



Estimating Crustal Velocity Structure in Alaska from Acoustic-to-Seismic Coupling from the 2022 Hunga Eruption, Tonga

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Infrasound Technology Workshop

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Cleared for release





Motivation

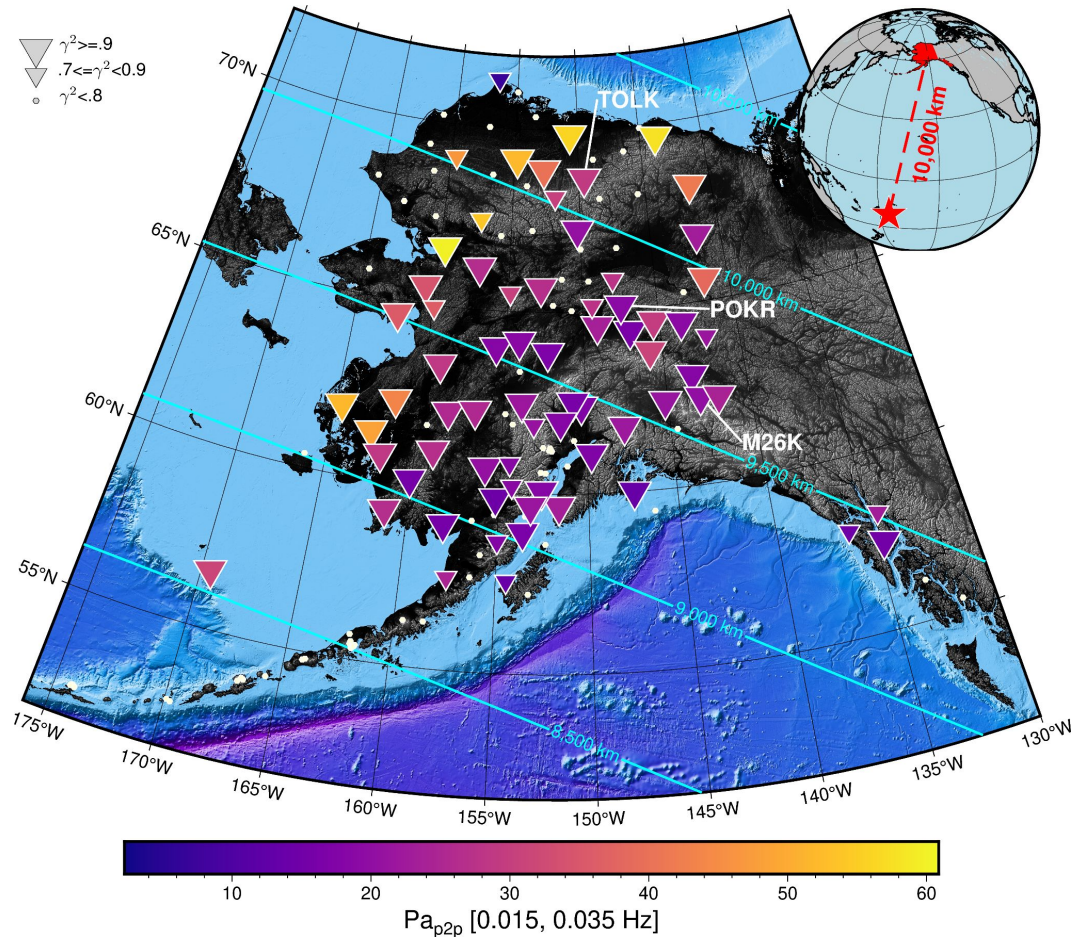
Use the once-in-a-lifetime source from the Hunga, Tonga eruption to examine crustal structure using acoustic-seismic coupling at deeper depths than is typically possible



Hunga, Tonga Infrasond in Alaska



- 150 stations equipped with colocated, broadband:
 - seismic (BH?)
 - infrasound (BDF)
 - barometer (BDO)
- Large pressure amplitudes (> 60.0 Pa) at huge offsets!

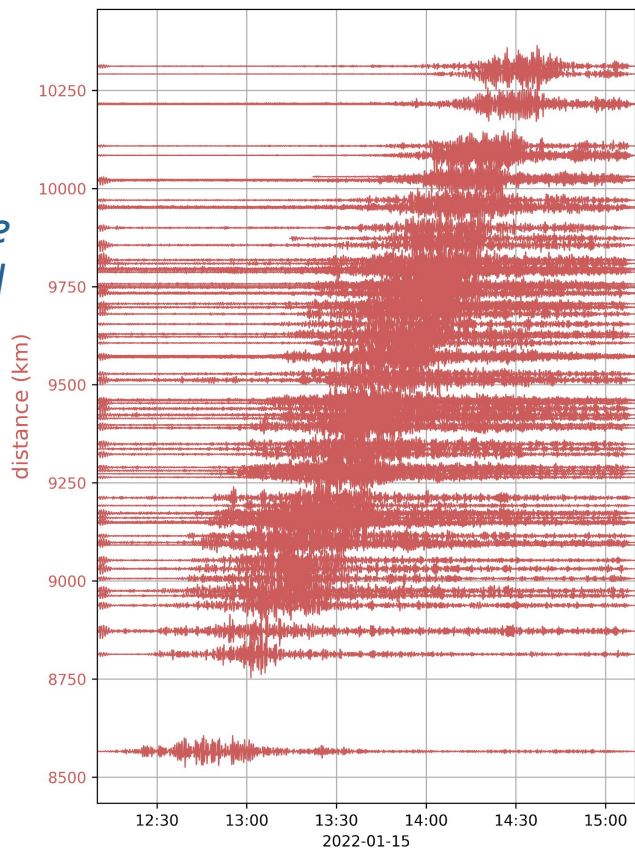




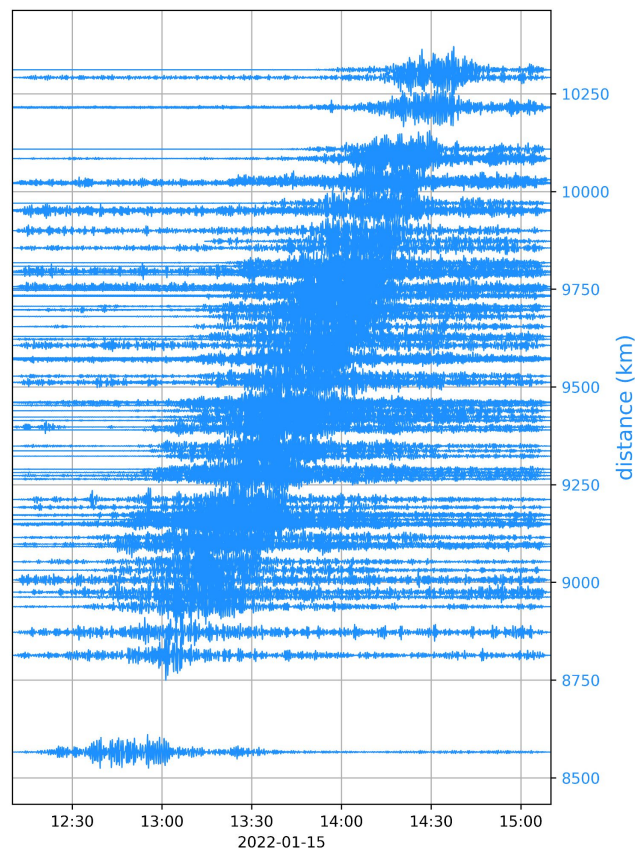
Pressure-to-Seismic Coupling

“A correlation has often been observed to exist between changes in the magnitude of the long-period seismic and atmospheric pressure fields”

– Sorrels, 1971



Infrasound (BDF)



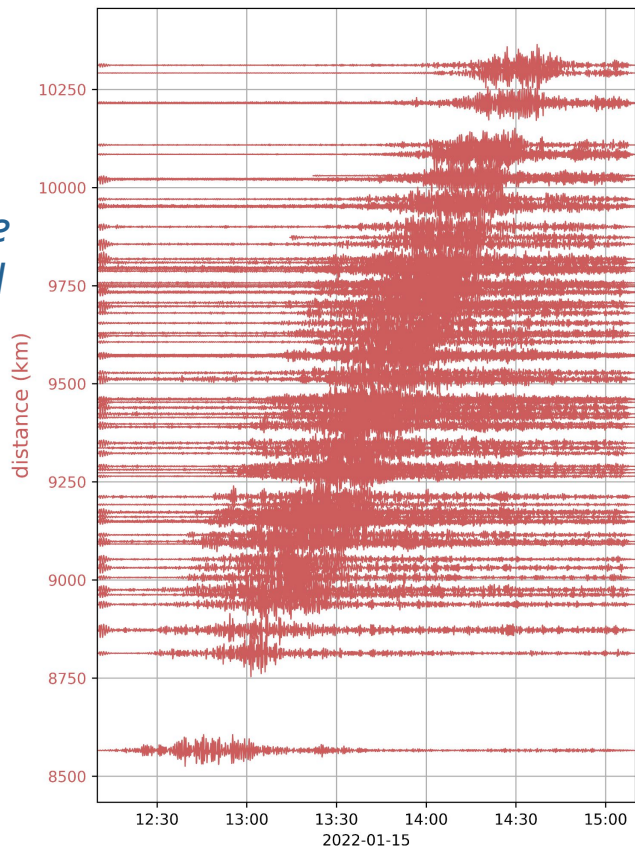
Seismic (BHZ)



