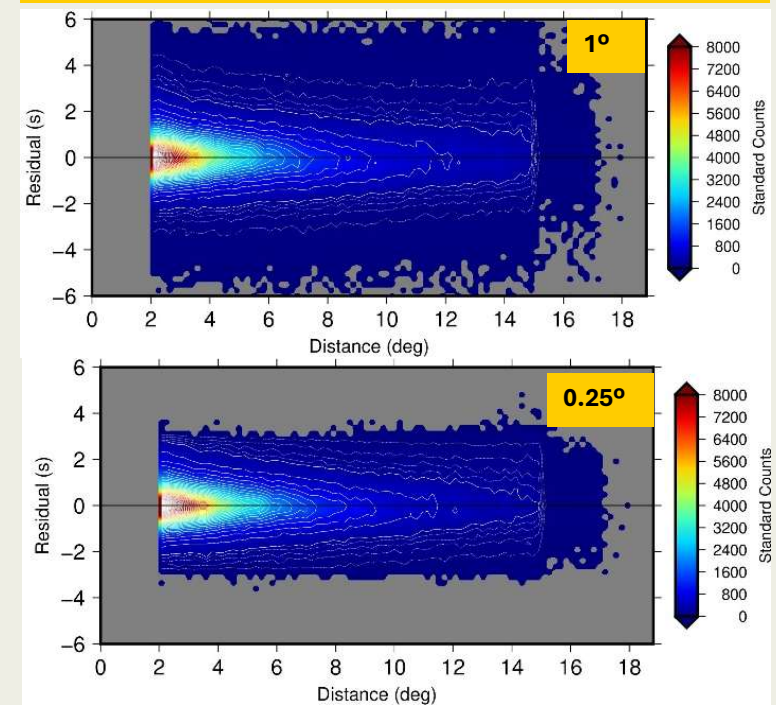


Data

- Pn travel time data for the current study is taken from a global compilation of seismic data (Begnaud et al., 2021)
 - GT≤25 or better events.
 - Relocated with Bayesloc relative relocation algorithm (Myers et al., 2007)
 - Events with focal depths above the Moho
 - Epicentral distances between 2° to 18°
- Removed phase arrivals whose TT residuals exceeded 3 STD from the mean



2D histograms of travel time residuals versus distance



Global map of tessellation points at different grid levels

Grid Refinement Method

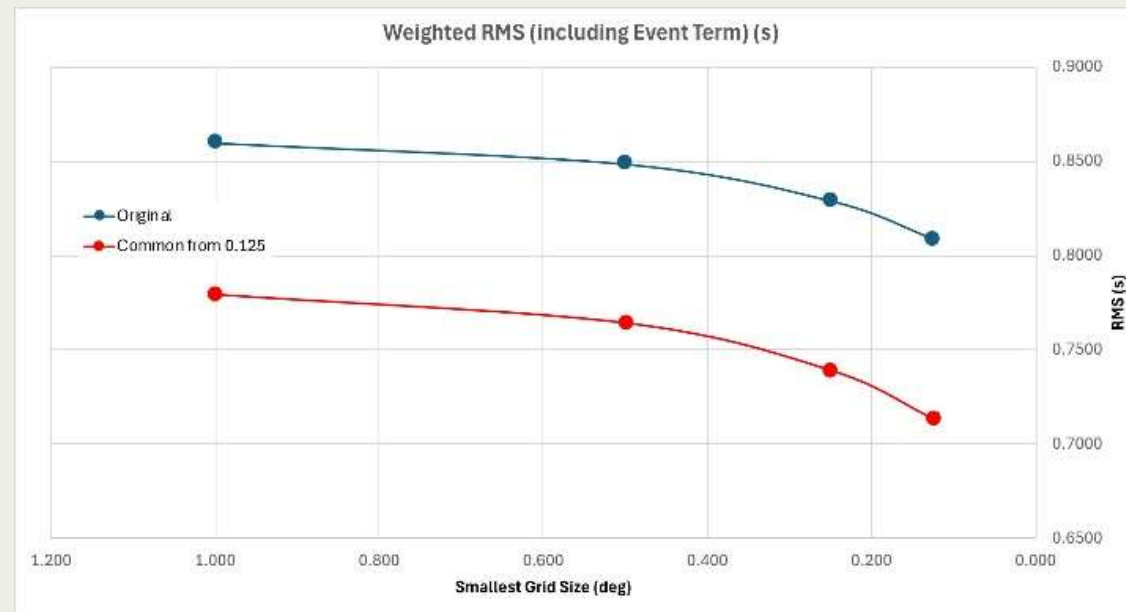
- Grid sizes were refined from 1° to 0.125° while adjusting smoothing and damping values using L-curve tests for upper mantle velocity and gradient
- A high damping value was used for cells with < 300 crossing ray paths
- Suitable damping and smoothing values were determined at each grid level
 - Initially for upper mantle slowness
 - Then for upper mantle gradient, holding the chosen value for the slowness values steady
- For each grid level, we performed tomographic inversions, incorporating event terms which enhanced the residual reduction and inversion stability

Grid Level	Upper Mantle Slowness		Upper Mantle Gradient	
	<i>Damping</i>	<i>Smoothing</i>	<i>Damping</i>	<i>Smoothing</i>
1.0°	0.5	0.2	0.3	0.5
0.5°	0.3	0.2	0.2	0.75
0.25°	0.3	0.2	0.2	1.0
0.125°	0.3	0.2	0.4	1.5