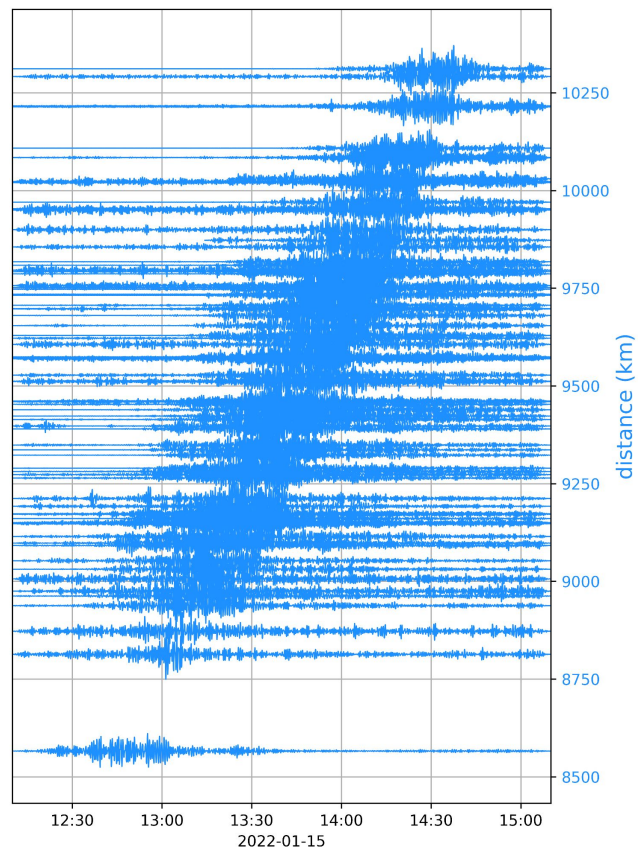
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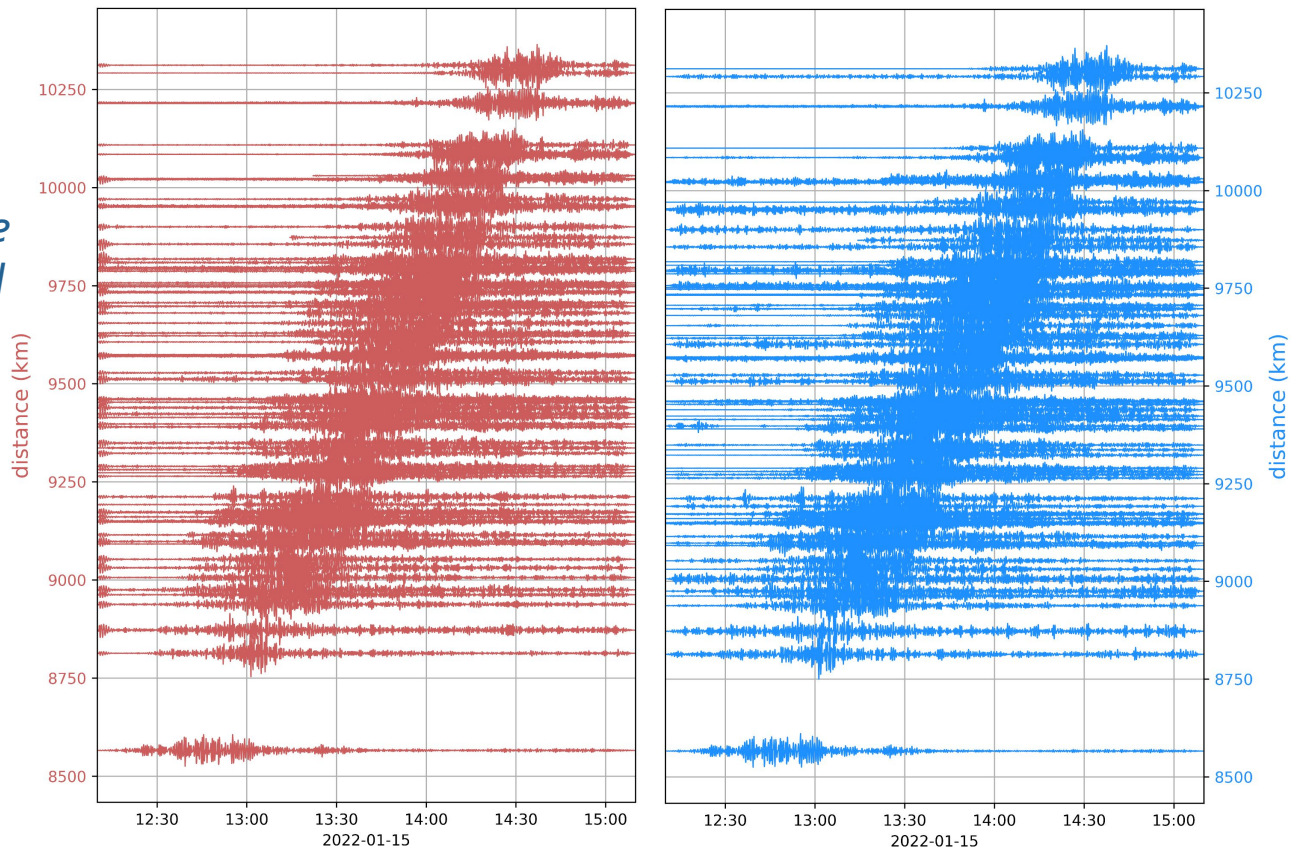
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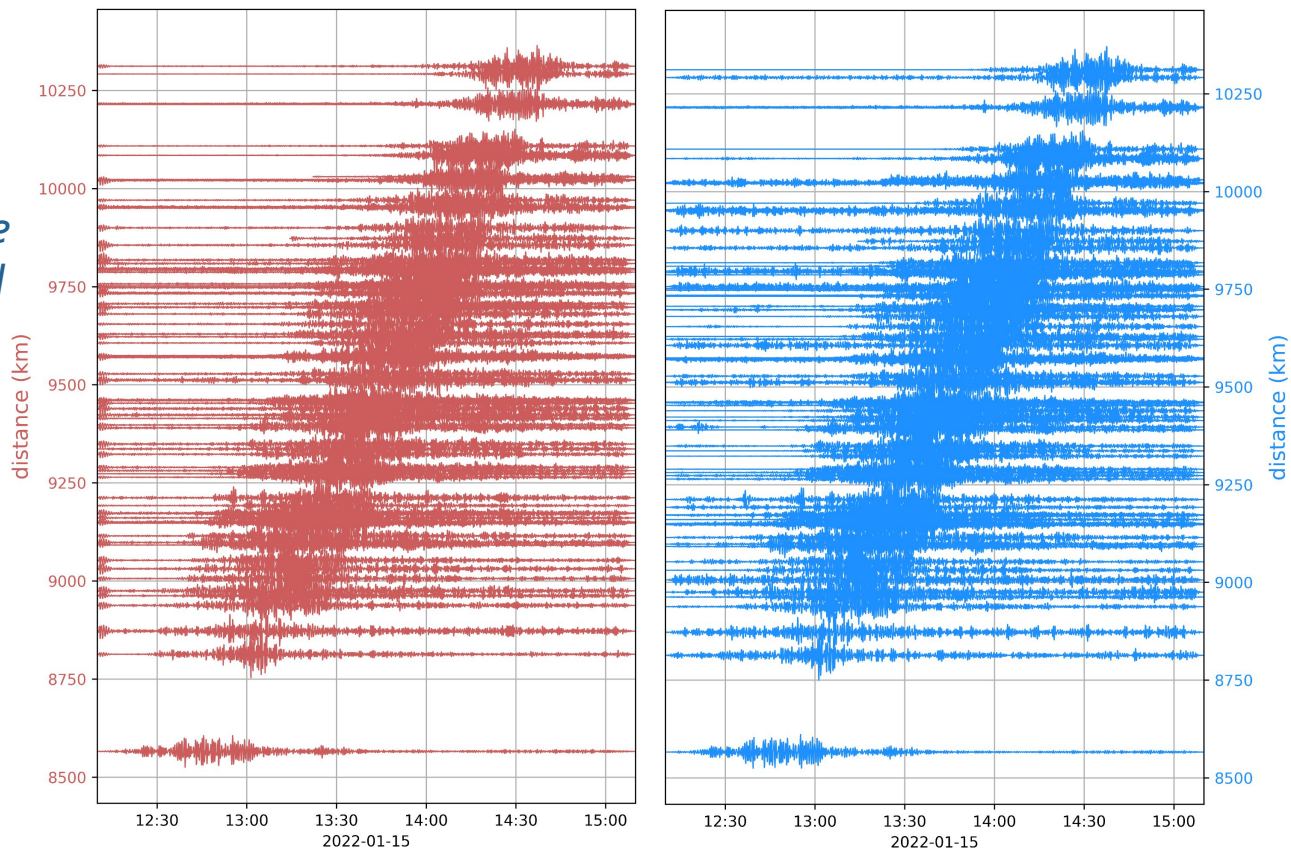
Infrasound (BDP) Seismic (BHZ)



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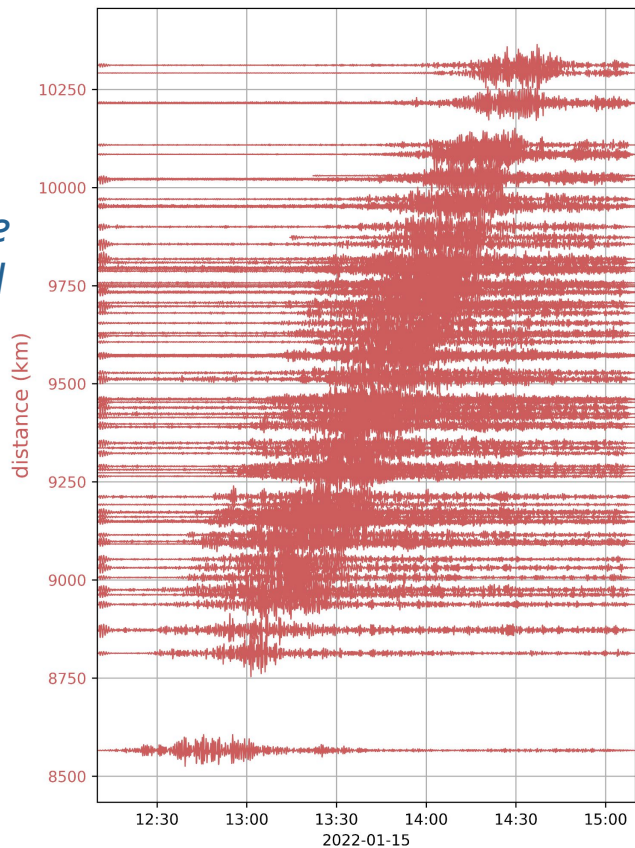
Seismic (BHZ) Infrasound (BDF)



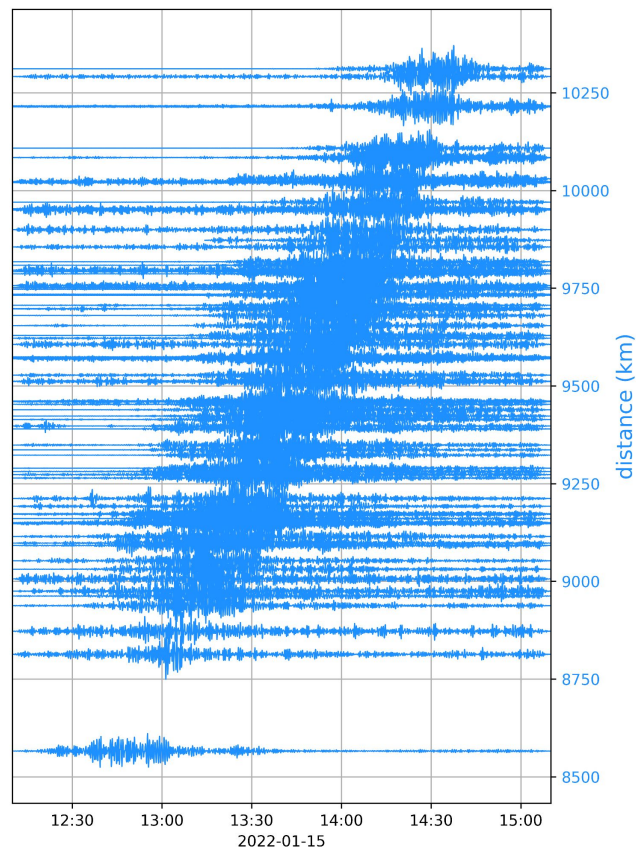
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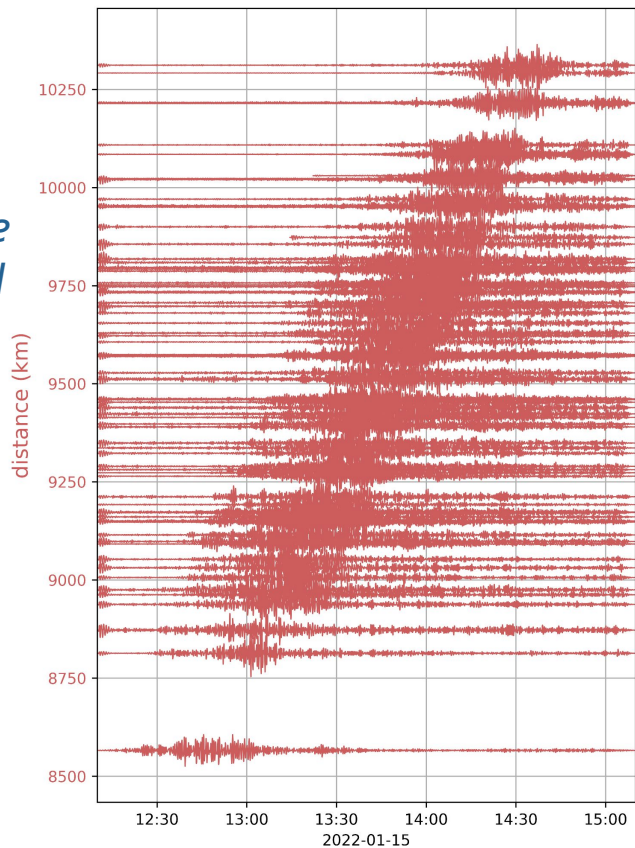
Infrasound (BDF)



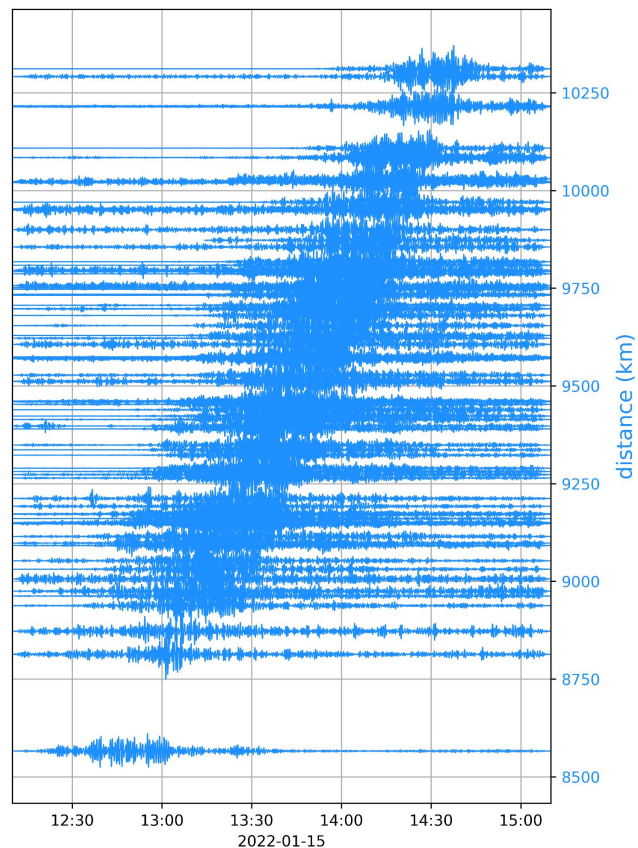
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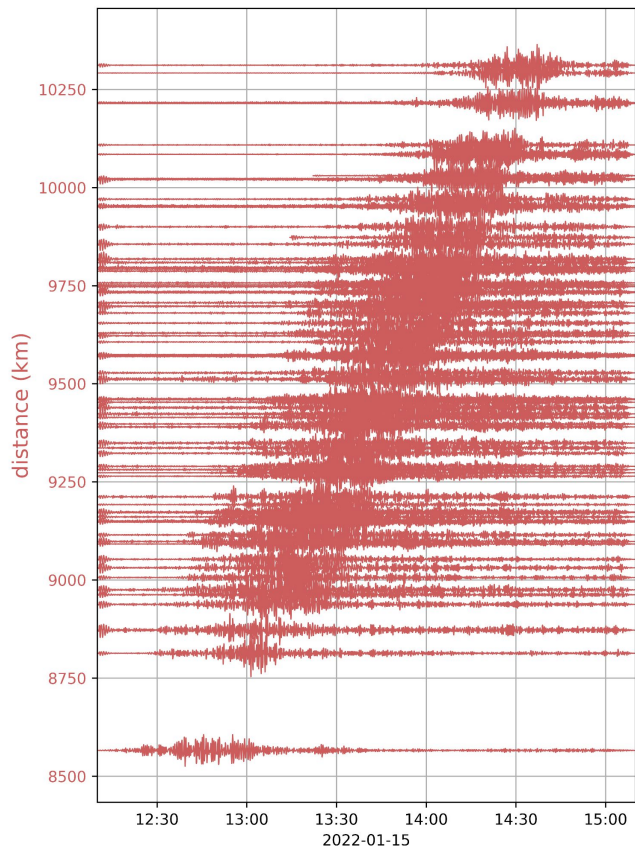
Infrasound (BDF)