Change of Travel Time Residuals from 1° to 0.125°

- RMS Pn travel time residual changes with each grid refinement
 - Original data
 - Common to all grid refinements (due to outlier removal)
- The RMS of the **Pn travel time residual reduced by 7.6%** from 1° to 0.125°.
- At 0.125° grid level:
 - 8,184 stations
 - 61,797 events
 - 1,142,792 ray paths

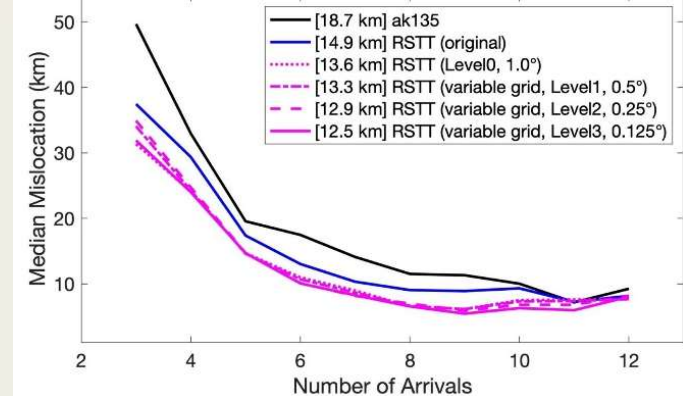
RMS residual changes with each grid refinement



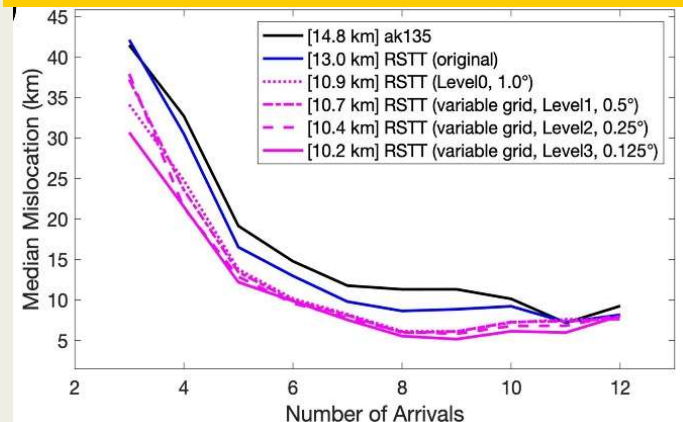
Mislocation of Validation Events

- 1395 validation events used from Begnaud et al. (2021) (not included in tomography)
- Median mislocation reduction for **Global arrivals and the 0.125° grid**:
 - **ak135**: 33.5%
 - **Original RSTT model**: 16.1%
- Median mislocation reduction for **Europe and the Middle East arrivals and the 0.125° grid**:
 - **ak135**: 32.4%
 - **Original RSTT model**: 21.6%
- Globally most validation events were recorded by < 6 stations

Global mislocation relative to number of Arrivals



Mislocation relative to number of Arrivals: Europe and the Middle East



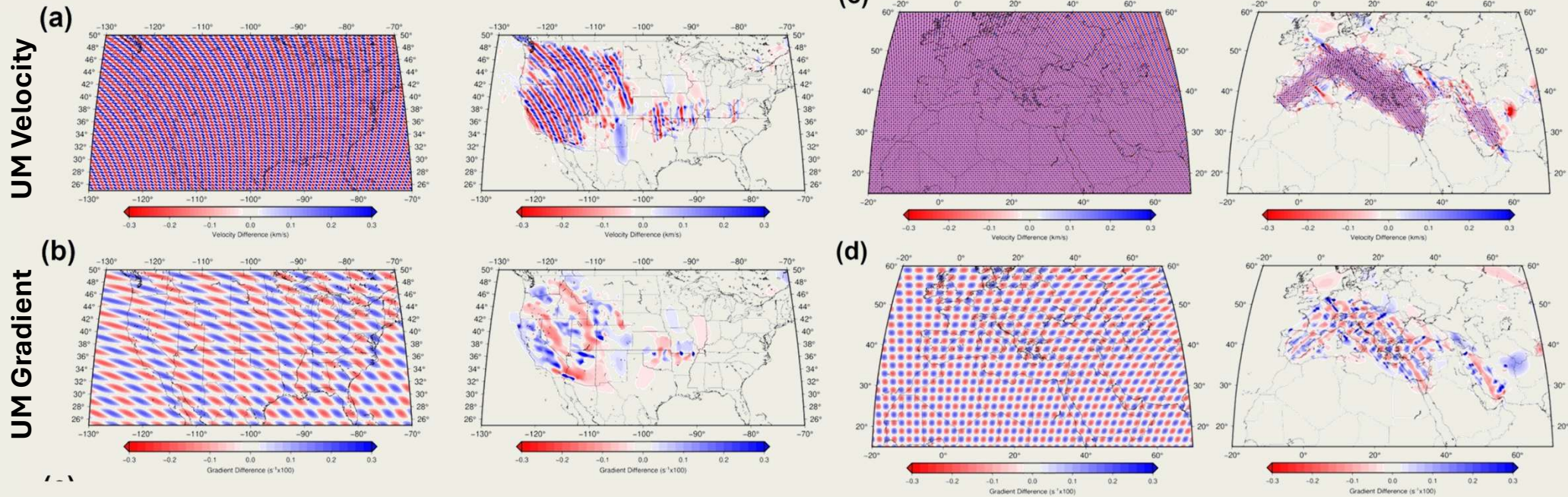
Checkerboard Tests

Checkerboard

Recovery

Checkerboard

Recovery



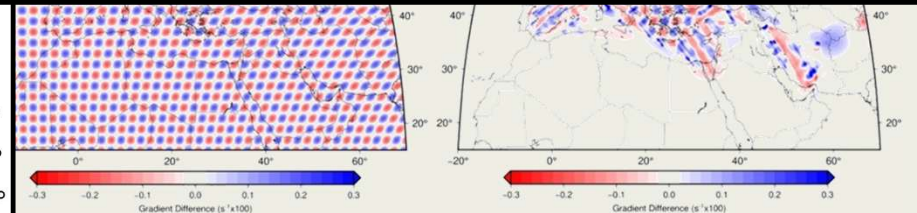
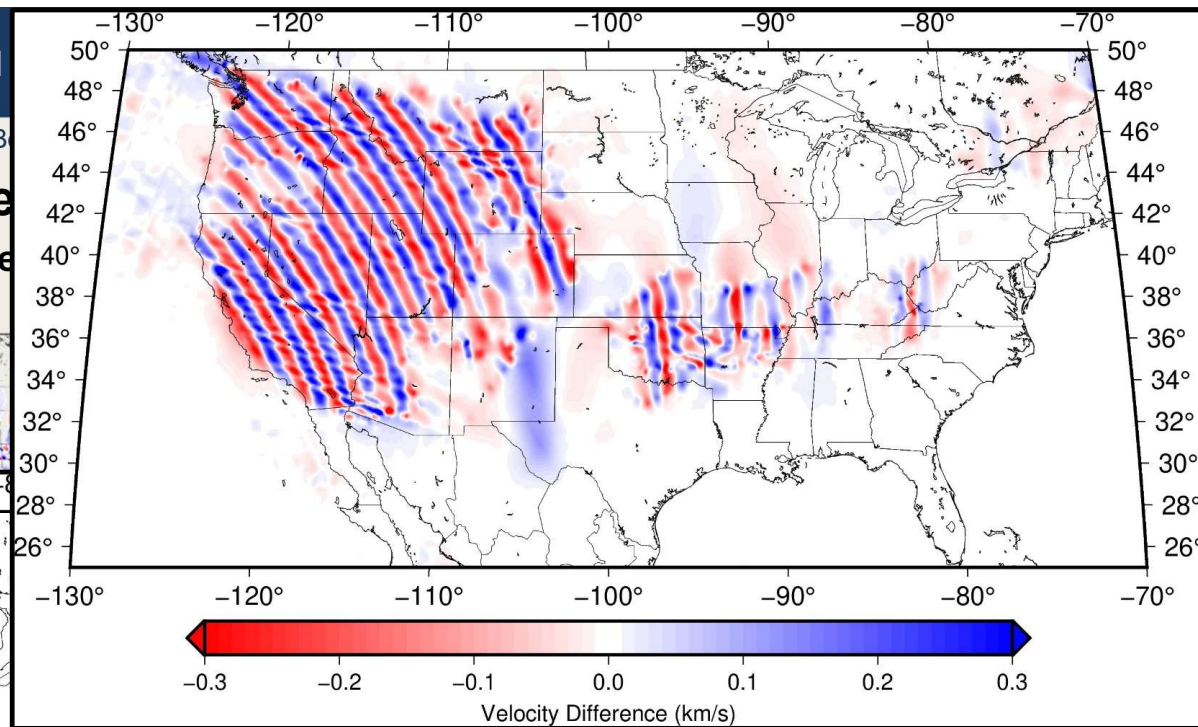
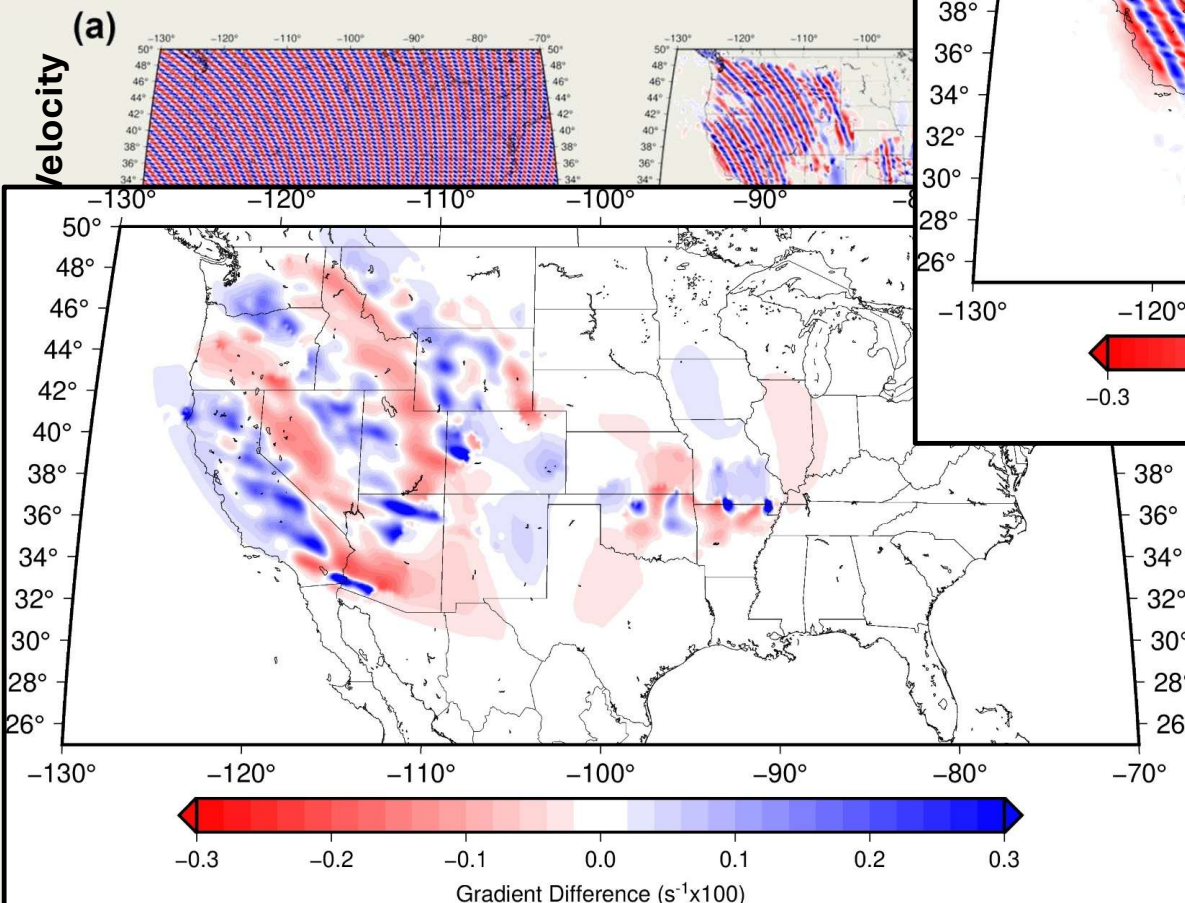
Contiguous U.S.