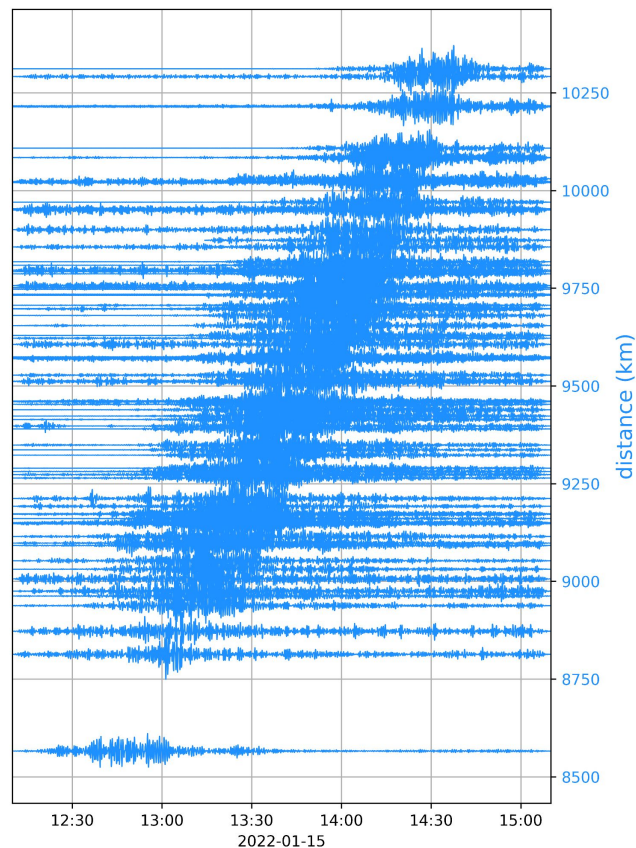
Pressure-to-Seismic Coupling

“...colocated data allow us to identify the frequency range of strong coupling between the atmosphere and the solid Earth and provide us information on how the solid Earth responds to surface pressure changes.”

—Tanimoto and Wang, 2018



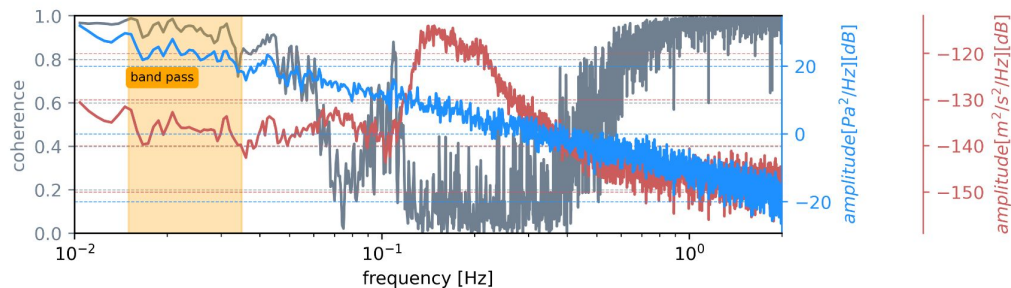
Seismic (BHZ)



Infrasound (BDF)



Data Selection



We choose bands with good coherence (> 0.8) between the seismic and pressure:

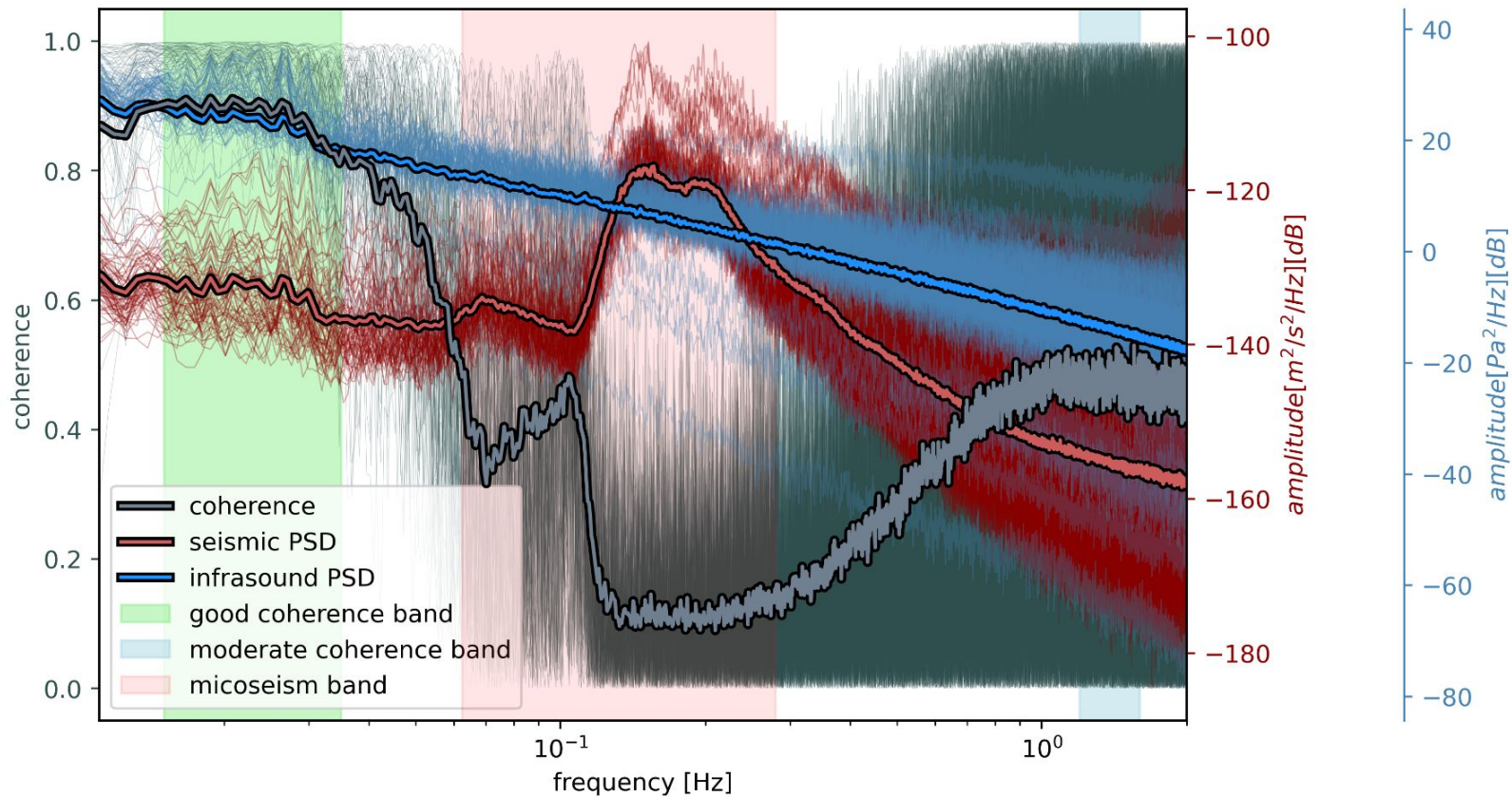
The magnitude squared coherence between the pressure and vertical seismic is:

$$\gamma^2 = \frac{\overline{G_{PS}}^2}{\overline{G_{PP}} \overline{G_{SS}}}$$

Where G_{PS} is the cross spectral density of the pressure and seismic, and G_{PP} and G_{SS} are the autospectral densities