Europe/Middle East

Rays are calculated through these checkerboard models to create synthetic “observed” travel times for tomography tests, mimicking the main tomography runs.

Upper mantle (UM) velocity: 0.5° size with ± 0.5 km/s amplitudes
UM Gradient: 2° size with ± 0.002 s⁻¹ amplitudes

Checkerboard



Europe/Middle East

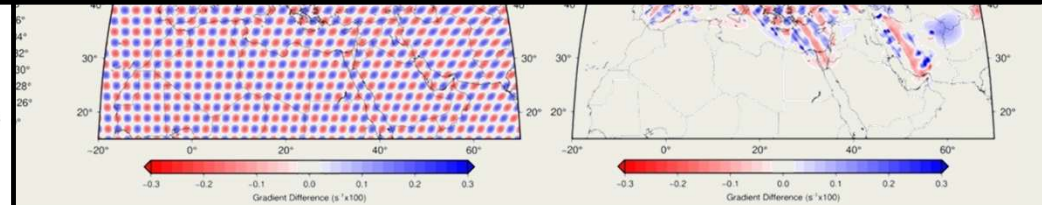
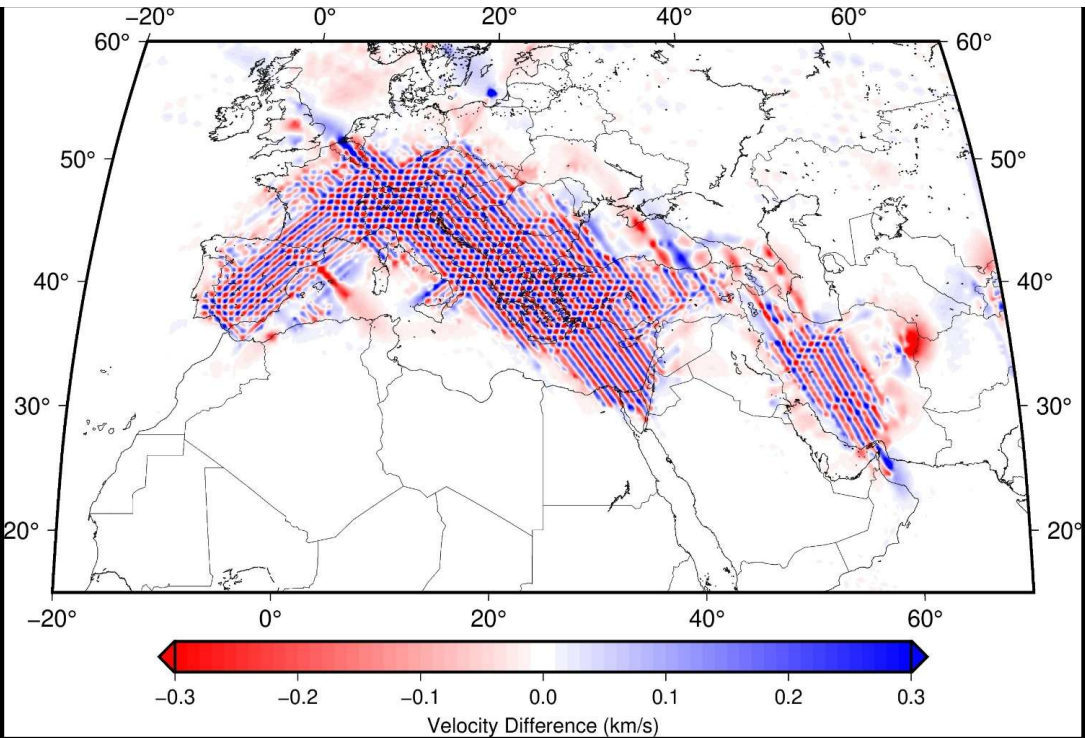
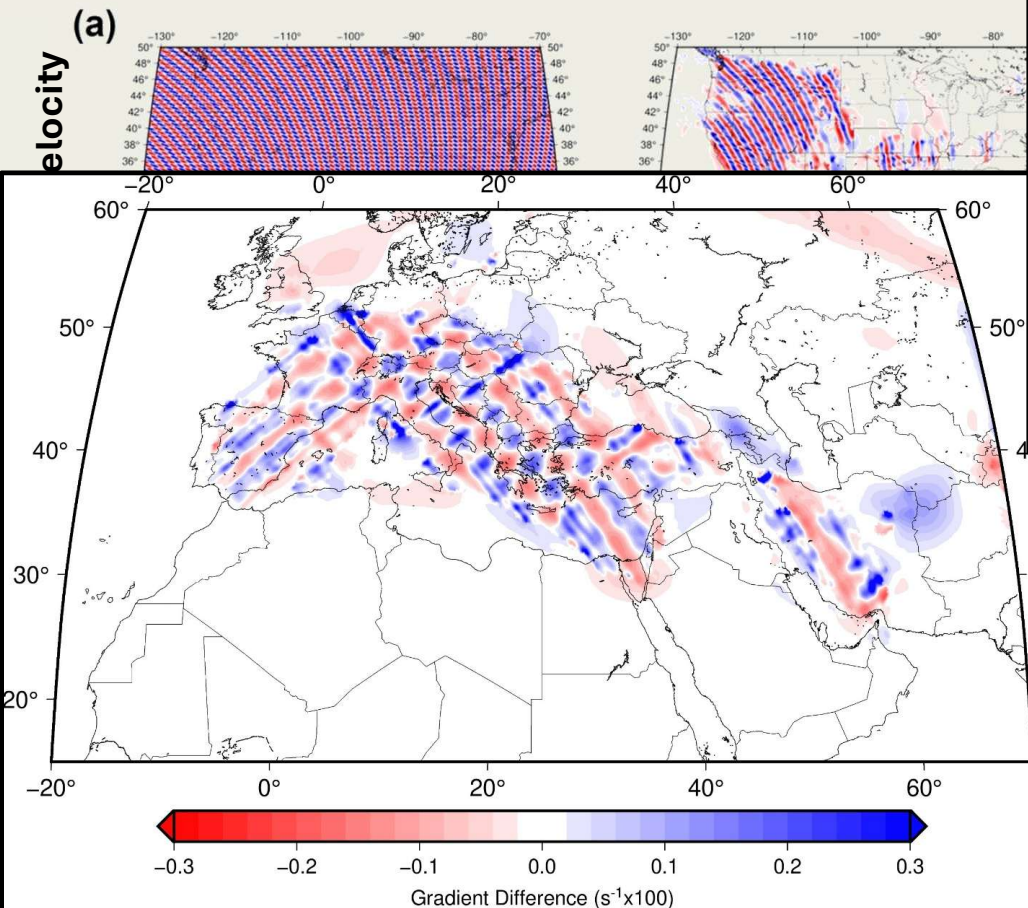
synthetic “observed” travel times for tomography

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Checkerboard

Checkerboard

Recovery

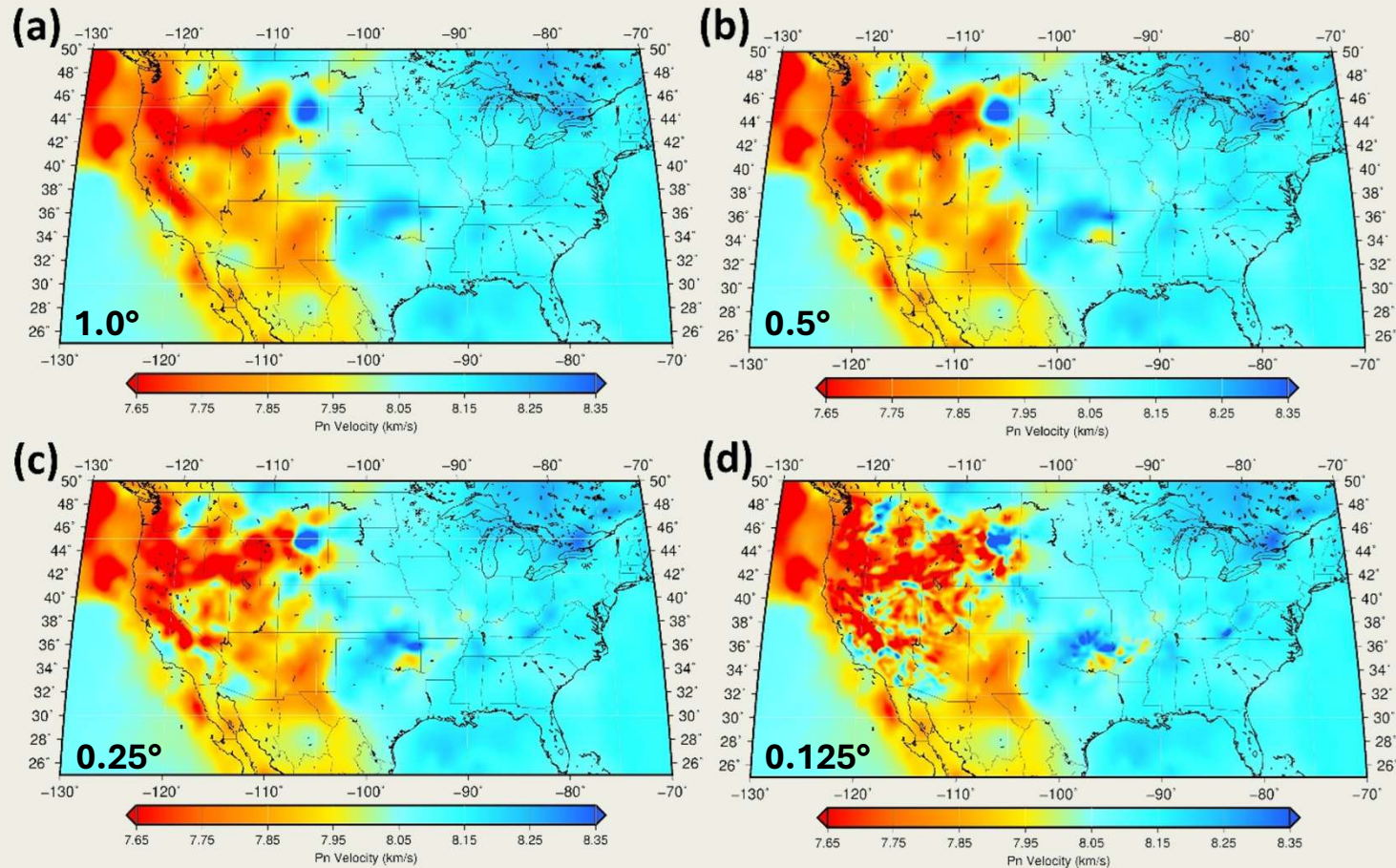


Europe/Middle East

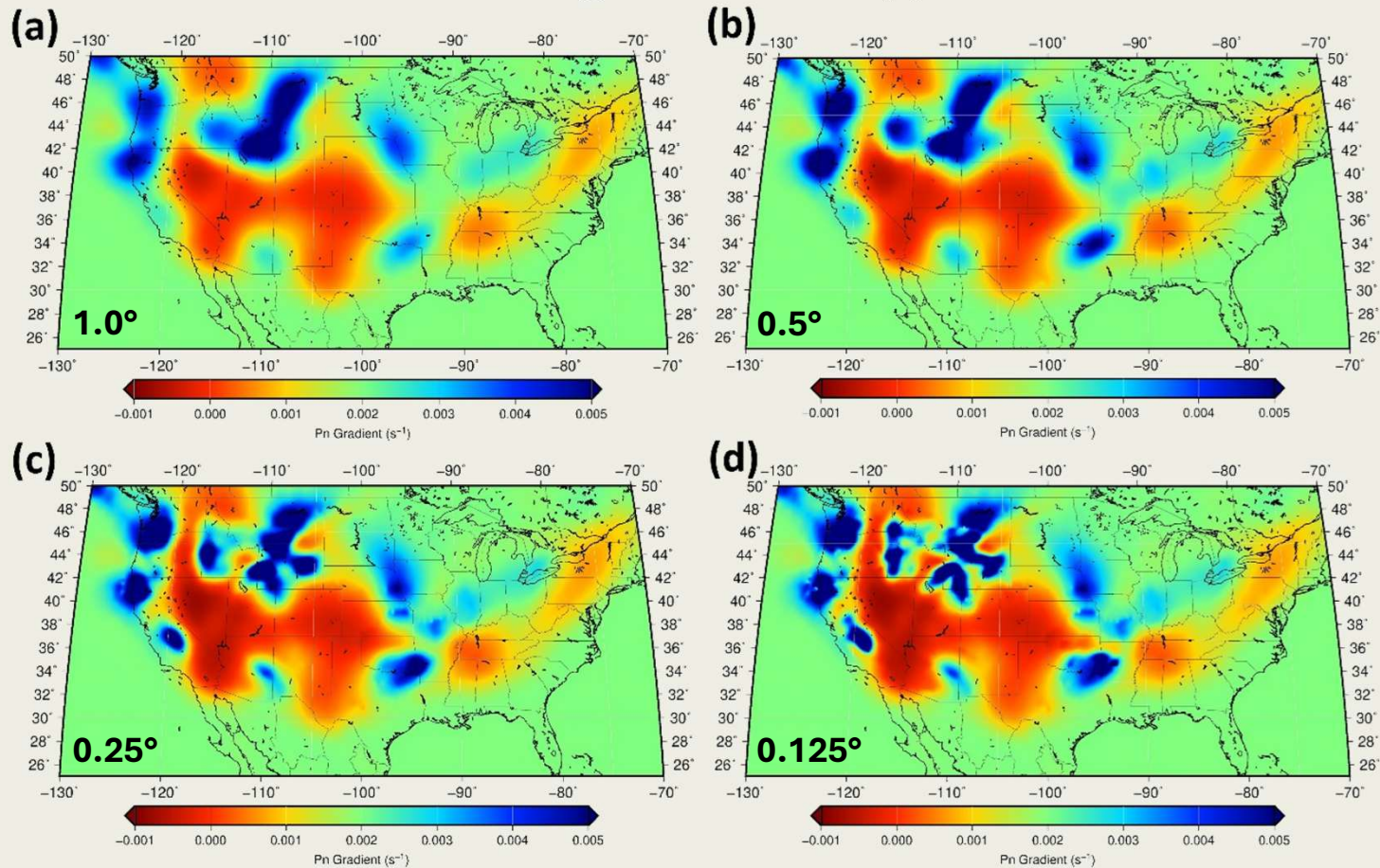