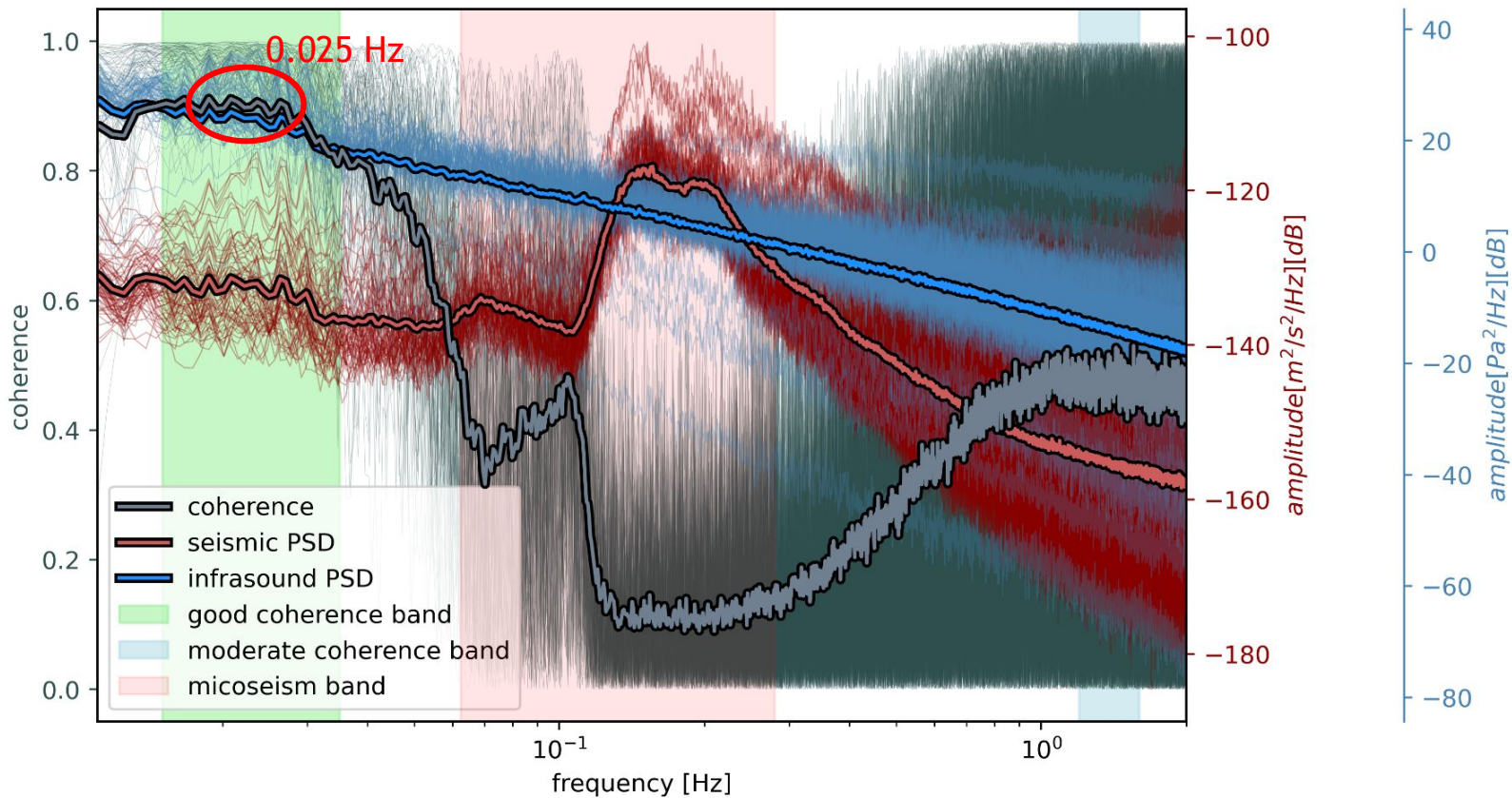
Network Coherence



Broadband infrasound and seismic

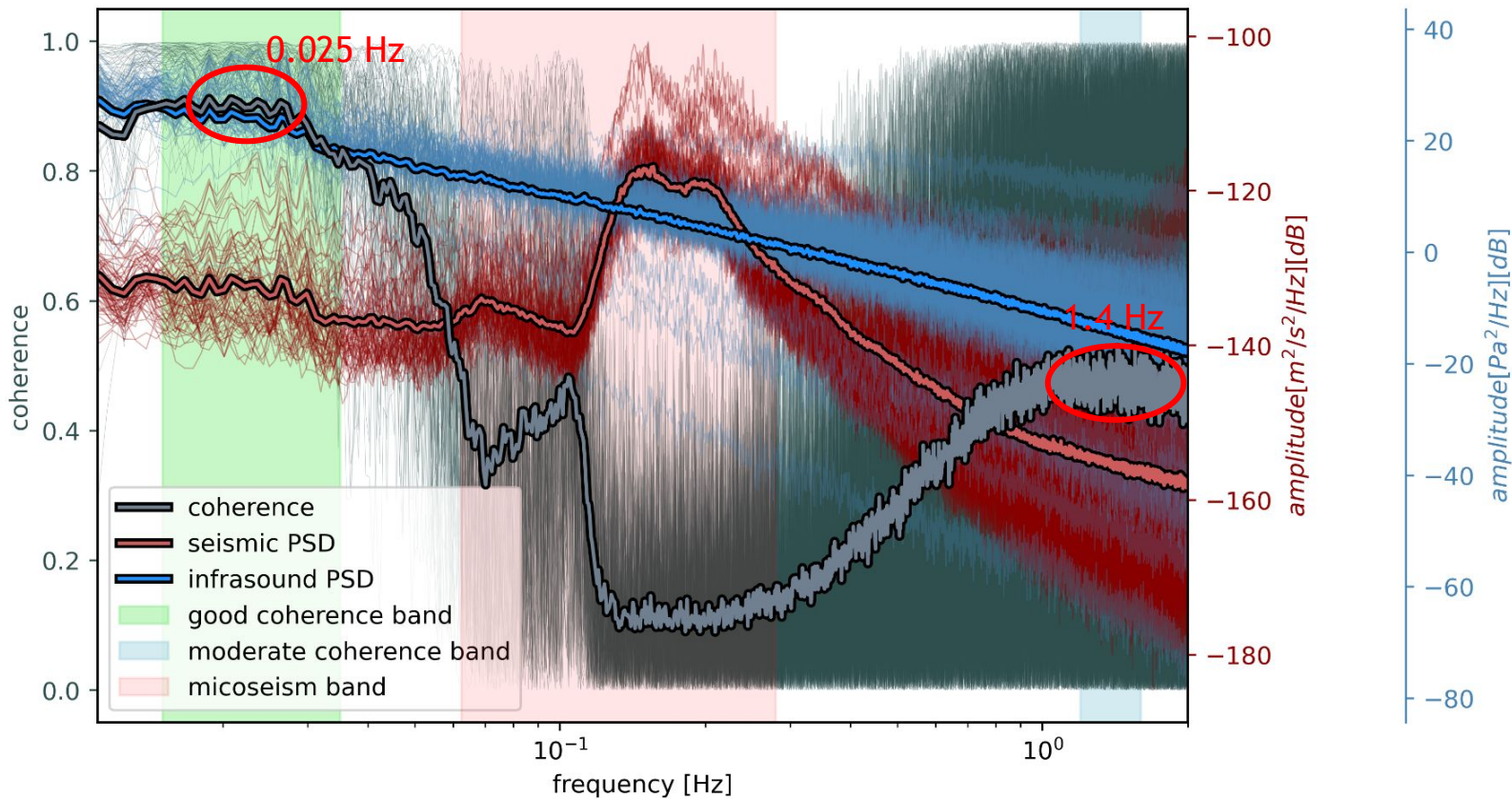


Network Coherence





Network Coherence





Coupling Calculation

Coupling spectra is simply the ratio of seismic amplitudes to infrasound amplitudes:

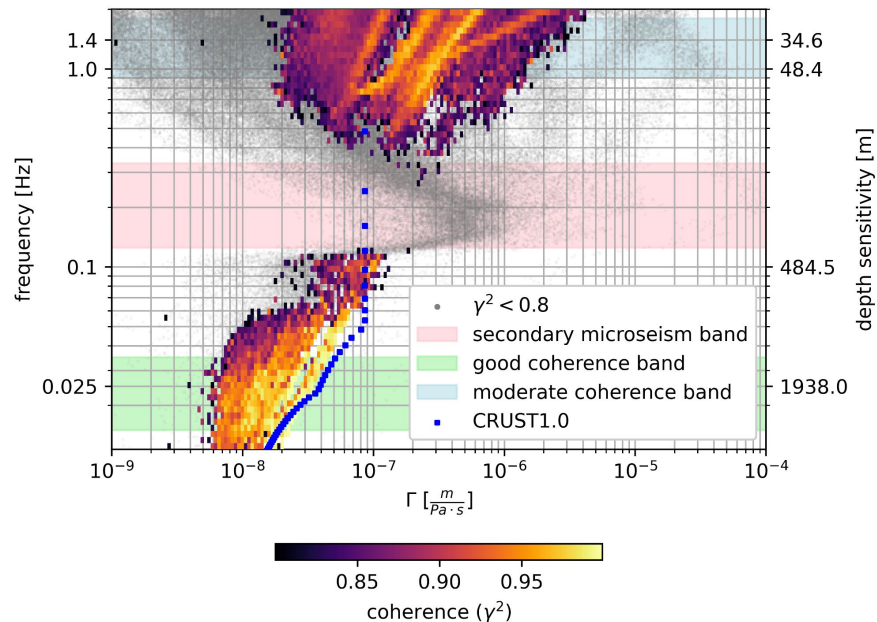
$$\Gamma(f) = \sqrt{\frac{PSD_s(f)}{PSD_p(f)}}$$

Where PSD_s and PSD_p are the seismic and pressure power spectral densities, respectively.

Also, a rule of thumb for the depth sensitivity of coupling to material parameters is give by;

$$h = 0.15 \cdot c \cdot T$$

Where h is depth, T is period, and c is the pressure source speed. (Tanimoto and Wang, 2019)





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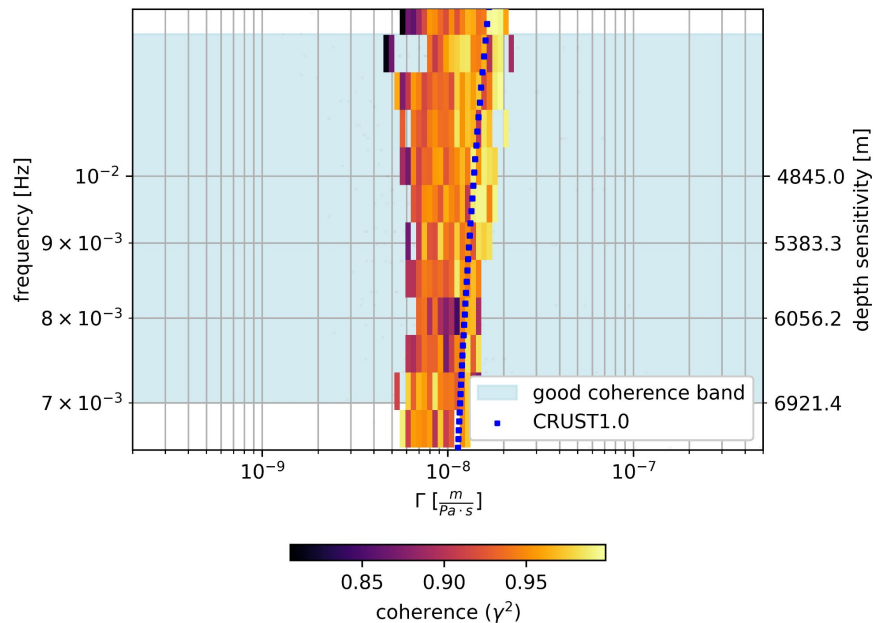
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~freq (Hz)	1.2-1.6	0.015 - 0.035	0.007 - 0.0125
~depth (km)	0.035	2.0	5.0

Relating Coupling to Elastic Parameters

$$\Gamma(f) = \sqrt{\frac{PSD_s(f)}{PSD_p(f)}} = \frac{c(\lambda + 2\mu)}{2\mu(\lambda + \mu)}$$

Where c is sound speed and λ and μ are the first Lamé' parameter and rigidity, respectively (Sorrels, 1971)

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$$\bar{\mu} = \frac{\lambda + \mu}{\lambda + 2\mu} \mu$$

Estimating Near-Surface Rigidity from
Low-Frequency Noise Using Collocated
Pressure and Horizontal Seismic Data

Jiong Wang¹ and Toshiro Tanimoto²

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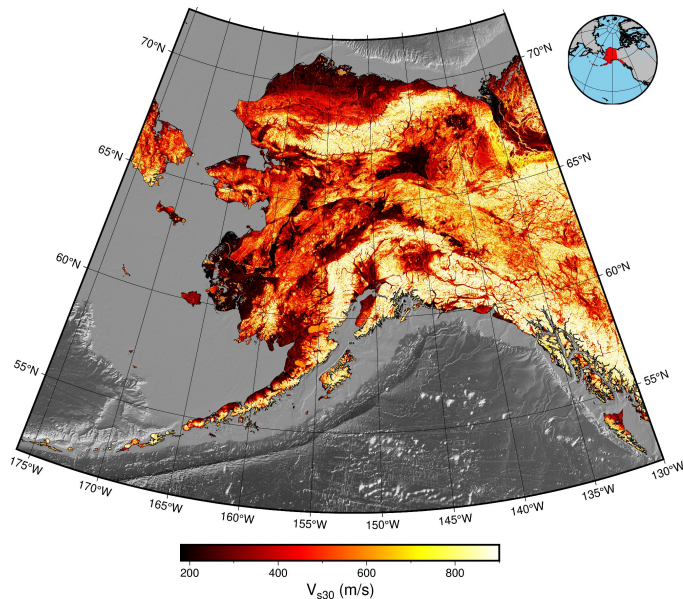
$$\bar{\mu} = \frac{c}{2\Gamma(f)}$$

$$V_s = \sqrt{\frac{\bar{\mu}}{\rho_{mod}}}$$

where ρ_{mod} is a depth-averaged density estimate from CRUST1.0

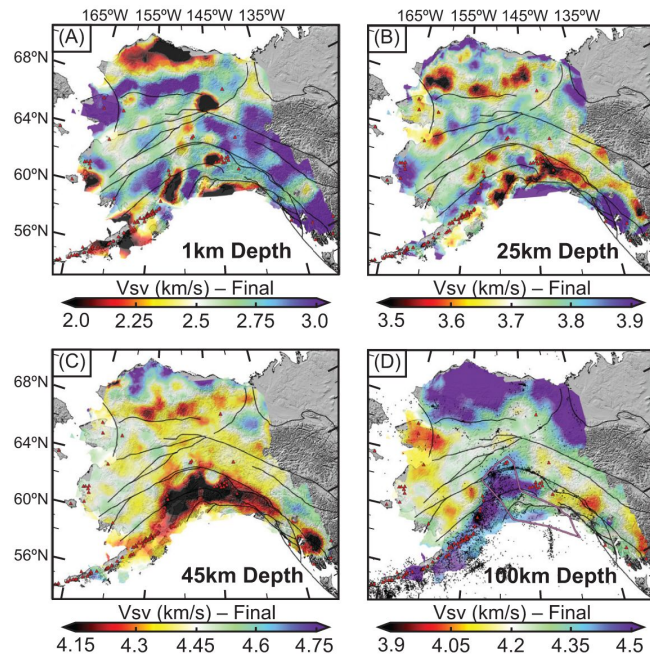


Compare to existing models:



1.4 Hz (35 m)

Model: USGS proxy V_{s30} (Allen and Wald, 2007)

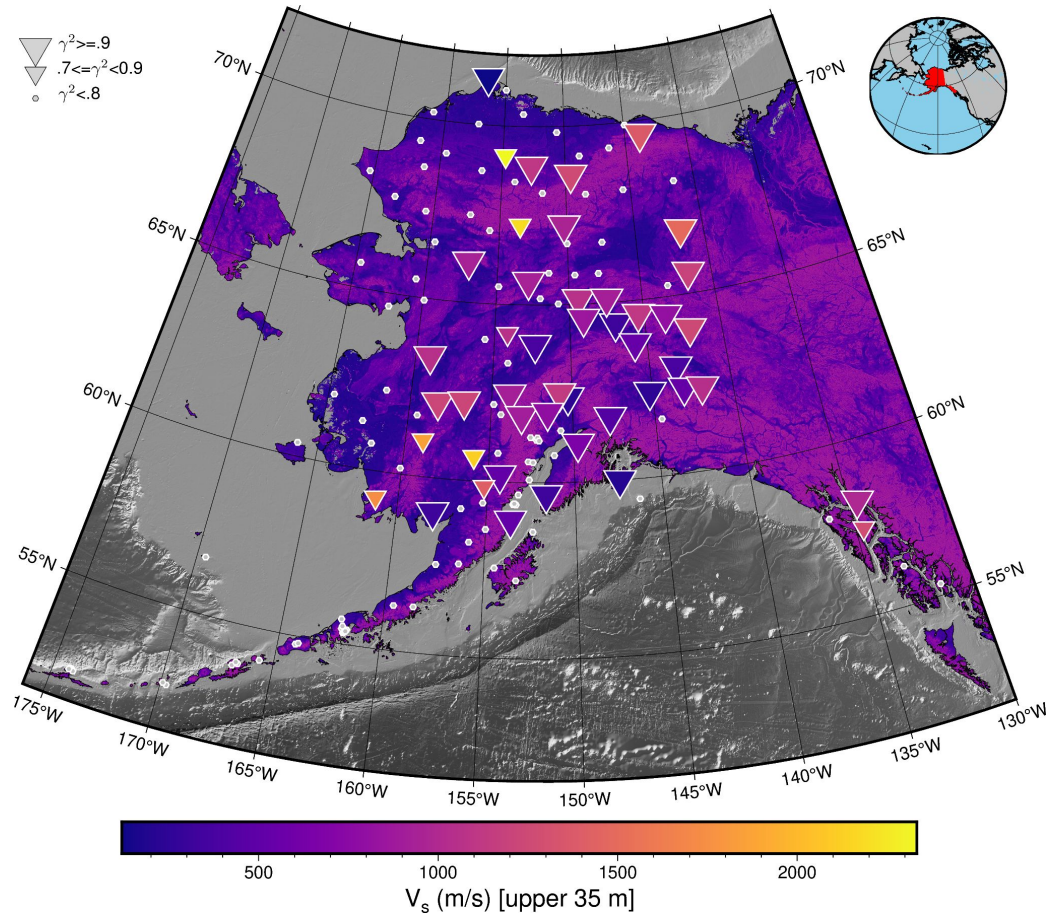
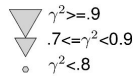
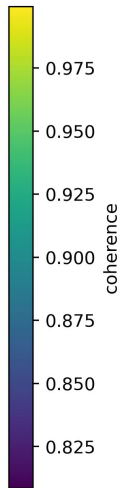
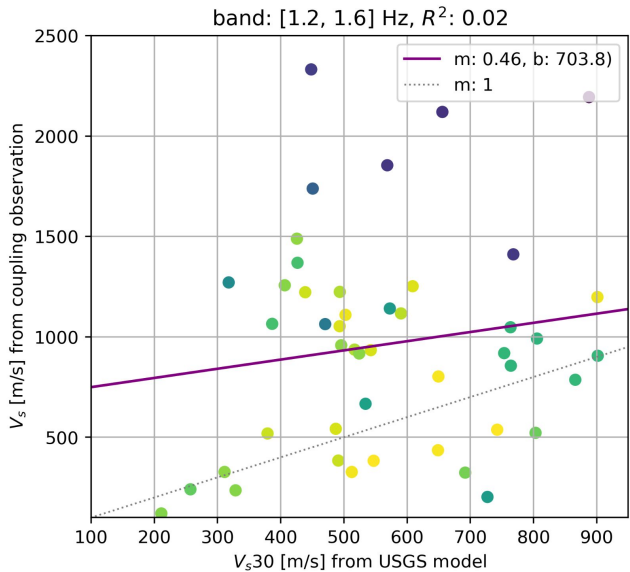