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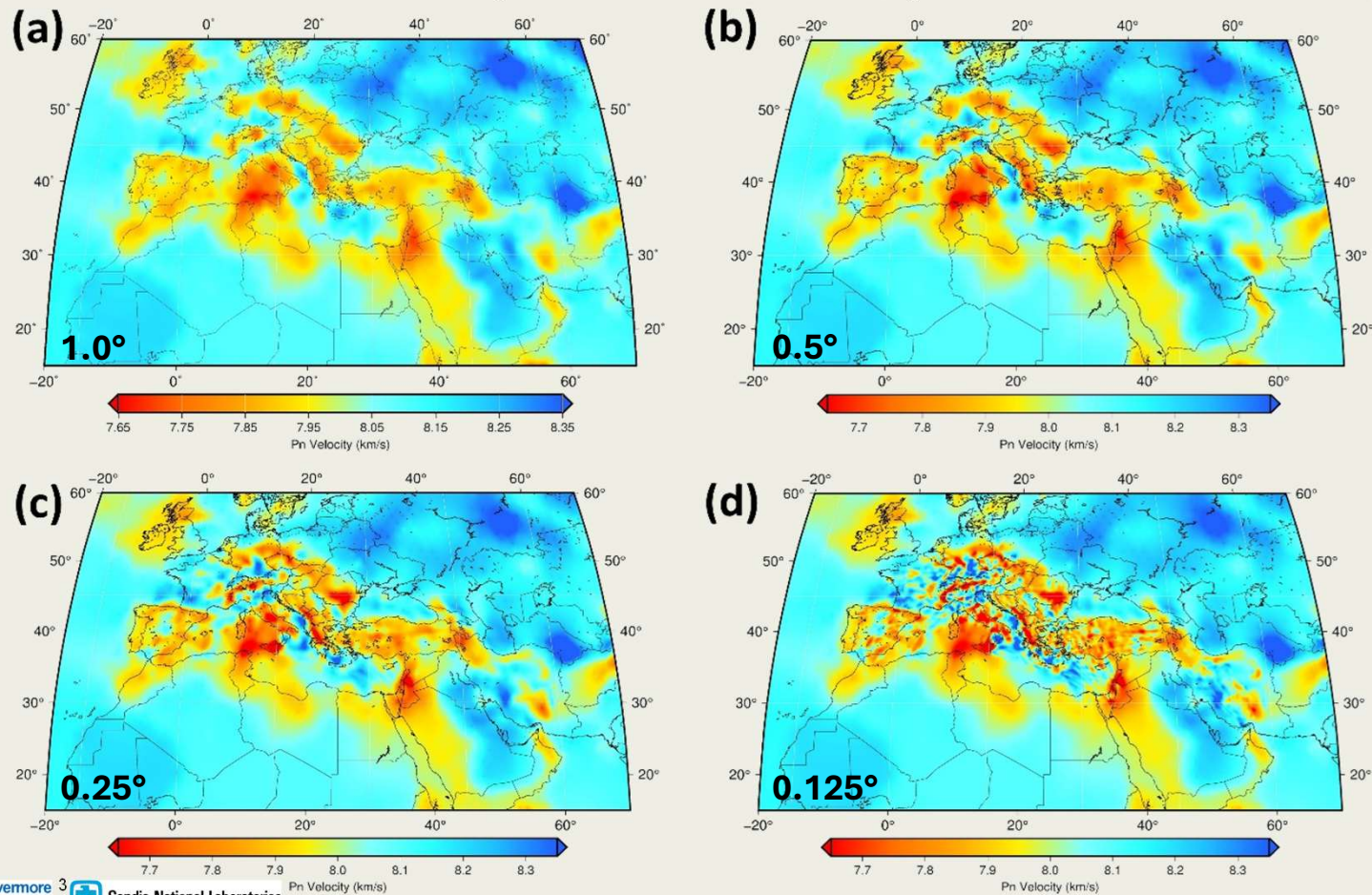
Grid Refinement in the Contiguous U.S.: Upper Mantle Pn Velocity



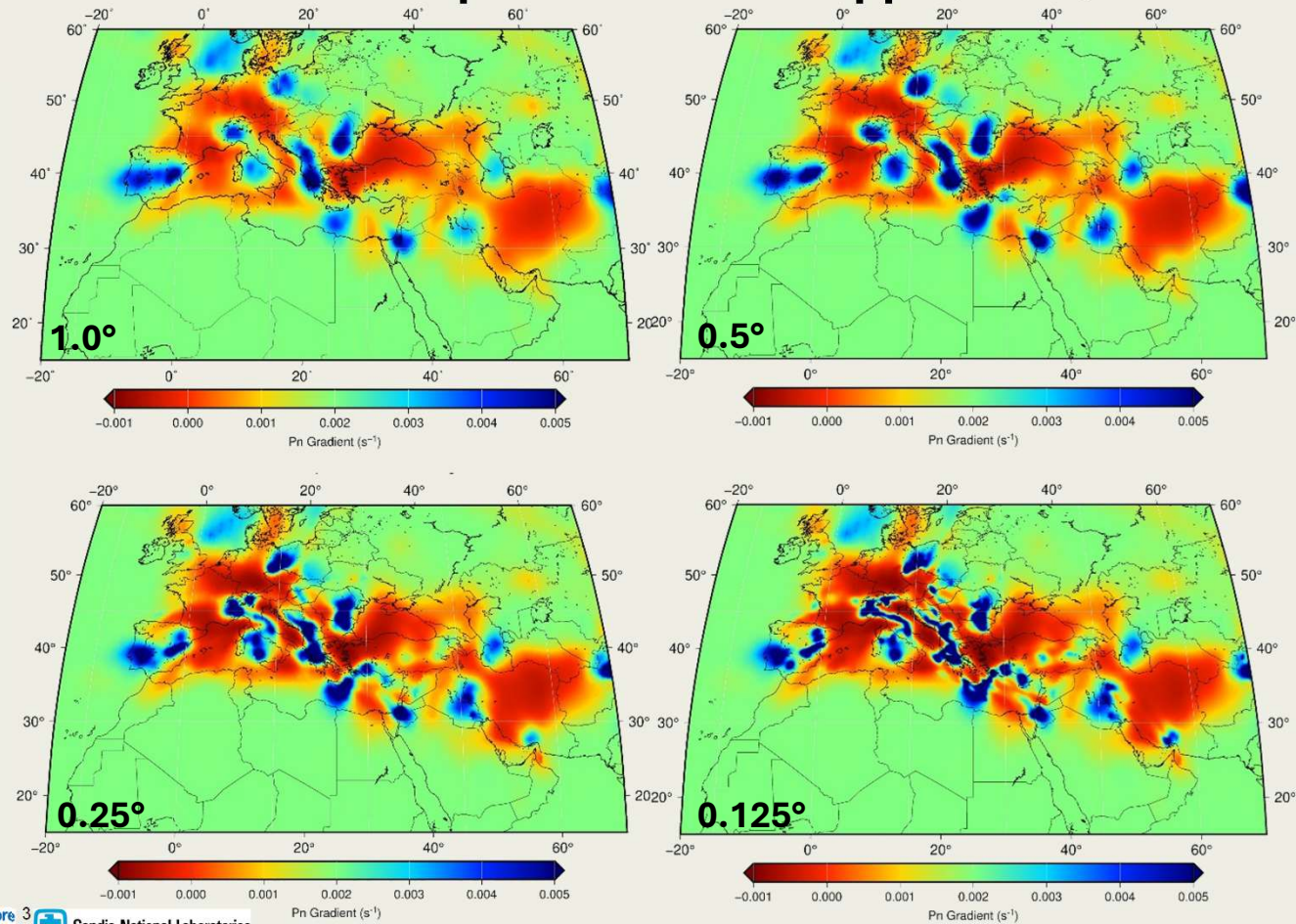
Grid Refinement in the Contiguous U.S.: Upper Mantle Pn Gradient