0.025 Hz (2.0 km) and 0.00975 Hz (5.0 km)

Model: tomographic (Berg, *et al.*, 2020)

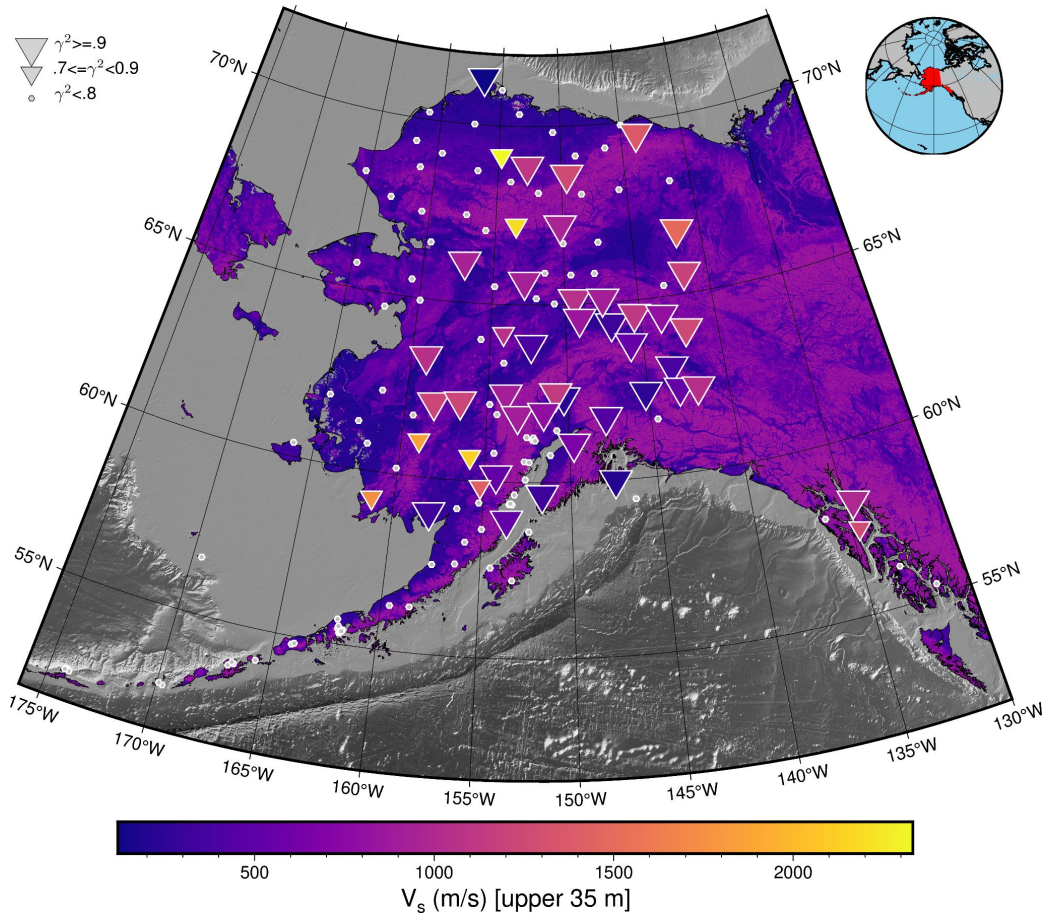
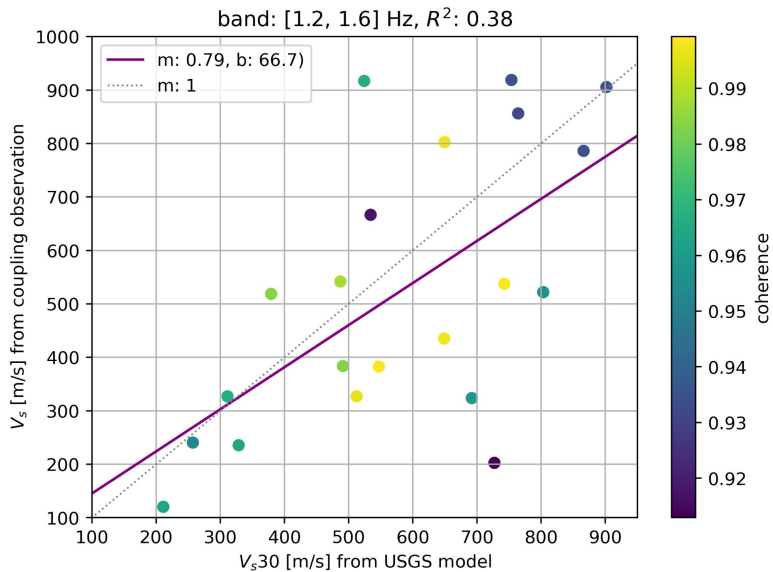
Depth-averaged to appropriate depth

Results: Mean V_s for Upper 35 m (~1.4 Hz)



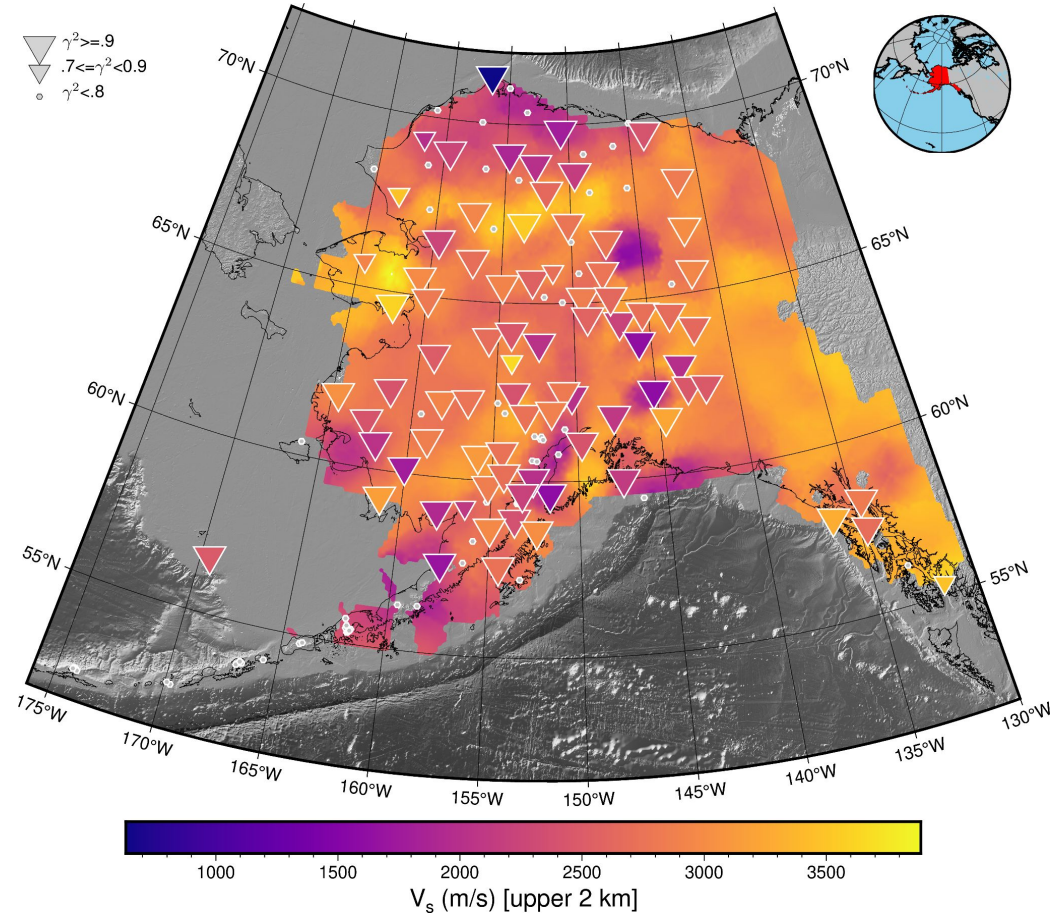
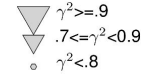
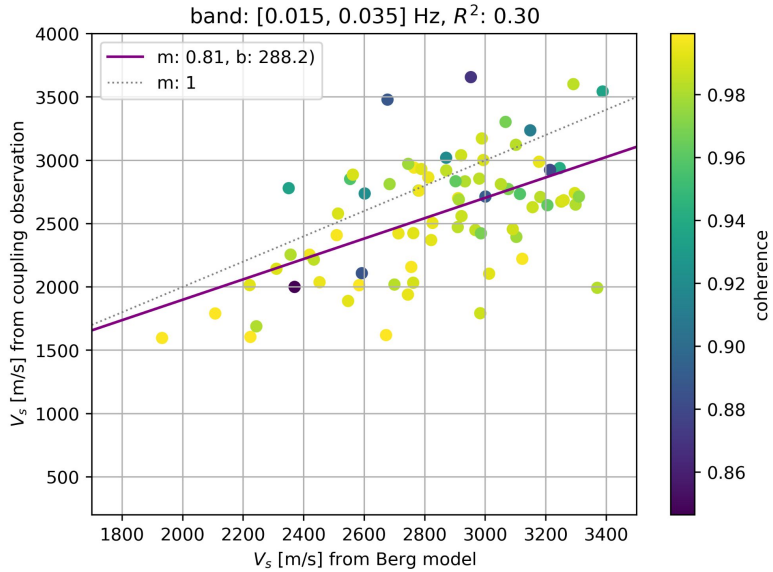
Background model from USGS
global proxy V_{s30}