Grid Refinement in Europe/Middle East: Upper Mantle Pn Velocity

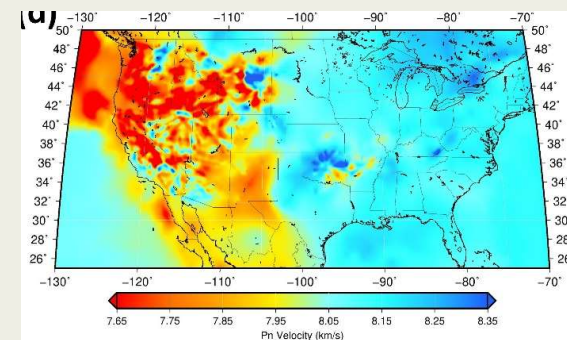
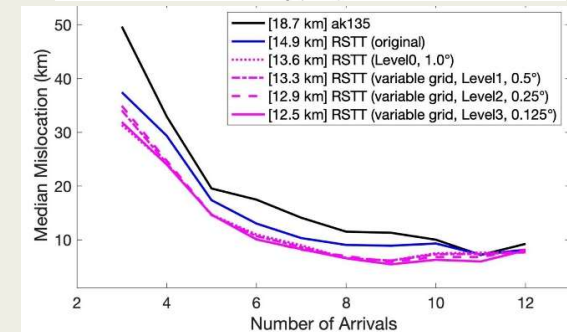
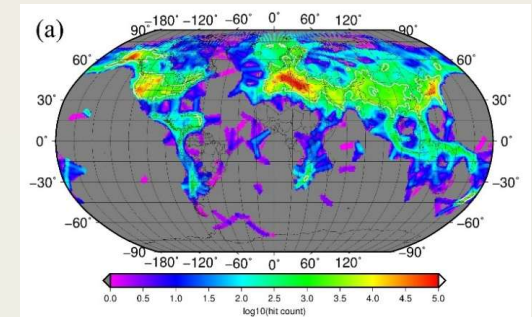


Grid Refinement in Europe/Middle East: Upper Mantle Pn Gradient



Conclusions

- High Pn ray density in the Western U.S., Europe and the Middle East, and East Asia enable systematic global grid refinement up to 0.125° (~ 14 km) using RSTT model.
- L-curve method was utilized to identify appropriate damping and smoothing values at each grid level.
- RSTT grid refinement improved the Pn travel time prediction by **33.5%** and **32.4% globally** and **Europe and the Middle East**, respectively, compared to *ak135* model.
- Smaller features are better delineated in the upper mantle velocity and gradient.
- Future work includes modeling Sn, Pg, and Lg using grid refinement.



Acknowledgements

- This research is supported by Ground-based Nuclear Detonation Detection (GNDD) and Office of Nuclear Verification research programs that are funded by the National Nuclear Security Administration (NNSA), Defense Nuclear Nonproliferation (NNSA DNN).
- The current RSTT model (pdu202009Du) used as the starting model for this study can be found and downloaded from <https://www.sandia.gov/rstt>.
- Seismic bulletin data were obtained from public sites (e.g., IDC Reviewed Event Bulletin, United States Geological Survey, International Seismological Centre).