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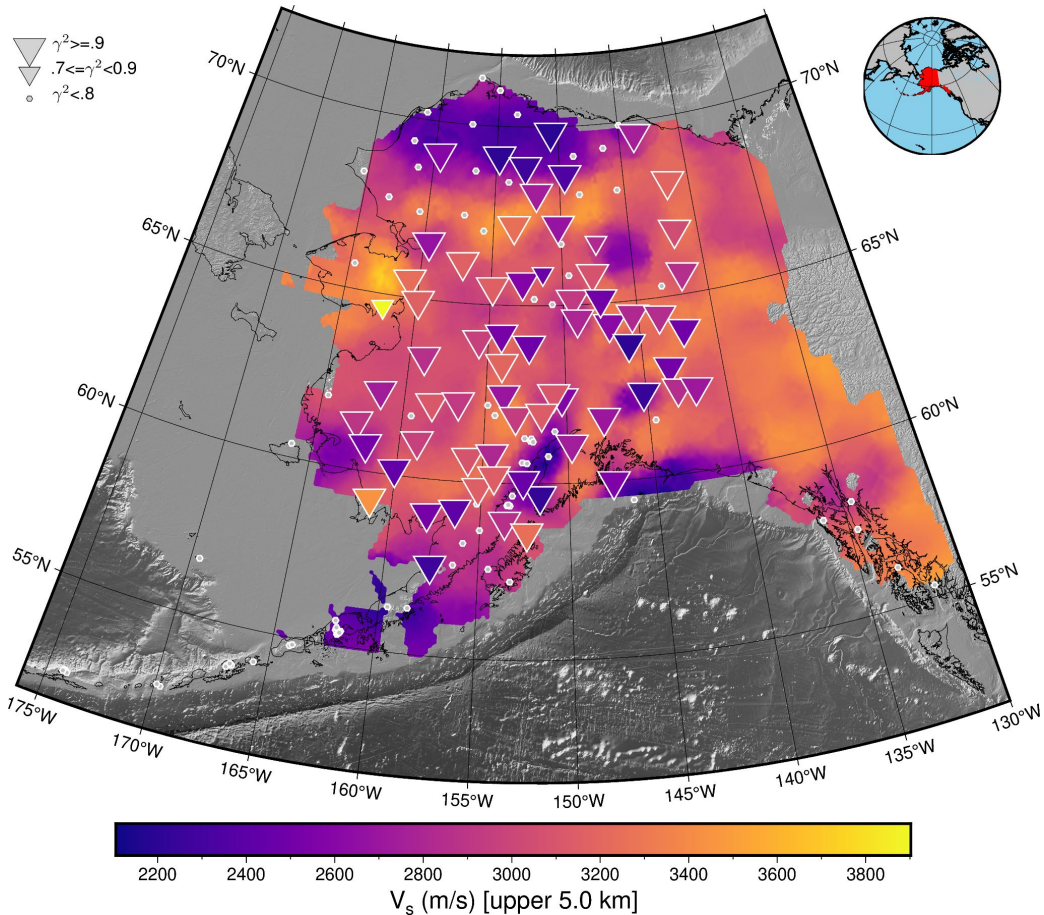
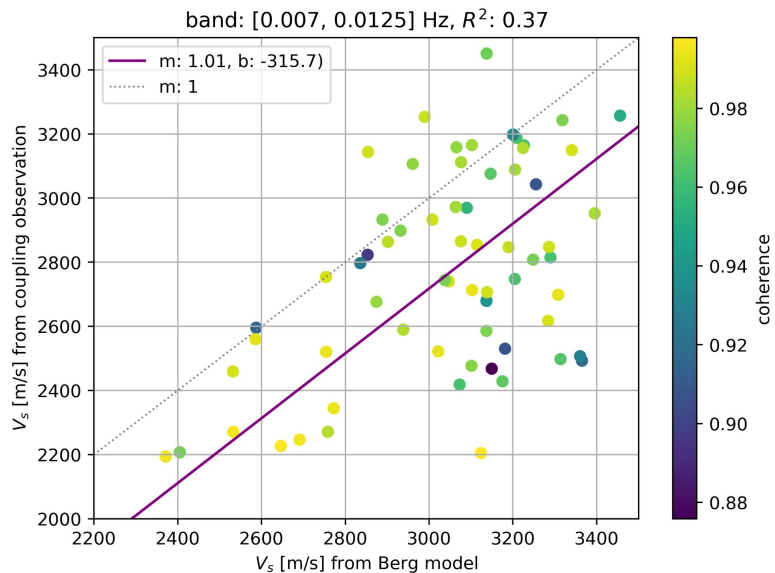
Results: Mean V_s for Upper 2.0 km (~0.025 Hz)



Background tomographic model
from Berg, *et al.*, 2020 (depth
averages)



Results: Mean V_s for Upper 5.0 km (~0.00975 Hz)



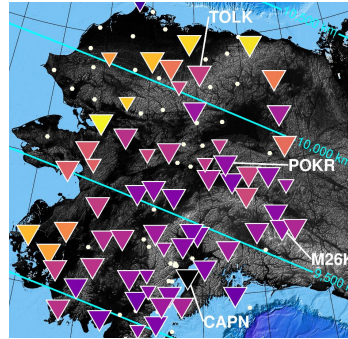
Background tomographic model
from Berg, *et al.*, 2020 (depth
averages)



Results: Comparison with 2013 Chelyabinsk Bolide

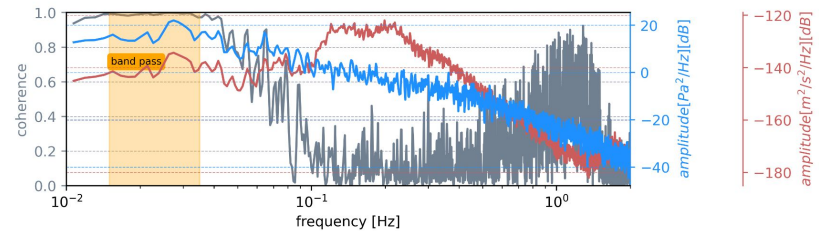
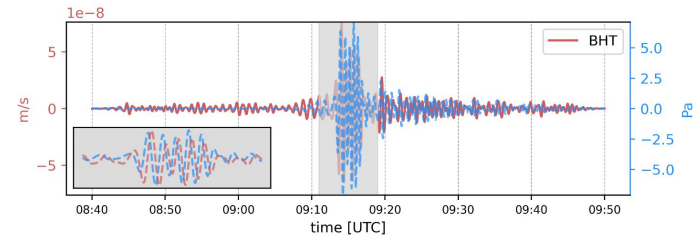
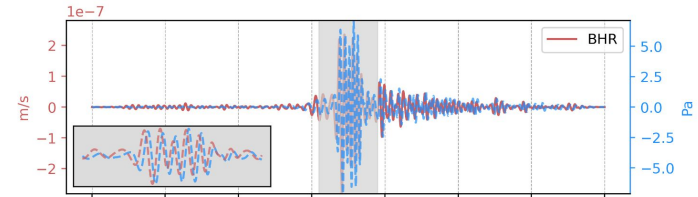
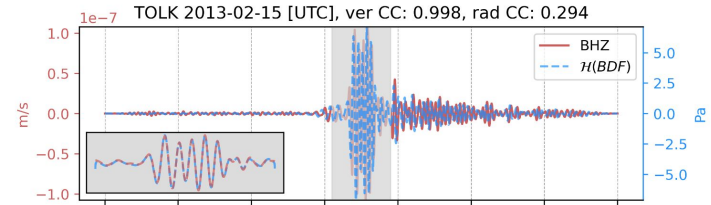


Photo: Alex Alishevskikh



V_S (m/s) at 2.0 km

	Hunga	Chely	% diff
POKR	2630	2645	0.6
TOLK	2158	2156	0.08





Conclusions:

- Pressure waves from the Hunga, Tonga eruption produced air-to-ground coupled waves that were beautifully recorded in Alaska
- Microseismic amplitudes generally exceed coupled seismic amplitudes
- Coupling was inversely proportional to the rigidity of the elastic medium, and this was used to estimate bulk V_s
- **Successful estimate of mean V_s to depths of:**
 - **35 m**
 - **2.0 km**
 - **5.0 km**

Select References:

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Thank You! Questions or Comments?

